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國立臺灣大學 111 學年度碩士班招生考試試題

科目：統計學(E)

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1. The following statistics were calculated based on samples drawn from four normal populations:

Statistic	Treatment			
	1	2	3	4
n_j	4	7	5	5
$\sum x_j$	52	69	71	61
$\sum x_j^2$	753	798	1248	912

- a) Set up the null hypothesis and the alternative hypothesis. (5%)
 b) What is the variance explained by the different treatments? (5%)
 c) What is the variance unexplained by the different treatments? (5%)
 d) Complete the ANOVA table. (8%)
 e) What is your conclusion for the test? (2%)
2. Bill has collected a set of data on quarterly sales revenues (Y_t , in \$ million) of his Microhard Co. during 2010-2017. Independent variables (explanatory variables) are defined as: X_{t1} = a linear trend variable, starting the first quarter of 2010 = 1; $X_{t2} = 1$ if period t is the first quarter, 0 otherwise; $X_{t3} = 1$ if period t is the second quarter, 0 otherwise; and $X_{t4} = 1$ if period t is the third quarter, 0 otherwise. OLS estimation results of fitting the quarterly sales revenue data are shown as follows:

	Constant	X_{t1}	X_{t2}	X_{t3}	X_{t4}
Parameters	172.34	10.536	57.06	131.29	43.85
	(4.322)	(2.464)	(4.767)	(3.786)	(4.818)

Note: $R^2 = 0.862$; $SSE = 1291.7$; DW statistic = 1.78.

Figures in parentheses are standard deviations.

- a) Explain the meaning of Durbin-Watson tests (DW statistic) in detail. Perform the test. (10%)
 b) Estimate the difference between expected revenues in any third quarter and expected revenues in the following fourth quarter that is attributable to (1) differential seasonal effects; (2) linear trend. (4%)
 c) Is the estimate of trend variable significant at the 1% significance level? (6%)
 d) Forecast the revenues in the second quarter of 2018. (5%)
3. An urn contains eight red and seven blue balls. A second urn contains an unknown number of red balls and nine blue balls. A ball is drawn from each urn at random, and the probability of getting two balls of the same color is 151/300. How many red balls are in the second urn? (10%)
4. Let X have a uniform distribution on the interval $(0, 1)$. Given that $X = x$, let Y have a uniform distribution on the interval $(0, x + 1)$.
- a) Find the joint pdf of X and Y . Sketch the region where $f(x, y) > 0$. (5%)
 b) Find $E(Y | x)$, the conditional mean of Y , given that $X = x$. Draw this line on the region sketched in part (a). (5%)
 c) Find $f_Y(y)$, the marginal pdf of Y . Be sure to include the domain. (5%)
5. Say the serum cholesterol level (X) (血清膽固醇) of Taiwanese males ages 25–34 follows a translated gamma distribution with pdf

$$f(x) = \frac{x-80}{50^2} e^{-(x-80)/50}, \quad 80 < x < \infty$$

- a) What are the mean and the variance of this distribution? (5%)
 b) What is the mode? (5%)

見背面

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- c) What percentage have a serum cholesterol level less than 200? (5%)
6. Let $Y_1 < Y_2 < \dots < Y_8$ be the order statistics of eight independent observations from a continuous-type distribution with 70th percentile $\pi_{0.7} = 27.3$.
- a) Determine $P(Y_7 < 27.3)$. (5%)
- b) Find $P(Y_5 < 27.3 < Y_8)$. (5%)

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TABLE 13(a) Critical Values for the Durbin-Watson d Statistic, $\alpha = .05$

