

系所組別：工業設計學系乙組

考試科目：統計概論與方法

考試日期：0223，節次：3

※ 考生請注意：本試題不可使用計算機

Part1: Multiple choice questions (50 pts)

1. An important implication of the formula for the standard error is that whenever the sample size equals two or more, the variability of the sampling distribution is _____ the variability of the population. (5 pts)
 - a) equal to
 - b) less than
 - c) more than
 - d) approximately the same as

2. Reducing the size of the standard error produces a shrinkage in the (5 pts)
 - a) retention region.
 - b) true sampling distribution.
 - c) retention region *or* the true sampling distribution.
 - d) retention region *and* the true sampling distribution.

3. Metal detectors at airports are used to determine whether passengers are carrying weapons. If the null hypothesis states that a passenger isn't carrying a weapon, a type II error would occur when (5 pts)
 - a) a weapon-free passenger passes the detector without activating the alarm.
 - b) a weapon-free passenger passes the detector and activates the alarm.
 - c) a weapon-carrying passenger passes the detector without activating the alarm.
 - d) a weapon-carrying passenger passes the detector and activates the alarm.

4. The mean height for a population is 65 inches and the standard deviation is 3 inches. Let A and B denote the events described below. Is the probability of event A greater than the probability of event B? (5 pts)
 - Event A: The mean height in a random sample of 16 people is within 1 inch of the population mean.
 - Event B: The mean height in a random sample of 50 people is within 1 inch of the population mean.
 - a) True
 - b) False

(背面仍有題目，請繼續作答)

※ 考生請注意：本試題不可使用計算機

5. The data below consists of the test scores of 16 students. Assuming $\sigma=13.36$, determine a 95.44% confidence interval for the population mean. Find the requested confidence interval. (5 pts)

95	74	64	93	95	73	84	65
54	98	93	87	72	75	85	96

- a) 75.19 to 84.63
- b) 53.19 to 106.63
- c) 74.76 to 88.12
- d) 54.72 to 108.16

6. If the null hypothesis is false because of a large effect, the probability of a correct decision (5 pts)

- a) will be relatively large.
- b) will be relatively small.
- c) will equal one minus the level of significance.
- d) will equal one minus the probability that the null hypothesis is false.

7. Ten years ago, at a small high school in Alabama, the mean SAT Math score of all high school students who took the exam was 490 with a standard deviation of 80. This year, the SAT Math scores of a random sample of 25 students who took the exam are obtained. The mean score of these 25 students is $\bar{x} = 525$. To determine if there is evidence that the scores in the district have improved, the hypotheses $H_0: \mu = 490$ versus $H_a: \mu > 490$ are tested at the 5% significance level. The P -value is found to be 0.014. Suppose that the average SAT Math score of all high school students at this high school is in fact equal to 505. Which of the following statements is true? (5 pts)

- a) A Type I error has been committed.
- b) A Type II error has been committed.
- c) No error has been committed.
- d) None of the above.

系所組別：工業設計學系乙組

考試科目：統計概論與方法

考試日期：0223，節次：3

※ 考生請注意：本試題不可使用計算機

Use the following to answer questions 8 and 9:

The time needed for college students to complete a certain paper-and-pencil maze follows a Normal distribution with a mean of 30 seconds and a standard deviation of 3 seconds. You wish to see if the mean time μ is changed by vigorous exercise, so you have a group of nine college students exercise vigorously for 30 minutes and then complete the maze. Assume that σ remains unchanged at 3 seconds. The hypotheses you decide to test are $H_0: \mu = 30$ versus $H_a: \mu \neq 30$.

8. Suppose it takes the nine students an average of $\bar{x} = 32.05$ seconds to complete the maze. At the 1% significance level, what can you conclude? (5 pts)
- H_0 should be rejected because the P-value is less than 0.01.
 - H_0 should not be rejected because the P-value is greater than 0.01.
 - H_a should be rejected because the P-value is less than 0.01.
 - H_a should not be rejected because the P-value is greater than 0.01.
9. Suppose you compute the average time \bar{x} that it takes these students to complete the maze and you find that the results are significant at the 5% level. What can you conclude? (5 pts)
- The test would also be significant at the 10% level.
 - The test would also be significant at the 1% level.
 - Both of the above.
 - None of the above.
10. The number of loaves of rye bread left on the shelf of a local bakery at closing (denoted by the random variable X) varies from day to day. Past records show that the probability distribution of X is as shown in the following table. Find the probability that there will be at least three loaves left over at the end of any given day. (5 pts)

