

國立成功大學

113學年度碩士班招生考試試題

編 號：116

系 所：工程科學系

科 目：材料力學

日 期：0202

節 次：第 2 節

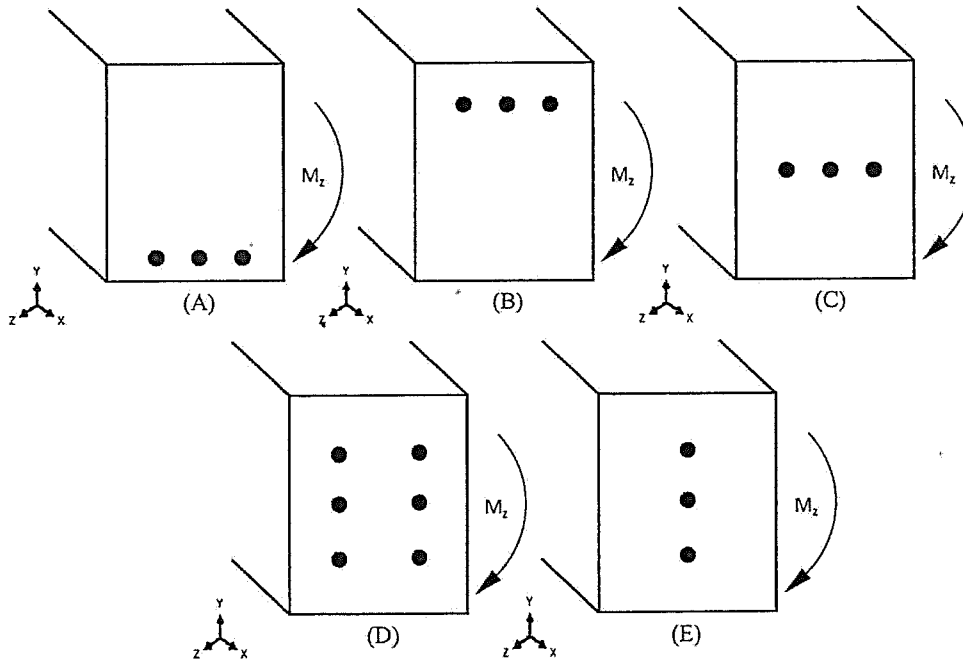
備 註：可使用計算機

※ 考生請注意：本試題可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

Part I Multiple Choice Questions Section (Comprising 30% of the Total Score)

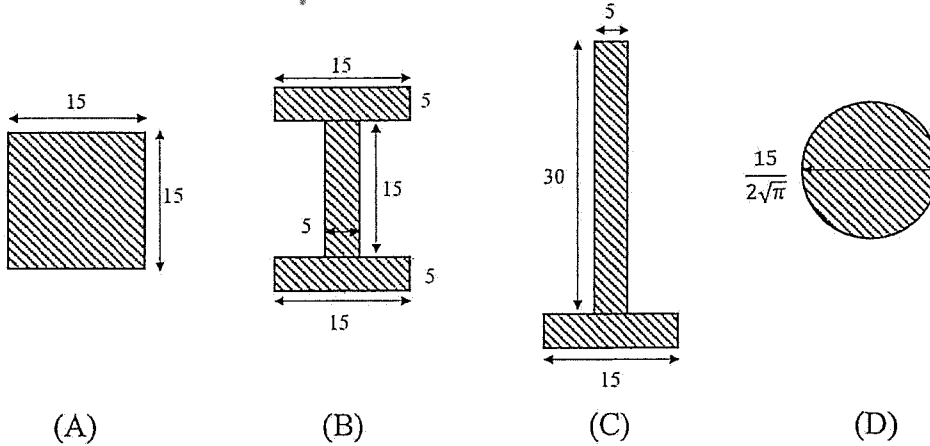
In this part, each question has only **one** correct answer. Correct answers are awarded 6 points, contributing to the overall score. Incorrect answers result in a 3-point deduction (倒扣三分), discouraging guessing. Please note, unanswered questions do not affect the score positively or negatively. If uncertain, it may be strategic to leave a question unanswered to avoid point deduction for incorrect guesses.

1. (6%) In the context of reinforced concrete structures when subjected solely to pure bending — that is, bending characterized by the absence of axial loads or shear forces — which of the specified reinforcement configurations below can withstand the greatest bending moment?



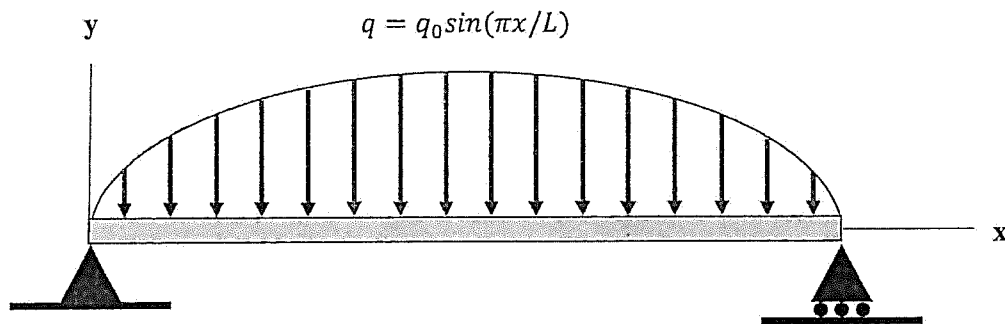
2. (6%) A straight rod with a length of 369mm and a cross-section of width 45mm and length 150mm , made of isotropic linearly elastic-perfectly plastic material with a yield strength of 360MPa . If one end is fixed and the other end is under tension, what is the ultimate load it can withstand?
 (A) 243 N (B) 2430 kN (C) 2.43 kN (D) 2.43 N (E) None of the above
3. (6%) Referencing the previously described straight rod with a fixed end and a free end, which is made of isotropic linearly elastic-perfectly plastic material and has a yield strength of 360 MPa : if the free end is subjected to a bending moment, what is the maximum bending moment (also known as the ultimate bending moment) that the rod can resist before yielding or failing?
 (A) $91.125\text{ kN}\cdot\text{cm}$ (B) $91.125\text{ kN}\cdot\text{mm}$ (C) $91.125\text{ kN}\cdot\text{m}$ (D) $91.125\text{ N}\cdot\text{m}$ (E) None of the above

4. (6%) Considering a beam with a uniform cross-sectional area, when comparing different geometric shapes of sections (such as rectangular, circular, I-shaped, etc.), which geometric shape would experience the highest level of bending stress under the same loading conditions?