n	$k = 1$			$k = 2$			$k = 3$			$k = 4$			$k = 5$		
	d_L	d_U	d_L	d_U	d_L	d_U	d_L	d_U	d_L	d_U	d_L	d_U	d_L	d_U	d_L
15	1.08	1.36	.95	1.54	.82	1.75	.69	1.97	.56	2.21					
16	1.10	1.37	.98	1.54	.86	1.73	.74	1.93	.62	2.15					
17	1.13	1.38	1.02	1.54	.90	1.71	.78	1.90	.67	2.10					
18	1.16	1.39	1.05	1.53	.93	1.69	.82	1.87	.71	2.06					
19	1.18	1.40	1.08	1.53	.97	1.68	.86	1.85	.75	2.02					
20	1.20	1.41	1.10	1.54	1.00	1.68	.90	1.83	.79	1.99					
21	1.22	1.42	1.13	1.54	1.03	1.67	.93	1.81	.83	1.96					
22	1.24	1.43	1.15	1.54	1.05	1.66	.96	1.80	.86	1.94					
23	1.26	1.44	1.17	1.54	1.08	1.66	.99	1.79	.90	1.92					
24	1.27	1.45	1.19	1.55	1.10	1.66	1.01	1.78	.93	1.90					
25	1.29	1.45	1.21	1.55	1.12	1.66	1.04	1.77	.95	1.89					
26	1.30	1.46	1.22	1.55	1.14	1.65	1.06	1.76	.98	1.88					
27	1.32	1.47	1.24	1.56	1.16	1.65	1.08	1.76	1.01	1.86					
28	1.33	1.48	1.26	1.56	1.18	1.65	1.10	1.75	1.03	1.85					
29	1.34	1.48	1.27	1.56	1.20	1.65	1.12	1.74	1.05	1.84					
30	1.35	1.49	1.28	1.57	1.21	1.65	1.14	1.74	1.07	1.83					
31	1.36	1.50	1.30	1.57	1.23	1.65	1.16	1.74	1.09	1.83					
32	1.37	1.50	1.31	1.57	1.24	1.65	1.18	1.73	1.11	1.82					
33	1.38	1.51	1.32	1.58	1.26	1.65	1.19	1.73	1.13	1.81					
34	1.39	1.51	1.33	1.58	1.27	1.65	1.21	1.73	1.15	1.81					
35	1.40	1.52	1.34	1.58	1.28	1.65	1.22	1.73	1.16	1.80					
36	1.41	1.52	1.35	1.59	1.29	1.65	1.24	1.73	1.18	1.80					
37	1.42	1.53	1.36	1.59	1.31	1.66	1.25	1.72	1.19	1.80					
38	1.43	1.54	1.37	1.59	1.32	1.66	1.26	1.72	1.21	1.79					
39	1.43	1.54	1.38	1.60	1.33	1.66	1.27	1.72	1.22	1.79					
40	1.44	1.54	1.39	1.60	1.34	1.66	1.29	1.72	1.23	1.79					
45	1.48	1.57	1.43	1.62	1.38	1.67	1.34	1.72	1.29	1.78					
50	1.50	1.59	1.46	1.63	1.42	1.67	1.38	1.72	1.34	1.77					
55	1.53	1.60	1.49	1.64	1.45	1.68	1.41	1.72	1.38	1.77					
60	1.55	1.62	1.51	1.65	1.48	1.69	1.44	1.74	1.49	1.77					
65	1.57	1.63	1.54	1.66	1.50	1.70	1.47	1.73	1.44	1.77					
70	1.58	1.64	1.55	1.67	1.52	1.70	1.49	1.74	1.46	1.77					
75	1.60	1.65	1.57	1.68	1.54	1.71	1.51	1.74	1.49	1.77					
80	1.61	1.66	1.59	1.69	1.56	1.72	1.53	1.74	1.51	1.77					
85	1.62	1.67	1.60	1.70	1.57	1.72	1.55	1.75	1.52	1.77					
90	1.63	1.68	1.61	1.70	1.59	1.73	1.57	1.75	1.54	1.78					
95	1.64	1.69	1.62	1.71	1.60	1.73	1.58	1.75	1.56	1.78					
100	1.65	1.69	1.63	1.72	1.61	1.74	1.59	1.76	1.57	1.78					

TABLE 6(b) Percentage Points of the F Distribution, $\alpha = .05$

v_1	NUMERATOR DEGREES OF FREEDOM													
	1	2	3	4	5	6	7	8	9	10	11	12	13	14
1	161.4	199.5	215.7	224.6	230.2	234.0	236.8	238.9	240.5					
2	18.51	19.00	19.16	19.30	19.33	19.35	19.37	19.38						
3	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81					
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00					
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77					
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10					
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68					
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39					
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18					
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02					
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90					
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80					
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71					
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65					
15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59					
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54					
17	4.45	3.59	3.20	2.96	2.81	2.71	2.60	2.51	2.45					
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46					
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42					
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39					
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37					
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.34	2.34					
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32					
24	4.26	3.40	3.01	2.78	2.62</td									