

1、For a plant  $G_p(s) = \frac{\omega_n^2}{s(s + 2\xi\omega_n)}$  (20%)

- (a) Design a PID controller  $G_c(s)$  and draw unity feedback form block diagram
- (b) Give an electronic-circuit realization of the PID controller in (a) find the gains of  $G_c(s)$ . (Represented it by R and C in your circuit)

- 2、(a) In Figure 1, using capacitor voltage and inductor current as state variables, current  $Y(t)$  as output, write dynamic equation. (5%)
- (b)  $C=1\mu\text{F}$ ,  $L=100\text{mH}$ ,  $R_1=100\text{k}\Omega$ ,  $R_2=10\Omega$ , whether the system is controllable and observable? (5%)
- (c) In question(b), what's the transfer function of the system? and find the poles of the system? (5%)
- (d) According to Figure 2, continue with question (c), design a state feedback controller  $K$  so that the Maximum overshoot  $M_o=0.1\%$ , rise time  $t_r=0.02$  sec. (5%)

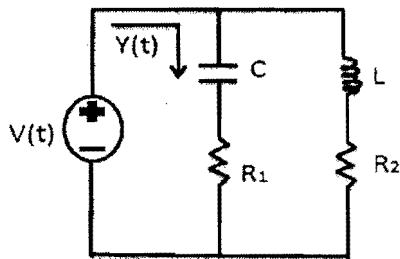


Figure 1

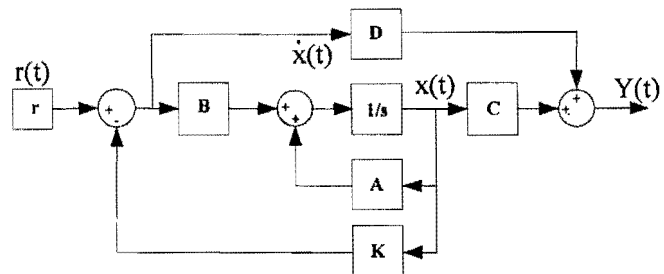


Figure 2

3. Consider a controller as given in Figure 3 (20%)

- (a) Find the transfer function  $V_o(s)/V_i(s)$  of the controller.
- (b) What kind of the controller for  $R_1=100\text{K}$ ,  $R_2=400\text{K}$ ,  $C_1=0.3\mu\text{F}$ , and  $C_2=0.1\mu\text{F}$  ?

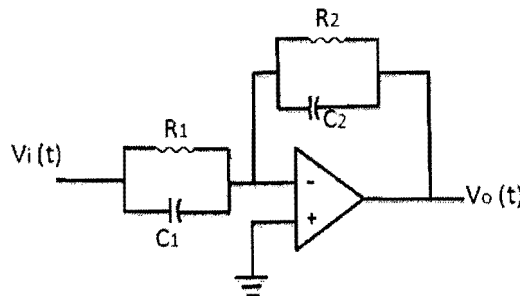


Figure 3

(背面仍有題目,請繼續作答)

4. (a) Write the force equations of the linear translational systems shown in Figure 4. (b) Draw system state diagrams and write the state equations. (c) Find the transfer function  $Y_1(s)/F(s)$  and  $Y_2(s)/F(s)$ . (20%)

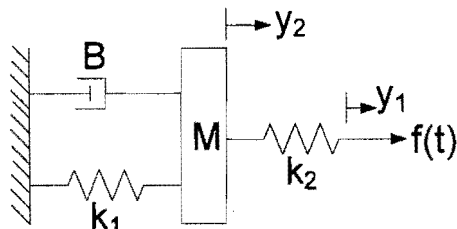


Figure 4

5. (a) For the translational mechanical system with a nonlinear spring shown in Figure 5, find the transfer function,  $G(s)=X(s)/F(s)$ , for small excursions around  $f(t)=1$ . The spring is defined by  $x_s(t)=1-e^{-f_s(t)}$ , where  $x_s(t)$  is the spring displacement and  $f_s(t)$  is the spring force. (5%)
- (b) Given the state description matrices in control canonical form of transfer function  $G(s)$ , and design a state feedback controller  $K$  so that the poles locate at  $-3, -5$ . (10%)
- (c) Check the observability of the state space dynamic equation in (b), and find the observer gain matrix  $L$  so that the observer error poles are at  $-2$  and  $-3$ , respectively. (5%)

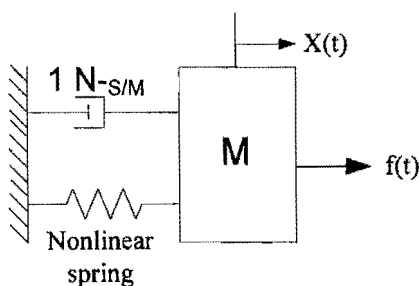


Figure 5