



1. For a direct-mapped cache design with a 32-bit address, the following bits of the address are used to access the cache.

Tag	Index	Byte offset
31-16	15-4	3-0

- (a) How many entries does the whole cache have? (5%)
- (b) In the whole cache, how many bits are used to store tag information? (5%)
2. What were the two major motivations for virtual memory? (5%)
- (a) Remove the programming burdens of a small, limited amount of main memory.
- (b) Enhance task-level and process-level parallelism.
- (c) Allow efficient and safe sharing of memory among multiple programs.
- (d) Reduce the miss rate of a cache.
3. For an 8-bit CPU, what is two's complement representation of -4? (5%)
4. Let processes P_1 , P_2 , P_3 and P_4 arrive at time 0. The length of CPU burst time of P_1 , P_2 , P_3 and P_4 is 6, 8, 7 and 3 respectively. Assuming that the shortest-job-first (SJF) scheduling algorithm is adopted to schedule these processes. What is the average waiting time? (5%)
5. Processes P_1 and P_2 are periodic tasks. P_1 has a period of 50 and a CPU burst time of 25. On the other hand, P_2 has a period of 80 and a CPU burst time of 20. What is the total CPU utilization of the two processes? (5%)
6. Suppose that a process is executing "counter = counter + 1" while another process is executing concurrently and independently "counter = counter - 2", where the counter is a variable shared between the two processes and is accessed only by these two statements once. Given that the initial value of counter is 5 before execution, please list all possible values of counter after both processes finish. (5%) (提示：共有三種情況，全對才給分，任一個錯誤零分)
7. How many processes are created by the following program? (5%)

```

#include <stdio.h>
#include <unistd.h>
int main()
{
    int i;
    for (i = 0; i < 4; i++)
        fork();

    return 0;
}

```



8. For the following program, what the output will be at lines C and P? (10%)

```

#include <pthread.h>
#include <stdio.h>
int value = 100;
void *runner(void *param); /* the thread */
int main(int argc, char *argv[])
{
    pid_t pid;
    pthread_t tid;
    pthread_attr_t attr;
    pid = fork();
    if (pid == 0) {
        pthread_attr_t attr;
        pthread_create(&tid, &attr, runner, NULL);
        pthread_join(tid, NULL);
        printf("CHILD: value = %d", value); /* LINE C */
    }
    else if (pid > 0) {
        wait(NULL);
        printf("PARENT: value = %d", value); /* LINE P */
    }
}
void *runner(void *param) {
    value = 50;
    pthread_exit(0);
}

```

9. In how many ways can one travel in the xy-plane from $(-1, 5)$ to $(-5, -2)$ if each move is one of the following three types(10%)

W: $(x, y) \rightarrow (x - 1, y)$,

S: $(x, y) \rightarrow (x, y - 1)$, and

SW: $(x, y) \rightarrow (x - 1, y - 1)$?

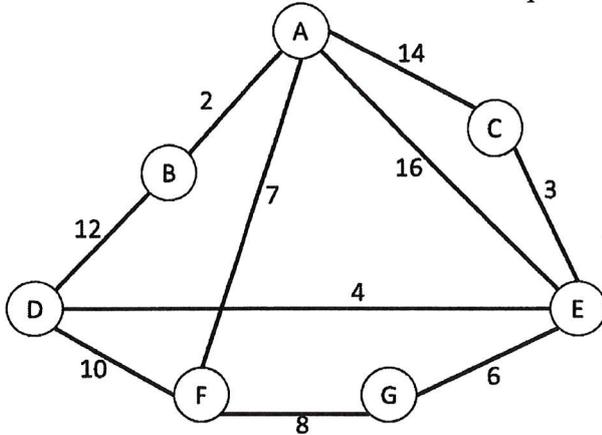
10. Let F_n denote the nth Fibonacci number, and $F_n = F_{n-1} + F_{n-2}$. Find the smallest Fibonacci number (>1), which is a perfect square.(10%)



11. Let $\mathbf{u} = (1, 1, 1)$ and $\mathbf{a} = (0, 2, -1)$.

- (a) Find the vector component of \mathbf{u} along \mathbf{a} .(5%)
 (b) Find the vector component of \mathbf{u} orthogonal to \mathbf{a} .(5%)

12. What is the cost of minimum cost spanning tree of the given graph?(10%)



13. Ackerman's function $A(m, n)$ is defined as below:

$$A(m, n) = \begin{cases} n + 1 & \text{if } m = 0 \\ A(m - 1, 1) & \text{if } n = 0 \\ A(m - 1, A(m, n - 1)) & \text{otherwise} \end{cases}$$

- (a) What is the value of $A(2, 1)$?(5%)
 (b) Write a recursive program to calculate $A(m, n)$.(5%)