題號: 335 國立臺灣大學111學年度碩士班招生考試試題

科目: 財務管理與財金數學

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第一部分:回答下列 6 題單選題,每題 10 分。作答於答案卡上。 第二部分(填空題):第7~10 題,請於制式試卷(答案本)上作答,"需列出"計算過程

第一部分:單選題

1. Let  $\tilde{y} = e^{\tilde{x}}$ , where  $\tilde{x}$  is normally distributed with mean  $\mu$  and variance  $\sigma^2$ .

What is the value of  $\frac{\text{stdev}(\tilde{y})}{E[\tilde{y}]}$ ?

a. 
$$\sqrt{e^{\sigma^2}-1}$$
 b.  $\sqrt{e^{2\sigma}-1}$  c.  $\sqrt{2e^{2\sigma}-1}$  d.  $\sqrt{e^{2\sigma}-2}$ 

[2, 3, 4] Suppose there are three possible states of the world which are equally likely, so  $\Omega = \{\omega_1, \omega_2, \omega_3\}$  with  $\mathbb{P}(\{\omega_1\}) = \mathbb{P}(\{\omega_2\}) = \mathbb{P}(\{\omega_3\}) = 1/3$ . Let  $\mathcal{G}$  be the collection of all subsets of  $\Omega$ :

$$\mathcal{G} \ = \ \{\emptyset, \{\omega_1\}, \{\omega_2\}, \{\omega_3\}, \{\omega_1, \omega_2\}, \{\omega_1, \omega_3\}, \{\omega_2, \omega_3\}, \Omega\}.$$

Let  $\tilde{x}$  and  $\tilde{y}$  be random variables, and set  $a_i = \tilde{x}(\omega_i)$  for i = 1, 2, 3. Assume no two of the  $a_i$  are the same. Suppose  $\tilde{y}(\omega_1) = b_1$  and  $\tilde{y}(\omega_2) = \tilde{y}(\omega_3) = b_2 \neq b_1$ .

- 2. Which of the following statement is not correct?
- a.  $\operatorname{prob}(\tilde{x} = a_1 | \tilde{y} = b_1) = 1$
- b.  $\operatorname{prob}(\tilde{x} = a_2 | \tilde{y} = b_1) = 0$
- c.  $\operatorname{prob}(\tilde{x} = a_2 | \tilde{y} = b_2) = 1$
- d.  $\operatorname{prob}(\tilde{x} = a_1 | \tilde{y} = b_2) = 0$
- 3. Which of the following statement is correct?
- a.  $E(\tilde{x}|\tilde{y}=b_1)=a_1$
- b.  $E(\tilde{x}|\tilde{y}=b_2)=a_2$
- c.  $E(\tilde{x}|\tilde{y}=b_1)=(a_1+a_2)/2$
- d.  $E(\tilde{x}|\tilde{y}=b_2)=(a_1+a_3)/2$
- 4. What is the  $\sigma$ -field generated by  $\tilde{y}$ ?
- a.  $\{\emptyset, \{\omega_1\}, \{\omega_2\}, \{\omega_3\}, \{\omega_1, \omega_2\}, \{\omega_1, \omega_3\}, \{\omega_2, \omega_3\}, \Omega\}$
- b.  $\{\emptyset, \{\omega_1\}, \{\omega_2\}, \{\omega_3\}, \Omega\}$
- c.  $\{\emptyset, \{\omega_1\}, \{\omega_2, \omega_3\}, \Omega\}$

## 見背面

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d. 
$$\{\emptyset, \{\omega_1, \omega_2\}, \{\omega_3\}, \Omega\}$$

