

1. (10%) Find the transfer function $\frac{V_{out}(s)}{V_{in}(s)}$ as shown in Fig. 1.

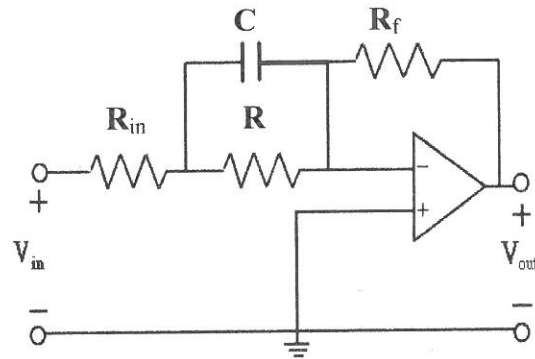


Fig. 1.

2. (20%) The block diagram of a control system is shown in Fig 2. The error signal is defined to be $e(t)$.

- (a) Find the steady-state errors in terms of K and K_I when the following inputs are applied (i) $r(t) = u_s(t)$ (ii) $r(t) = tu_s(t)$
 (b) Find the value of K and K_I so that the maximum overshoot is 10 percent and the settling time approximated as $t_s \approx \frac{3.2}{\zeta\omega_n}$ is 0.05sec.

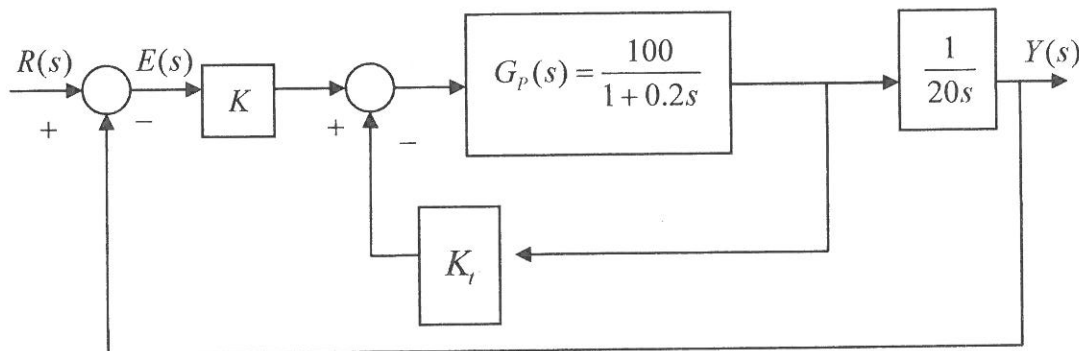


Fig. 2.

3. (20%) Given the system $\frac{dx(t)}{dt} = Ax(t) + Bu(t)$, $y(t) = Cx(t)$

where $A = \begin{bmatrix} 0 & 1 \\ -1 & -3 \end{bmatrix}$, $B = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$, $C = [1 \ 1]$

- (a) Determine the controllability and observability of the closed-loop system.
 (b) Let $u(t) = -Kx(t)$, where $K = [k_1 \ k_2]$. Determine if and how controllability and observability of the closed-loop system are affected by the elements of K .

4. (10%) The transfer function of a unity feedback control system is

$$G(s) = \frac{K}{s(s+6.54)}$$

Find the resonance peak M_r , resonance frequency ω_r , and bandwidth BW of the closed-loop system with $K=21.39$.

5. (30%) The forward-path transfer function of a unity-feedback control system is given

in the following. $G(s) = \frac{K}{(s+3)^3}$

- Construct the root loci of the characteristic equation of the closed-loop system for $K > 0$.
- Apply the Nyquist criterion to determine the range of K for stability and check the answer with the Routh-Hurwitz criterion.
- Find the value of K so that the phase margin of the system is 45° .

6. (10 %) Please prove that the following electric network is a phase-lag compensator

$$\frac{E_o(s)}{E_i(s)} = K \frac{s+a}{s+b}, \quad a > b > 0.$$

