219, 206 繼號:

國立成功大學九十七學年度碩士班招生考試試題

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系所:電腦與通信工程研究所甲組。電構、工程等系丁組

科目:離散數學

本試歷是否可以使用計算機: 凹可使用 , 口不可使用

(請命題老師勾選)

考試日期:0301 - 節次:3

- 1. For p a prime determine all elements  $a \in \mathbb{Z}_p$  where  $a^2 = a$ . (10%)
- 2. Find the number of n-digit words generated from the alphabet {0, 1, 2, 3, 4} in each of which the total number of 0's and 1's is even. (15%)
- 3. Apply the state minimization process to the following machine.

	Next state		Output	
<u> </u>	0	1	0	1
$S_1$	$S_6$	$S_3$	0	0
$S_2$	$S_3$	S <sub>1</sub>	0	0
$S_3$	$S_2$	S <sub>4</sub>	0	0
S <sub>4</sub>	S <sub>7</sub>	S <sub>4</sub>	0	0
$S_5$	$S_6$	S <sub>7</sub>	0	0
	$S_5$	$S_2$	. 1	0
$\frac{S_6}{S_7}$	S <sub>4</sub>	$S_1$	0	0

- 4. On the first day of a new year, Joseph deposits \$1000 in an account that pays 6% interest compounded monthly. At the beginning of each month he added \$200 to his account. If he continues to do this for next four years (so that he makes 47 additional deposits of \$200), how much will his account be worth exactly four years after he opened it? (15%)
- 5. In how many different ways can we use two different colors to paint the faces of a cube. (15%)
- 6. Let  $f, g: \mathbb{Z}^+ \to \mathbb{R}$  where  $f(n) = n^2 + n$  and  $g(n) = (1/2)n^3$ . Please prove that  $f \in O(g)$  but  $g \notin O(f)$ . (15%)
- 7. Please find a 3 clock cycles scheduled data flow graph (the one like a state diagram) for the following computations and derive the minimum number of registers used in the graph using 2 adders and 1 multiplier. Assume both of the adder and the multiplier have one clock cycle delay. (Hint: using the graph coloring approach) (15%)

$$r=g+h+i$$

$$s = g + c + h * c$$