5. Assume X is an Itô process. Which of the following statement is not correct?

(a) Define 
$$Y_t = e^{Xt}$$
, then  $\frac{dY}{Y} = dX + \frac{1}{2}(dX)^2$ 

- (b) Assume X is strictly positive. Define  $Y_t = \log X_t$ , then  $dY = \frac{dX}{X} \frac{1}{2} \left(\frac{dX}{X}\right)^2$
- (c) Assume X is strictly positive. Define  $Y_t = X_t^{-\lambda}$  for a constant  $\lambda$ , then  $\frac{dY}{Y} = -\lambda \frac{dX}{X} + \frac{\lambda(1+\lambda)}{2} \left(\frac{dX}{X}\right)^2$
- (d) Assume S is a geometric Brownian motion:  $\frac{dS}{S} = \mu dt + \sigma dB$ , for constants  $\mu$  and  $\sigma$  and a Brownian motion B, then  $var_t\left(\frac{S_{t+1}}{S_t}\right) = e^{2\mu}\left(e^{2\sigma} 1\right)$
- 6. Which of the following statement is not correct
- (a) Assume  $X_t = \theta e^{-\kappa t}(\theta X_0) + \sigma \int_0^t e^{-\kappa (t-s)} dB_s$  for a Brownian motion B and constants  $\theta$  and  $\kappa$ , then  $dX = -\kappa X dt + \sigma dB$
- (b) Assume  $dX = -\kappa X dt + \sigma dB$  for constants  $\kappa$  and  $\sigma$ . Set  $Y = X^2$ , then  $dY = \hat{\kappa} (\hat{\theta} Y) dt + \hat{\sigma} \sqrt{Y} dB$ , for constants  $\hat{\kappa}$ ,  $\hat{\theta}$  and  $\hat{\sigma}$ .
- (c) Let B be a Brownian motion. Define  $Y_t = B_t^2 t$ , then Y is a martingale.
- (d) Let  $dM = \theta dB$  for a Brownian motion B, then  $M_t^2 \int_0^t (dM_s)^2$  is a local martingale.

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第二部分:填空題(共四十分。每題10分)

注意事項:

※※所有問題均請詳列計算過程,若只有答案將不予計分※※

※※填空題題型請至少計算至小數點後第二位※※

※※答案請於答案卷(本)上標示清楚,如 ANS:\_\_\_XXXXXX\_\_\_\_※※

※※一律作答於所附之考試答案卷(本)上。若於試題卷上作答者,將不予計分 ※※

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(7)	(7)之答案與計算過程	1110
(8)	(8)之答案與計算過程	
(9)	(9)之答案與計算過程	
(10)	(10)之答案與計算過程	

- 7. Your firm is planning to invest in a new electrostatic power generation system that is all equity financed. Hoothoot Inc. is a firm that specializes in this business. Hoothoot has a stock price of \$30 per share with 15 million shares outstanding. Hoothoot's equity beta is 2.11. It also has \$350 million in debt outstanding with a debt beta of 0.03. If the risk-free rate is 2.5%, and the market risk premium is 11%, then your estimate of your cost of capital for electrostatic power generators is close to: ANS:
- 8. You expect that MIT Enterprise will have earnings per share of \$2.8 for the coming year. MIT plans to retain all of its earnings for the next three years. For the subsequent two years, the firm plans on retaining 25% of its earnings. It will then retain only 10% of its earnings from that point forward. Retained earnings will be invested in projects with an expected return of 12% per year. If MIT's equity cost of capital is 9%, then the price of a share of MIT's stock is close to: ANS:
- 9. After graduation, you plan to work for Glalie Corp. for 12 years and then start your own business. You expect to save and deposit \$5,000 a year for the first 6 years and \$19,000 annually for the following 6 years. The first deposit will be made a year from today. In addition, your aunt just gave you a \$60,000 graduation gift which you will deposit immediately. If the account earns 8.5% compounded annually, how much will you have when you start your business 12 years from now? ANS:

## 見背面

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10. Tesla Food Company is considering a new salsa whose data are shown below. The equipment to be used would be depreciated by the straight-line method over its 3-year life and would have a zero salvage value, and no change in net operating working capital would be required. Revenues and other operating costs are expected to be constant over the project's 3-year life. However, this project would compete with other Tesla products and would reduce their pre-tax annual cash flows. What is the project's NPV? ANS:

WACC	11%
Pre-tax cash flow reduction for other products (cannibalization)	\$6,000
Investment cost (depreciable basis)	\$99,000
Annual sales revenues	\$70,000
Annual operating costs (excl. depreciation)	\$20,000
Tax rate	40%

試題隨卷繳回