## 國立中央大學102學年度碩士班考試入學試題卷

科目:普通物理 共 2 頁 第 / 頁 所別:大氣科學學系大氣物理碩士班 不分組(一般生) 大氣科學學系大氣物理碩士班 不分組(在職生)

本科考試禁用計算器

\*請在試卷答案卷(卡)內作答

- 1. A particle of mass m is dropped onto the top of a vertical spring with the force constant k. If the particle is released from a height habove the top of spring.
  - (a) What is the maximum kinetic energy of the particle? (5%)
  - (b) What is the maximum compression of the spring? (5%)
  - (c) At what compression is the particle kinetic energy half its maximum value?
- 2. A particle of mass m sliding on a frictionless table is attached to a string that passes through a hole in the table. Initially, the particle is sliding with speed  $v_i$  in a circle of radius  $r_i$ .
  - (a) Find the tension in the string in terms of the angular momentum of the particle.
  - (b) If the string is pulled downward very slowly. How much work is required to reduce the radius of the circle  $r_f = r_i / 2$ ?
- 3. A large spherical helium weather balloon with the radius 3m and the total mass 18kg (balloon, helium and equipment). The air mass density is  $1.3kg/m^3$  at sea level where the atmospheric pressure is 1atm.
  - (a) What is the initial upward acceleration of the balloon when it is released from sea level? (5%)
  - (b) If the drag force on the balloon is given by  $f_d = \frac{\pi r^2}{2} \rho v^2$ , where r is the balloon radius,  $\rho$  is the density of air, and v is the ascension speed of the balloon, determine the terminal velocity of the ascending balloon. (5%)
  - (c) Estimate the time will it take for the balloon to ascend to a height of 20km.
- 4. Two sources separated by some distance emit harmonic waves of the same frequency with wavelength  $\lambda$ . At some point P, the intensity of the wave due to each source separately is  $I_0$ . The path distance from P to one of the sources is  $\lambda/2$  greater than that from to the other source. What is the intensity at P for each case,
  - (a) the sources are coherent and in phase. (5%)
  - (b) the sources are incoherent.
  - (c) the sources are coherent but have a phase difference of  $\pi$  rad. (5%)
- 5. One mole of an ideal gas with the ratio of the heat capacities  $\gamma = 1.4$  and the heat capacities of constant volume  $C_V = \frac{5}{2}R$  initially at a pressure of 1 atm and a temperature of  $T_1 = 0^{\circ}C$ , where the gas constant  $R = 8.314 J/mol \cdot K$ . The gas is heated at constant volume to  $T_2 = 100^{\circ} C$  and is then expanded adiabatically until its pressure is again 1 atm. It is then compressed at constant pressure back to its original state.
  - (a) Find the temperature  $T_3$  after the adiabatic expansion.
  - (b) Calculate the heat entering or leaving the system during each process. (5%)
  - (c) Estimate the efficiency of this cycle.





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- 6. A ring of radius R that lies in the x-y plane carries a positive charge Q uniformly distributed over its length. A particle of mass m that carries a negative charge magnitude q is at the center of the ring.
  - (a) Find the electric field along the axis of the ring (z-axis). (5%)
  - (b) Let the charge particle of mass m moving in z-axis with coordinates  $z \ll R$ , Find the force on it as a linear function of z. (5%)
  - (c) Estimate the period T of the harmonic moving particle near the center of the ring along z-axis. (5%).
- 7. A ray of light passes from one medium to another medium, striking the surface of the boundary. Which of the following quantities change as the light enters the second medium:
  - (1) wavelength, (2) frequency, (3) speed of propagation, (4) direction of the propagation,
  - (5) the polarizing angle for which the reflected light is completely polarized. (5%)
- 8. A ray of light is incident in air of the refraction index n=1 and the polarizing angle for a certain substance is  $30^{\circ}$ .
  - (a) What is the angle of refraction of light incident at this angle? (5%)
  - (b) What is the index of refraction of this substance? (5%)

注:背面有試題

参考用