X	0	1	2	3	4	5	6
$P(X=x)$	0.2	0.25	0.2	0.15	0.1	0.08	0.02

- 0.8
- 0.2
- 0.35
- 0.65

(背面仍有題目，請繼續作答)

系所組別：工業設計學系乙組

考試科目：統計概論與方法

考試日期：0223，節次：3

※ 考生請注意：本試題不可使用計算機

Part 2: Short-answer questions (20 pts)

1. Explain in (a) and (b) the effect of the margin of error on the precision of estimating a population mean by a sample mean.
 - (a) Increasing the confidence level while keeping the same sample size (5 pts).
 - (b) Increasing the sample size while keeping the same confidence level (5 pts).
2. Explain the Central Limit Theorem (5 pts).
3. The mean and the standard deviation of the sampled population are respectively, 211.7 and 21.9. Find the mean and standard deviation of the sampling distribution of the sample mean \bar{x} ($n=64$). Round to two decimal places as needed. (5 pts)

※ 考生請注意：本試題不可使用計算機

Part 3: Long-answer questions (30 pts)

- HTC is planning to release 5 inch handset for elders in 2014. To understand whether **Type of Icon influences Smartphone Usability**, the Interaction Design group at HTC conducted an experiment with a total of 15 elderly participants, each evaluating the readability of an icon from 1 to 10, low to high. The rating scores are summarized in the following table:

Style	1	2	3	4	5
Icon					
Readability Score	4	8	3	4	9
	2	5	6	0	6
	5	5	9	2	9

The research problem for the experiment is: Does there appear to be a difference in the mean readability scores among the icons? The group decided to use F to test the null hypothesis at the 0.05 level of significance. Answer the following questions (round to two decimal places as needed):

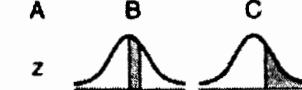
- (1) State the statistical hypotheses. (4 pts)
- (2) Describe your decision rule. (4 pts)
- (3) Compute SS_{total} , SS_{between} , and SS_{within} and construct a one-way ANOVA table (18 pts).
- (4) State your decision and interpretation. (4 pts)

