

Multiple Choice Questions (24%, 4% per question)

Please select one and only one most appropriate answer.

1. If 35% of the students in my statistics class use the Google mail (or gmail), I conclude from this that 35% of all students at the University have gmail accounts. The most important logical weakness of this conclusion would be:
A) relying on any sample instead of surveying every student.
B) using a sample that may not be representative of all students.
C) failing to correct for unconscious interviewer bias.
D) assuming cause and effect where none exists.
2. The Dean of Students mailed a survey to a total of 400 students. The sample included 100 students randomly selected from each of the freshman, sophomore, junior, and senior classes on campus last term. What sampling method was used?
A) simple random sample B) systematic sample
C) stratified sample D) cluster sample
3. A drug company wanted to test a new indigestion medication. The researchers found 400 adults aged 25-35 and randomly assigned them to two groups. The first group received the new drug, while the second received a placebo. After one month of treatment, the percentage of each group whose indigestion symptoms decreased was recorded and compared. How many levels does the treatment in this experiment have?
A) 2 (medication or placebo) B) 400 (number of respondents)
C) 1 (months of treatment) D) 10 (age span of respondents)
4. A regression intercept represents:
A) the slope of the line. B) the amount of change in Y given a one unit change in X.
C) the value of Y when X is equal to zero. D) the strength of the X-Y relationship.
5. Which is not a likely area of application of statistics in business?
A. Auditing supplier invoices for correct payment.
B. Questioning the executives' strategic decisions.
C. Looking for patterns in a large marketing database.
D. Making forecasts of several key product lines.
6. How many degrees of freedom are there in a 5x7 contingency table when the chi-square test of association is used?
A) 12 B) 24 C) 30 D) 35 E) None of the above.

Computational Questions (76%)

Please clearly show your calculations in detail.

C1. To test if a certain training course can improve performance of production line workers, the researcher randomly selected 6 workers and wrote down their performance indicators before and after the training course, as below: (The performance indicators are normally distributed)

Employee	1	2	3	4	5	6
Perf. indicator before training (X)	110	125	100	90	110	130
Perf. indicator after training (Y)	113	121	103	92	112	125

Given the sum of $x^2 = 74825$, the sum of $y^2 = 74652$, the sum of $xy = 74705$, $\alpha = 0.05$

- (A) Please conduct hypothesis testing on the effectiveness of the training course using t statistics. (12%)
(B) Please calculate and present the linear regression equation for predicting Y from X. (12%)
(C) Please use ANOVA to test if the regression equation slope equals zero. (12%)

C2. 已知在總人口中帶有某遺傳基因 K 的比率為 5%，而目前測試遺傳基因 K 的檢驗對於帶有基因 K 者有 5% 的機率呈現陰性，對於未帶基因 K 者有 2% 機率呈現陽性。今隨機檢驗一人是否帶有基因 K，請問：

- (A) 此人呈現陽性反應的機率為何？(10%)
(B) 若已知此人檢驗結果呈現陽性反應，但此人並未帶有基因 K 的機率為何？(10%)

C3. 某企業抽出 50 名員工並調查其年齡，發現平均年齡為 36 歲，標準差為 12 歲。請問：

- (A) 員工平均年齡之 95% 信賴區間為何？(10%)
(B) 若希望員工平均年齡的 95% 信賴區間能調整到 (33, 39)，請問應抽取多少樣本？(10%)

F critical values		Degrees of freedom in the numerator						
	p	1	2	3	4	5	6	7
Degrees of freedom in the denominator	1	39.86	49.50	53.59	55.83	57.24	58.20	58.91
	.100	161.45	199.50	215.71	224.58	230.16	233.99	236.77
	.050	647.79	799.50	864.16	899.58	921.85	937.11	948.22
	.025	4052.2	4999.5	5403.4	5624.6	5763.6	5859.0	5928.4
	.010	40528.4	50000.0	54037.9	56250.0	57640.5	58593.7	59287.3
	.001	8.53	9.00	9.16	9.24	9.29	9.33	9.35
	.100	18.51	19.00	19.16	19.25	19.30	19.33	19.35
2	.050	38.51	39.00	39.17	39.25	39.30	39.33	39.36
3	.025	98.50	99.00	99.17	99.25	99.30	99.33	99.36
	.010	998.50	999.00	999.17	999.25	999.30	999.33	999.36
	.001	5.54	5.46	5.39	5.34	5.31	5.28	5.27
	.100	10.13	9.55	9.28	9.12	9.01	8.94	8.89
	.050	17.44	16.04	15.44	15.10	14.88	14.73	14.62
	.025	34.12	30.82	29.46	28.71	28.24	27.91	27.67
	.010	167.03	148.50	141.11	137.10	134.58	132.85	131.58
4	.001	4.54	4.32	4.19	4.11	4.05	4.01	3.98
5	.100	7.71	6.94	6.59	6.39	6.26	6.16	6.09
	.050	12.22	10.65	9.98	9.60	9.36	9.20	9.07
	.025	21.20	18.00	16.69	15.98	15.52	15.21	14.98
	.010	74.14	61.25	56.18	53.44	51.71	50.53	49.66
	.001	4.06	3.78	3.62	3.52	3.45	3.40	3.37
	.100	6.61	5.79	5.41	5.19	5.05	4.95	4.88
	.050	10.01	8.43	7.76	7.39	7.15	6.98	6.85
6	.025	16.26	13.27	12.06	11.39	10.97	10.67	10.46
	.010	47.18	37.12	33.20	31.09	29.75	28.83	28.16
	.001	3.78	3.46	3.29	3.18	3.11	3.05	3.01
	.100	5.99	5.14	4.76	4.53	4.39	4.28	4.21
	.050	8.81	7.26	6.60	6.23	5.99	5.82	5.70
	.025	13.75	10.92	9.78	9.15	8.75	8.47	8.26
	.010	35.51	27.00	23.70	21.92	20.80	20.03	19.46
7	.001	3.59	3.26	3.07	2.96	2.88	2.83	2.78
8	.100	5.59	4.74	4.35	4.12	3.97	3.87	3.79
	.050	8.07	6.54	5.89	5.52	5.29	5.12	4.99
	.025	12.25	9.55	8.45	7.85	7.46	7.19	6.99
	.010	29.25	21.69	18.77	17.20	16.21	15.52	15.02
	.001	3.26	2.96	2.78	2.68	2.60	2.54	2.49
	.100	5.14	4.39	4.01	3.78	3.63	3.53	3.45
	.050	7.26	5.99	5.34	5.05	4.88	4.73	4.62

