國立中山大學 101 學年度碩士暨碩士專班招生考試試題

科目:微積分丙【企管系甲班碩士班丙組選考】

共1頁第1頁

題號:4113

請依題號順序作答,違者扣分。

1. Find the derivatives for the following functions. 20%

i.
$$f(x) = \frac{1}{1 + e^{-x}}$$
 ii. $y = e^{-\pi} + \pi^{-e}$ iii. $f(x) = \frac{x}{\sin^2 x}$

iv. Find dy/dx where $\sin(3y) + \cos(5x) = xy$

- 2. Sketch the function $f(x) = e^{-x} \sin x$, $(0 \le x \le 2\pi)$. 20% Indicate
 - the critical points, i.
 - the reflection point(s), ii.
 - the global maxima and minima, iii.
 - the increasing and decreasing and concavity of the function iv.
- 3. Evaluate the following. 30 %

i.
$$\int xe^{-x^2} dx$$
 ii.
$$\int_{2}^{3} \ln x dx$$
 iii.
$$\int_{1}^{\infty} \frac{dx}{5x+2}$$
 v.
$$\int_{0}^{6} \int_{x/3}^{2} x \sqrt{y^3 + 1} dy dx$$
. v.
$$\lim_{x \to \infty} xe^{-x}$$

iv.
$$\int_{0}^{6} \int_{x/3}^{2} x \sqrt{y^3 + 1} dy dx.$$
 v. $\lim_{x \to \infty} x e^{-x}$

Determine if the sequences converge a. $\sum_{n=1}^{\infty} \frac{n-5}{n^3+8}$ b. $\sum_{n=1}^{\infty} \sin(\frac{1}{n})$ vi.

4. By looking at their Taylor series, decide which of the following functions is the largest and which is the smallest, for x near 0. 15%

i.
$$e^x$$
 ii. $1 + \sin x$ iii. $\frac{1}{\sqrt{1 - 2x}}$

- 5. While taking a walk along the road where you live, you accidentally drop your i-pad, but you don't know where. The probability density p(x) for having dropped the i-phone x kilometers from home (along the road) is $p(x) = e^{-x}$ for $x \ge 0$. 15%
 - What is the probability that you dropped it within 1 kilometer of home?
 - ii. At what distance y from home is the probability that you dropped it within y kmof home equal to 0.95