219, 206 絕號:

國立成功大學九十七學年度碩士班招生考試試題

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系所:電腦與通信工程研究所甲組。電機工程學系工組 科目:離散數學

本試題是否可以使用計算機: 凹可使用 , □不可使用 (請命題老師勾選)

考試日期:0301 - 節次:3

- 1. For p a prime determine all elements $a \in Z_p$ where $a^2 = a$. (10%)
- 2. Find the number of n-digit words generated from the alphabet {0, 1, 2, 3, 4} in each of which the total number of 0's and 1's is even. (15%)
- 3. Apply the state minimization process to the following machine.

	Next state		Output	
	0	1	0	1
S_1	S_6	S_3	0	0
S ₂	S_3	· · · ·S ₁ ·····	0	0
S_3	S_2	S ₄	0	0
S ₄	S ₇	S ₄	0	0
S ₅	S_6	S ₇	0	0
S_6	S_5	S ₂	. 1	0
S ₇	S ₄	S_1	0	0

- 4. On the first day of a new year, Joseph deposits \$1000 in an account that pays 6% interest compounded monthly. At the beginning of each month he added \$200 to his account. If he continues to do this for next four years (so that he makes 47 additional deposits of \$200), how much will his account be worth exactly four years after he opened it? (15%)
- 5. In how many different ways can we use two different colors to paint the faces of a cube. (15%)
- 6. Let $f, g: \mathbb{Z}^+ \to \mathbb{R}$ where $f(n) = n^2 + n$ and $g(n) = (1/2)n^3$. Please prove that $f \in O(g)$ but $g \notin O(f)$. (15%)
- 7. Please find a 3 clock cycles scheduled data flow graph (the one like a state diagram) for the following computations and derive the minimum number of registers used in the graph using 2 adders and 1 multiplier. Assume both of the adder and the multiplier have one clock cycle delay. (Hint: using the graph coloring approach) (15%)

$$r = g + h + i$$

$$s = g + c + h * c$$