系所組別：工業設計學系乙組

考試科目：統計概論與方法

考試日期：0223，節次：3

※ 考生請注意：本試題不可使用計算機

A B C			A B C			A B C		
								
								
0.00	.0000	.5000	0.56	.2123	.2877	1.12	.3686	.1314
0.01	.0040	.4960	0.57	.2157	.2843	1.13	.3708	.1292
0.02	.0080	.4920	0.58	.2190	.2810	1.14	.3729	.1271
0.03	.0120	.4880	0.59	.2224	.2776	1.15	.3749	.1251
0.04	.0160	.4840	0.60	.2257	.2743	1.16	.3770	.1230
0.05	.0199	.4801	0.61	.2291	.2709	1.17	.3790	.1210
0.06	.0239	.4761	0.62	.2324	.2676	1.18	.3810	.1190
0.07	.0279	.4721	0.63	.2357	.2643	1.19	.3830	.1170
0.08	.0319	.4681	0.64	.2389	.2611	1.20	.3849	.1151
0.09	.0359	.4641	0.65	.2422	.2578	1.21	.3869	.1131
0.10	.0398	.4602	0.66	.2454	.2546	1.22	.3888	.1112
0.11	.0438	.4562	0.67	.2486	.2514	1.23	.3907	.1093
0.12	.0478	.4522	0.68	.2517	.2483	1.24	.3925	.1075
0.13	.0517	.4483	0.69	.2549	.2451	1.25	.3944	.1056
0.14	.0557	.4443	0.70	.2580	.2420	1.26	.3962	.1038
0.15	.0596	.4404	0.71	.2611	.2389	1.27	.3980	.1020
0.16	.0636	.4364	0.72	.2642	.2358	1.28	.3997	.1003
0.17	.0675	.4325	0.73	.2673	.2327	1.29	.4015	.0985
0.18	.0714	.4286	0.74	.2704	.2296	1.30	.4032	.0968
0.19	.0753	.4247	0.75	.2734	.2266	1.31	.4049	.0951
0.20	.0793	.4207	0.76	.2764	.2238	1.32	.4066	.0934
0.21	.0832	.4168	0.77	.2794	.2206	1.33	.4082	.0918
0.22	.0871	.4129	0.78	.2823	.2177	1.34	.4099	.0901
0.23	.0910	.4090	0.79	.2852	.2148	1.35	.4115	.0885
0.24	.0948	.4052	0.80	.2881	.2119	1.36	.4131	.0869
0.25	.0987	.4013	0.81	.2910	.2090	1.37	.4147	.0853
0.26	.1026	.3974	0.82	.2939	.2061	1.38	.4162	.0838
0.27	.1064	.3936	0.83	.2967	.2033	1.39	.4177	.0823
0.28	.1103	.3897	0.84	.2995	.2005	1.40	.4192	.0808
0.29	.1141	.3859	0.85	.3023	.1977	1.41	.4207	.0793
0.30	.1179	.3821	0.86	.3051	.1949	1.42	.4222	.0778
0.31	.1217	.3783	0.87	.3078	.1922	1.43	.4236	.0764
0.32	.1255	.3745	0.88	.3106	.1894	1.44	.4251	.0749
0.33	.1293	.3707	0.89	.3133	.1867	1.45	.4265	.0735
0.34	.1331	.3669	0.90	.3159	.1841	1.46	.4279	.0721
0.35	.1368	.3632	0.91	.3186	.1814	1.47	.4292	.0706
0.36	.1406	.3594	0.92	.3212	.1788	1.48	.4306	.0694
0.37	.1443	.3557	0.93	.3238	.1762	1.49	.4319	.0681
0.38	.1480	.3520	0.94	.3264	.1736	1.50	.4332	.0668
0.39	.1517	.3483	0.95	.3289	.1711	1.51	.4345	.0655
0.40	.1554	.3446	0.96	.3315	.1685	1.52	.4357	.0643
0.41	.1591	.3409	0.97	.3340	.1660	1.53	.4370	.0630
0.42	.1628	.3372	0.98	.3365	.1635	1.54	.4382	.0618
0.43	.1664	.3336	0.99	.3389	.1611	1.55	.4394	.0606
0.44	.1700	.3300	1.00	.3413	.1587	1.56	.4406	.0594
0.45	.1738	.3264	1.01	.3438	.1562	1.57	.4418	.0582
0.46	.1772	.3228	1.02	.3461	.1539	1.58	.4429	.0571
0.47	.1808	.3192	1.03	.3485	.1515	1.59	.4441	.0559
0.48	.1844	.3156	1.04	.3508	.1492	1.60	.4452	.0548
0.49	.1879	.3121	1.05	.3531	.1469	1.61	.4463	.0537
0.50	.1915	.3085	1.06	.3554	.1446	1.62	.4474	.0526
0.51	.1950	.3050	1.07	.3577	.1423	1.63	.4484	.0516
0.52	.1985	.3015	1.08	.3599	.1401	1.64	.4495	.0505
0.53	.2019	.2981	1.09	.3621	.1379	1.65	.4505	.0495
0.54	.2054	.2946	1.10	.3643	.1357	1.66	.4515	.0485
0.55	.2088	.2912	1.11	.3665	.1335	1.67	.4525	.0475

*Discussed in Section 5.3.

系所組別：工業設計學系乙組

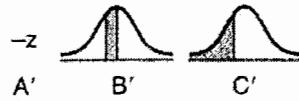
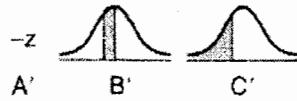
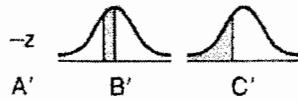
考試科目：統計概論與方法