t distribution critical values											
		Upper-tail probability <i>p</i>									
df		.25	.20	.15	.10	.05	.025	.02	.01	.005	
1		1.000	1.376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	
2		0.816	1.061	1.386	1.886	2.920	4.303	4.849	6.965	9.925	
3		0.765	0.978	1.250	1.638	2.353	3.182	3.482	4.541	5.841	
4		0.741	0.941	1.190	1.533	2.132	2.776	2.999	3.747	4.604	
5		0.727	0.920	1.156	1.476	2.015	2.571	2.757	3.365	4.032	
6		0.718	0.906	1.134	1.440	1.943	2.447	2.612	3.143	3.707	
7		0.711	0.896	1.119	1.415	1.895	2.365	2.517	2.998	3.499	
8		0.706	0.889	1.108	1.397	1.860	2.306	2.449	2.896	3.355	
9		0.703	0.883	1.100	1.383	1.833	2.262	2.398	2.821	3.250	
10		0.700	0.879	1.093	1.372	1.812	2.228	2.359	2.764	3.169	
11		0.697	0.876	1.088	1.363	1.796	2.201	2.328	2.718	3.106	
12		0.695	0.873	1.083	1.356	1.782	2.179	2.303	2.681	3.055	
13		0.694	0.870	1.079	1.350	1.771	2.160	2.282	2.650	3.012	
14		0.692	0.868	1.076	1.345	1.761	2.145	2.264	2.624	2.977	
15		0.691	0.866	1.074	1.341	1.753	2.131	2.249	2.602	2.947	
16		0.690	0.865	1.071	1.337	1.746	2.120	2.235	2.583	2.921	
17		0.689	0.863	1.069	1.333	1.740	2.110	2.224	2.567	2.898	
18		0.688	0.862	1.067	1.330	1.734	2.101	2.214	2.552	2.878	
19		0.688	0.861	1.066	1.328	1.729	2.093	2.205	2.539	2.861	
20		0.687	0.860	1.064	1.325	1.725	2.086	2.197	2.528	2.845	
21		0.686	0.859	1.063	1.323	1.721	2.080	2.189	2.518	2.831	
22		0.686	0.858	1.061	1.321	1.717	2.074	2.183	2.508	2.819	
23		0.685	0.858	1.060	1.319	1.714	2.069	2.177	2.500	2.807	
24		0.685	0.857	1.059	1.318	1.711	2.064	2.172	2.492	2.797	
25		0.684	0.856	1.058	1.316	1.708	2.060	2.167	2.485	2.787	
26		0.684	0.856	1.058	1.315	1.706	2.056	2.162	2.479	2.779	
27		0.684	0.855	1.057	1.314	1.703	2.052	2.158	2.473	2.771	
28		0.683	0.855	1.056	1.313	1.701	2.048	2.154	2.467	2.763	
29		0.683	0.854	1.055	1.311	1.699	2.045	2.150	2.462	2.756	
30		0.683	0.854	1.055	1.310	1.697	2.042	2.147	2.457	2.750	
40		0.681	0.851	1.050	1.303	1.684	2.021	2.123	2.423	2.704	
50		0.679	0.849	1.047	1.299	1.676	2.009	2.109	2.403	2.678	
60		0.679	0.848	1.045	1.296	1.671	2.000	2.099	2.390	2.660	
80		0.678	0.846	1.043	1.292	1.664	1.990	2.088	2.374	2.639	
100		0.677	0.845	1.042	1.290	1.660	1.984	2.081	2.364	2.626	
1000		0.675	0.842	1.037	1.282	1.646	1.962	2.056	2.330	2.581	
z*		0.674	0.841	1.036	1.282	1.645	1.960	2.054	2.326	2.576	
		50%	60%	70%	80%	90%	95%	96%	98%	99%	
Confidence level <i>C</i>											