國立臺北大學 109 學年度碩士班一般入學考試試題

系(所)組別:財政學系

科 目:微積分

第1頁 共1頁 □可 ☑不可 使用計算機

- 1. (10%) Find the limits: (a) $\lim_{x\to 1} \frac{x^{50}-1}{x-1}$. (b) $\lim_{x\to \infty} \frac{x+\sin x+2\sqrt{x}}{x+\sin x}$.
- 2. (10%) Find h'(0) if $h(x) = \left[\frac{g(x) x}{3 + g(x)}\right]^2$, where g(0) = 3 and g'(0) = -2.
- 3. (10%) Find dy/dx for the equation $xy^3 + (2y)^2 5y = \frac{(x^2 9)}{\sqrt{x^2 + 2}}$.
- 4. (20%) Analyze and sketch the graph of $f(x) = \frac{2(x^2 9)}{x^2 4}$. (Label the intercepts, the coordinates of any local and absolute extreme points, inflection points, and asymptotes if any.)
- 5. (10%) $\int_{1}^{2} (\ln(x+1))^{2} dx$.
- 6. (10%) Set up the integral $\int_R \int \frac{y}{1+x^2} dA$ for both orders of integration and use the more convenient order to evaluate the integral over the region R bounded by $y=0, y=\sqrt{x}, x=4$.
- 7. (10%) Determine the convergence or divergence:

(a)
$$\sum_{n=1}^{\infty} \frac{4^n}{3^n + 1}$$
, (b) $\frac{1}{1} - \frac{2}{1} + \frac{4}{2} - \frac{8}{6} + \frac{16}{24} - \cdots$

- 8. (10%) Find the Taylor series generated by $f(x) = 2^x$ at a = 1.
- 9. (10%) Assume that $w = f(s^3 + t^2)$ and $f'(x) = e^x$. Find $\frac{\partial w}{\partial t}$ and $\frac{\partial w}{\partial s}$.