考試日期：0223，節次：3

※ 考生請注意：本試題不可使用計算機

Table A1 (Continued)
PROPORTIONS (OF AREA) UNDER THE STANDARD NORMAL CURVE FOR VALUES OF Z

A	B	C	A	B	C	A	B	C
1.68	.4535	.0465	2.24	.4875	.0125	2.80	.4974	.0026
1.69	.4545	.0455	2.25	.4878	.0122	2.81	.4975	.0025
1.70	.4554	.0446	2.26	.4881	.0119	2.82	.4976	.0024
1.71	.4564	.0436	2.27	.4884	.0116	2.83	.4977	.0023
1.72	.4573	.0427	2.28	.4887	.0113	2.84	.4977	.0023
1.73	.4582	.0418	2.29	.4890	.0110	2.85	.4978	.0022
1.74	.4591	.0409	2.30	.4893	.0107	2.86	.4979	.0021
1.75	.4599	.0401	2.31	.4896	.0104	2.87	.4979	.0021
1.76	.4608	.0392	2.32	.4898	.0102	2.88	.4980	.0020
1.77	.4616	.0384	2.33	.4901	.0099	2.89	.4981	.0019
1.78	.4625	.0375	2.34	.4904	.0096	2.90	.4981	.0019
1.79	.4633	.0367	2.35	.4906	.0094	2.91	.4982	.0018
1.80	.4641	.0359	2.36	.4909	.0091	2.92	.4982	.0018
1.81	.4649	.0351	2.37	.4911	.0089	2.93	.4983	.0017
1.82	.4656	.0344	2.38	.4913	.0087	2.94	.4984	.0016
1.83	.4664	.0336	2.39	.4916	.0084	2.95	.4984	.0016
1.84	.4671	.0329	2.40	.4918	.0082	2.96	.4985	.0015
1.85	.4678	.0322	2.41	.4920	.0080	2.97	.4985	.0015
1.86	.4686	.0314	2.42	.4922	.0078	2.98	.4986	.0014
1.87	.4693	.0307	2.43	.4925	.0075	2.99	.4986	.0014
1.88	.4699	.0301	2.44	.4927	.0073	3.00	.4987	.0013
1.89	.4706	.0294	2.45	.4929	.0071	3.01	.4987	.0013
1.90	.4713	.0287	2.46	.4931	.0069	3.02	.4987	.0013
1.91	.4719	.0281	2.47	.4932	.0068	3.03	.4988	.0012
1.92	.4726	.0274	2.48	.4934	.0066	3.04	.4988	.0012
1.93	.4732	.0268	2.49	.4936	.0064	3.05	.4989	.0011
1.94	.4738	.0262	2.50	.4938	.0062	3.06	.4989	.0011
1.95	.4744	.0256	2.51	.4940	.0060	3.07	.4989	.0011
1.96	.4750	.0250	2.52	.4941	.0059	3.08	.4990	.0010
1.97	.4756	.0244	2.53	.4943	.0057	3.09	.4990	.0010
1.98	.4761	.0239	2.54	.4945	.0055	3.10	.4990	.0010
1.99	.4767	.0233	2.55	.4946	.0054	3.11	.4991	.0009
2.00	.4772	.0228	2.56	.4948	.0052	3.12	.4991	.0009
2.01	.4778	.0222	2.57	.4949	.0051	3.13	.4991	.0009
2.02	.4783	.0217	2.58	.4951	.0049	3.14	.4992	.0008
2.03	.4788	.0212	2.59	.4952	.0048	3.15	.4992	.0008
2.04	.4793	.0207	2.60	.4953	.0047	3.16	.4992	.0008
2.05	.4798	.0202	2.61	.4955	.0045	3.17	.4992	.0008
2.06	.4803	.0197	2.62	.4956	.0044	3.18	.4993	.0007
2.07	.4808	.0192	2.63	.4957	.0043	3.19	.4993	.0007
2.08	.4812	.0188	2.64	.4959	.0041	3.20	.4993	.0007
2.09	.4817	.0183	2.65	.4960	.0040	3.21	.4993	.0007
2.10	.4821	.0179	2.66	.4961	.0039	3.22	.4994	.0006
2.11	.4826	.0174	2.67	.4962	.0038	3.23	.4994	.0006
2.12	.4830	.0170	2.68	.4963	.0037	3.24	.4994	.0006
2.13	.4834	.0166	2.69	.4964	.0036	3.25	.4994	.0006
2.14	.4838	.0162	2.70	.4965	.0035	3.30	.4995	.0005
2.15	.4842	.0158	2.71	.4966	.0034	3.35	.4996	.0004
2.16	.4846	.0154	2.72	.4967	.0033	3.40	.4997	.0003
2.17	.4850	.0150	2.73	.4968	.0032	3.45	.4997	.0003
2.18	.4854	.0146	2.74	.4969	.0031	3.50	.4998	.0002
2.19	.4857	.0143	2.75	.4970	.0030	3.60	.4998	.0002
2.20	.4861	.0139	2.76	.4971	.0029	3.70	.4999	.0001
2.21	.4864	.0136	2.77	.4972	.0028	3.80	.4999	.0001
2.22	.4868	.0132	2.78	.4973	.0027	3.90	.49995	.00005
2.23	.4871	.0129	2.79	.4974	.0026	4.00	.49997	.00003



(背面仍有題目,請繼續作答)

