

1. Find the derivative of (a) $\sin^3(4x)$ (5%)
(b) $\frac{1}{(2x^5 - 7)^3}$ (5%)
2. Find the integral of (a) $\int(4xe^{-x} + 3x^{-2} + \sqrt{x})dx$ (5%)
(b) $\int(\ln x + 3 \cos x)dx$ (5%)
3. Find the length of the curve $y = (4 - x^{2/3})^{3/2}$ from $x = 1$ to $x = 8$. (10%)
4. Find (a) the average value of $f(x) = \cos^2 x$ on $[0, 2\pi]$. (5%)
(b) the slope of the tangent line to the graph of $x^2 + 4y^2 = 4$
at the point $(\sqrt{2}, \frac{-1}{\sqrt{2}})$. (5%)
5. Let R be the region bounded by the curves $y^2 = 4x$ and $4x - 3y = 4$.
(a) Sketch the area R. (7%)
(b) Find the area R. (8%)
6. Expand $f(x) = e^{-x}$ in a Taylor series about $x = 0$. (10%)
7. Find (a) $\lim_{x \rightarrow 0} \frac{\sin x - x}{x^3}$ (5%)
(b) $\lim_{x \rightarrow \infty} \frac{e^{-x}}{x^{-1}}$ (5%)
8. Does $\sum \frac{n}{5n^2 - 4}$ converge? If not, show the detail. (5%)
9. Find (a) the integral of $\int x^2 \sin ax dx$ (10%)
(b) the integral of $\int \frac{x^2 - x}{x + 1} dx$ (10%)