5. (6%) Consider a simply supported beam, which is affected by a variable distributed load represented by the equation $q = q_0 \sin(\pi x/L)$, where q represents the load per unit length at a point x along the beam, q_0 is the maximum intensity of the distributed load, and L is the length of the beam. Could you determine the vertical deflection at the midpoint of the beam due to this sinusoidally varying distributed force?

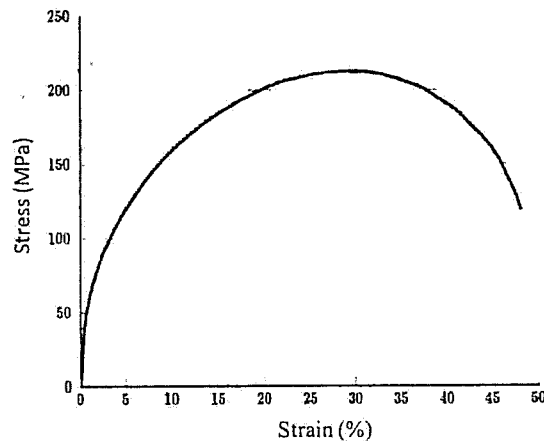
- (A) $\frac{q_0 L^3}{\pi^4 EI}$ (B) $\frac{q_0 L^4}{\pi^3 EI}$ (C) $\frac{q_0 L^2}{\pi^2 EI}$ (D) $\frac{q_0 L^2}{\pi^4 EI}$ (E) $\frac{q_0 L^4}{\pi^4 EI}$



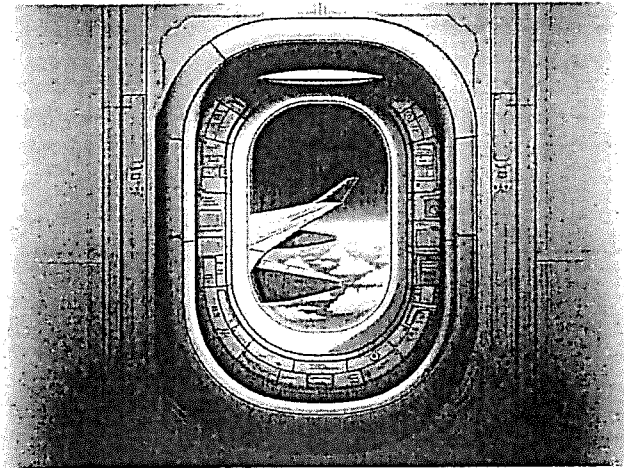
Part II: Conceptual Questions: In-Depth Definitions and Explanations (20% of the Total Score)

You are expected to provide detailed, accurate, and nuanced explanations of various key terms. Each definition should encompass not only the basic description but also a contextual backdrop, including examples or scenarios where applicable, the significance of the term in its respective field, and any pertinent theoretical or practical implications.

1. (5%) Could you explain what the **stress concentration factor** is, and how one might define or calculate it?
2. (5%) What is the primary cause of **plastic deformation** in low carbon steels at room temperature when they are subjected to mechanical loading?
3. (5%) In the context of the stress-strain diagram provided, how would you identify and define the **yield stress**?



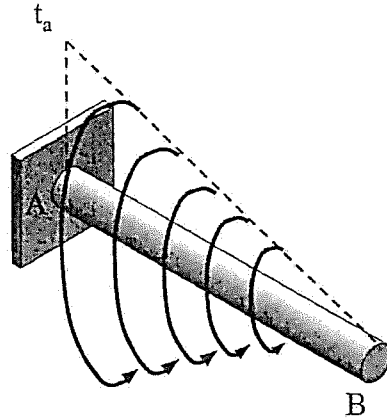
4. (5%) Why are airplane windows designed with an **oval shape**, and what are the benefits of this design choice in terms of structural integrity and safety?



Part III: Derivation Problems (50%)

In this part, you are required to provide comprehensive and detailed derivations for the question presented below. This part will account for 50% of the overall assessment score. Ensure that your derivations are clear, well-structured, and thoroughly explained to demonstrate a deep understanding of the subject matter.

1. (25%) Consider a solid circular shaft, as depicted in the following theoretical diagram. The shaft has point A as the fixed end, a length denoted by L , and a diameter represented by d . It also has a shear modulus G . A torque is applied to the shaft, distributed linearly from t_a at the left end to 0 at the right end. The goal is to determine the relative twist angle between the two ends. This angle should be expressed in terms of L , d , G , and t_a , considering the direction of the applied torque.



2. (25%) Consider a circular ring that is in contact with the ground, assuming friction is negligible. This ring has a radius, denoted as r , thickness t , and possesses a bending stiffness represented by EI . When a force, labeled P , is applied at the ring's top center point (point A), the objective is to determine the vertical displacement at point A. This determination should be made using Castigliano's theorem, which is a principle for calculating displacements in elastic systems subjected to a load.

