## 元智大學 107 學年度 碩士班 招生試題卷

系(所)別: 管理學院財務金 組別:財務金融碩士學程 融暨會計碩士班

科目:微積分

用紙第| 頁共| 頁

●可使用現行『國家考試電子計算器規格標準』規定第一類之計算機

©Write down your answers in order. You should include all the necessary calculation.

1. (28%) Find the derivative dy/dx. (1% for each)

(a) 
$$y = f(x) = \frac{e^x + x}{\ln x}$$

(b) 
$$y = f(x) = x^x$$

(c) 
$$y = f(x) = \ln(e^{-2x} + \ln 2x)$$

(d) 
$$y = f(x) = \left[ \frac{(2x^2 + 1)^3 \sqrt{(3x - 1)^5}}{\sqrt[3]{2x^3 + 10}} \right]$$

2. (32%) Evaluate the indicated integral. (8% for each)

(a) 
$$\int \frac{1}{\sqrt{x} \left(\sqrt{x} + 1\right)} dx$$

(b) 
$$\int x^3 e^{x^2} dx$$

(c) 
$$\int_{0}^{1} \int_{\sqrt{y}}^{1} e^{x^{3}} dx dy$$

(d) 
$$\int_{-\infty}^{\infty} \frac{5x^5 + 3x^3 + x}{6x^6 + 4x^4 + 2x^2 + 1} dx$$

- 3. (10%) Show that if q(p) units of a quantity are demanded when the price is p, the price elasticity of demand is given by the ratio of derivatives  $E(p) = -(\ln q)'/(\ln p)'$ .
- 4. (15%) Find the general solution of the separable differential equation,  $\frac{dQ}{dt} = kQ(C-Q)$ , where k and C are positive constants.
- 5. (15%) Find the third Taylor polynomial of  $f(x) = \ln(x+1)$  at x=0, and use it to estimate the value of  $\int_0^{1/2} \ln(x+1) dx$ . Compare your result with its exact value. (*Note*:  $\ln 3 = 1.0986$ ,  $\ln 2 = 0.6931$ )