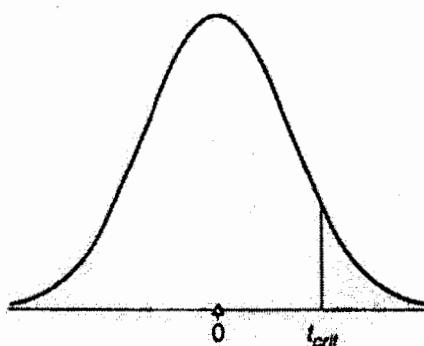
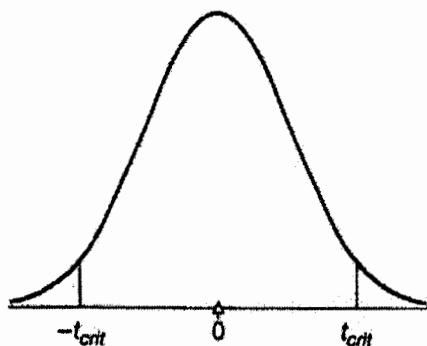
系所組別：工業設計學系乙組

考試科目：統計概論與方法

考試日期：0223，節次：3

※ 考生請注意：本試題不可使用計算機

Table B^a
CRITICAL VALUES OF *t*



Two-tailed or Nondirectional Test
LEVEL OF SIGNIFICANCE
(*p*-value in color)

p > .05 *p* < .05 *p* < .01 *p* < .001

<i>df</i>	.05*	.01**	.001
1	12.708	63.657	636.62
2	4.303	9.925	31.598
3	3.182	5.841	12.924
4	2.776	4.604	8.610
5	2.571	4.032	6.869
6	2.447	3.707	5.959
7	2.365	3.499	5.408
8	2.306	3.355	5.041
9	2.262	3.250	4.781
10	2.228	3.169	4.587
11	2.201	3.106	4.437
12	2.179	3.055	4.318
13	2.160	3.012	4.221
14	2.145	2.977	4.140
15	2.131	2.947	4.073
16	2.120	2.921	4.015
17	2.110	2.898	3.965
18	2.101	2.878	3.922
19	2.093	2.861	3.883
20	2.086	2.845	3.850
21	2.080	2.831	3.819
22	2.074	2.819	3.792
23	2.069	2.807	3.767
24	2.064	2.797	3.745
25	2.060	2.787	3.725
26	2.056	2.779	3.707
27	2.052	2.771	3.690
28	2.048	2.763	3.674
29	2.045	2.756	3.659
30	2.042	2.750	3.646
40	2.021	2.704	3.551
60	2.000	2.660	3.460
120	1.980	2.617	3.373
∞	1.960	2.576	3.291

One-tailed or Directional Test
LEVEL OF SIGNIFICANCE
(*p*-value in color)

<i>df</i>	.05	.01	.001
1	6.314	31.821	318.31
2	2.920	6.965	22.326
3	2.353	4.541	10.213
4	2.132	3.747	7.173
5	2.015	3.365	5.893
6	1.943	3.143	5.208
7	1.895	2.998	4.785
8	1.860	2.896	4.501
9	1.833	2.821	4.297
10	1.812	2.764	4.144
11	1.796	2.718	4.025
12	1.782	2.681	3.930
13	1.771	2.650	3.852
14	1.761	2.624	3.787
15	1.753	2.602	3.733
16	1.746	2.583	3.686
17	1.740	2.567	3.646
18	1.734	2.552	3.610
19	1.729	2.539	3.579
20	1.725	2.528	3.552
21	1.721	2.518	3.527
22	1.717	2.508	3.505
23	1.714	2.500	3.485
24	1.711	2.492	3.467
25	1.708	2.485	3.450
26	1.706	2.479	3.435
27	1.703	2.473	3.421
28	1.701	2.467	3.408
29	1.699	2.462	3.396
30	1.697	2.457	3.385
40	1.684	2.423	3.307
60	1.671	2.390	3.232
120	1.658	2.358	3.160
∞	1.645	2.326	3.090

*Discussed in Section 13.2.

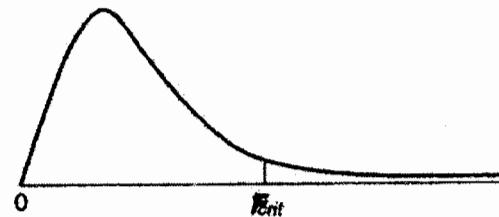
**95% level of confidence.

