

系所組別：工程科學系在職專班乙組

考試科目：熱傳學（專班）

考試日期：0223，節次：3

※ 考生請注意：本試題不可使用計算機

I. One side of a plane wall is maintained at 100°C , while the other side is exposed to a convection environment having $T = 10^{\circ}\text{C}$ and $h = 12 \text{ W}/(\text{m}^2\cdot^{\circ}\text{C})$. The wall has $k = 1.2 \text{ W}/(\text{m}\cdot^{\circ}\text{C})$ and is 40 cm thick. Calculate the heat flux through the wall. (10%)

II. Derive an expression for the temperature distribution in plane wall having uniformly distributed heat source \dot{q} and one face maintained at a temperature T_1 while the other face is maintained at a temperature T_2 . The thickness of the wall may be taken as $2L$. (15%)
Hint: the energy equation for the problem can be written as $\frac{d^2T}{dx^2} + \frac{\dot{q}}{k} = 0$.

III. The one-dimensional Fourier law can be written as

$$q'' = -k \frac{\partial T}{\partial z}$$

- (1) What are q'' , k and $\partial T / \partial z$? (6%)
- (2) What is the meaning of the negative sign in the equation? (4%)
- (3) If the Fourier is re-written as

$$q'' = k \frac{\partial T}{\partial z},$$

is it correct? Why or Why not? (5%)

IV. Explain the following terms: (20%)

- (1) Heat conduction equation or Heat diffusion equation
- (2) Heat transfer rate
- (3) Specific heat
- (4) Thermal diffusivity
- (5) Nusselt number

V. Answer the following questions: (25%)

(1) What are the differences between heat transfer and thermodynamics?

(2) 以熱傳觀點，來闡釋發熱衣的禦寒效果？

(3) 核電廠發生事情，為何大都是與熱傳問題有關？

(4) 以熱傳觀點，來闡釋羽毛衣的禦寒效果？

(5) 高功率元件，常以鰭片(fin)幫助散熱。請以熱傳觀點，闡釋其理由。

VI. The temperature distribution across a wall 1m thick at certain instant of time is given as

$$T(x) = a + bx + cx^2$$

where T is in degrees Celsius and x is in meters, while $a = 900^{\circ}\text{C}$, $b = -300^{\circ}\text{C}/\text{m}$, and $c = -50^{\circ}\text{C}/\text{m}^2$.

A uniform heat generation, $\dot{q} = 2000 \text{ W}/\text{m}^3$, is present in the wall of area 10 m^2 having properties $\rho = 1000 \text{ kg}/\text{m}^3$, $k = 40 \text{ W}/\text{m}\cdot\text{K}$, and $c_p = 4 \text{ kJ}/\text{kg}\cdot\text{K}$.

- (1) Determine the rate of heat transfer entering the wall ($x = 0$) and leaving the wall ($x = 1\text{m}$). (8%)
- (2) Determine the time rate of temperature change at $x = 0.5 \text{ m}$. (7%)

Hint:
$$\frac{\partial T}{\partial t} = \frac{k}{\rho c_p} \frac{\partial^2 T}{\partial x^2} + \frac{\dot{q}}{\rho c_p}$$