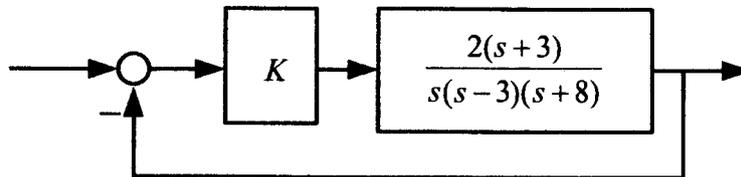


※ 考生請注意：本試題不可使用計算機

1. (15%) Consider the system in the figure, determine the range of  $K$  so that the closed-loop system is stable.



2. (18%) A negative unity feedback control system has the open loop transfer function  $\frac{\omega_n^2}{s(s+2\zeta\omega_n)}$  in which the damping ratio satisfies  $0 < \zeta \leq \frac{1}{\sqrt{2}}$ . Determine

(a) the peak value of the magnitude of the closed-loop frequency response. (9%)

(b) the -3dB system bandwidth. (9%)

3. (33%) A lag-lead compensator is given with the transfer function  $G_c(s) = \left(\frac{s+0.1}{s+0.01}\right)\left(\frac{s+1}{s+10}\right)$ .

(a) Implement this compensator with a passive network. (11%)

(b) Implement this compensator with active realization. (11%)

(c) Implement this compensator using cascade lag and lead networks with isolation. (11%)

4. (24%) A unity feedback control system has the open-loop transfer function,  $KG(s) = K(s+8)^2 / s^3$ .

(a) Please sketch the Nyquist plot for this system and determine the range of  $K$  via this plot such that the feedback control system is stable.. (14%)

(b) If  $K = 20$ , please give the gain margin of this system and its meaning. (10%)

5. (10%) Reduce the state equation  $\dot{X} = \begin{bmatrix} \lambda_1 & 1 & 0 & 0 & 0 \\ 0 & \lambda_1 & 1 & 0 & 0 \\ 0 & 0 & \lambda_1 & 0 & 0 \\ 0 & 0 & 0 & \lambda_2 & 1 \\ 0 & 0 & 0 & 0 & \lambda_2 \end{bmatrix} X + \begin{bmatrix} 1 \\ 2 \\ 0 \\ 0 \\ 3 \end{bmatrix} u$ ,  $y = [0 \ 3 \ 2 \ 0 \ 1]X$ , into a

controllable and observable equation.