***99% level of confidence.

系所組別：工業設計學系乙組
考試科目：統計概論與方法

※ 考生請注意：本試題不可使用計算機

Table C¹
CRITICAL VALUES OF F



FINDING p -VALUE

If observed F is

...smaller than light number, $p > .05$

...between light and dark numbers, $p < .05$

... larger than dark number, $p < .0$

.05 level of significance (light numbers)
.01 level of significance (dark numbers)

DEGREES OF FREEDOM IN NUMERATOR

(前面仍有題目，請繼續作答)

※ 考生請注意：本試題不可使用計算機

**TABLE OF CRITICAL
CRITICAL VALUES OF F**

FINDING p-VALUE

If observed F is

- ... smaller than light number, $p > .05$
- ... between light and dark numbers, $p < .05$
- ... larger than dark number, $p < .01$

DEGREES OF FREEDOM IN NUMERATOR

DEGREES OF FREEDOM IN DENOMI- NATOR	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150	151	152	153	154	155	156	157	158	159	160	161	162	163	164	165	166	167	168	169	170	171	172	173	174	175	176	177	178	179	180	181	182	183	184	185	186	187	188	189	190	191	192	193	194	195	196	197	198	199	200	201	202	203	204	205	206	207	208	209	210	211	212	213	214	215	216	217	218	219	220	221	222	223	224	225	226	227	228	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379	380	381	382	383	384	385	386	387	388	389	390	391	392	393	394	395	396	397	398	399	400	401	402	403	404	405	406	407	408	409	410	411	412	413	414	415	416	417	418	419	420	421	422	423	424	425	426	427	428	429	430	431	432	433	434	435	436	437	438	439	440	441	442	443	444	445	446	447	448	449	450	451	452	453	454	455	456	457	458	459	460	461	462	463	464	465	466	467	468	469	470	471	472	473	474	475	476	477	478	479	480	481	482	483	484	485	486	487	488	489	490	491	492	493	494	495	496	497	498	499	500
14	4.60	3.74	3.34	3.11	2.96	2.85	2.77	2.70	2.65	2.60	2.58	2.53	2.48	2.44	2.39	2.35	2.31	2.27	2.24	2.21	2.19	2.16	2.14	2.13	2.11	2.09	2.08	2.07	2.06	2.05	2.04	2.03	2.02	2.01	2.00	1.99	1.98	1.97	1.96	1.95	1.94	1.93	1.92	1.91	1.90	1.89	1.88	1.87	1.86	1.85	1.84	1.83	1.82	1.81	1.80	1.79	1.78	1.77	1.76	1.75	1.74	1.73	1.72	1.71	1.70	1.69	1.68	1.67	1.66	1.65	1.64	1.63	1.62	1.61	1.60	1.59	1.58	1.57	1.56	1.55	1.54	1.53	1.52	1.51	1.50	1.49	1.48	1.47	1.46	1.45	1.44	1.43	1.42	1.41	1.40	1.39	1.38	1.37	1.36	1.35	1.34	1.33	1.32	1.31	1.30	1.29	1.28	1.27	1.26	1.25	1.24	1.23	1.22	1.21	1.20	1.19	1.18	1.17	1.16	1.15	1.14	1.13	1.12	1.11	1.10	1.09	1.08	1.07	1.06	1.05	1.04	1.03	1.02	1.01	1.00	0.99	0.98	0.97	0.96	0.95	0.94	0.93	0.92	0.91	0.90	0.89	0.88	0.87	0.86	0.85	0.84	0.83	0.82	0.81	0.80	0.79	0.78	0.77	0.76	0.75	0.74	0.73	0.72	0.71	0.70	0.69	0.68	0.67	0.66	0.65	0.64	0.63	0.62	0.61	0.60	0.59	0.58	0.57	0.56	0.55	0.54	0.53	0.52	0.51	0.50	0.49	0.48	0.47	0.46	0.45	0.44	0.43	0.42	0.41	0.40	0.39	0.38	0.37	0.36	0.35	0.34	0.33	0.32	0.31	0.30	0.29	0.28	0.27	0.26	0.25	0.24	0.23	0.22	0.21	0.20	0.19	0.18	0.17	0.16	0.15	0.14	0.13	0.12	0.11	0.10	0.09	0.08	0.07	0.06	0.05	0.04	0.03	0.02	0.01	0.00																																																																																																																																																																																																																																																																									
15	4.54	3.66	3.29	3.06	2.90	2.79	2.70	2.64	2.59	2.55	2.51	2.48	2.43	2.39	2.35	2.31	2.27	2.24	2.21	2.18	2.15	2.12	2.10	2.08	2.06	2.04	2.03	2.02	2.01																																																																																																																																																																																																																																																																																																																																																																																																																																																																																							