

# 國立成功大學

## 113學年度碩士班招生考試試題

編 號： 73

系 所： 化學工程學系

科 目： 化工熱力學

日 期： 0201

節 次： 第 2 節

備 註： 可使用計算機

※ 考生請注意：本試題可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

**Problem 1 (13%)**

Internal pressure can be used to measure the change in internal energy of a system when it expands or contracts at constant temperature,  $(\frac{\partial U}{\partial V})_T$ . (U and V are the molar properties)

(a) Please show the internal pressure of a gas obeying ideal gas behavior or van der Waals equation,  $(P + \frac{a}{V^2})(V - b) = RT$ . (5%)

(b) A gas is assumed to obey the van der Waals equation and these two parameters,  $a = 1.4 (\frac{\text{atm} \times \text{dm}^6}{\text{mol}^2})$  and  $b = 0.04 (\frac{\text{dm}^3}{\text{mol}})$ . If 5 mol of this gas expands reversibly isothermally at 300 K from an initial volume of 2.5 dm<sup>3</sup> to a final volume of 10 dm<sup>3</sup>, please calculate the changes in heat (Q), work (W), internal energy (U), and enthalpy (H) during the expansion process. (8%)

**Problem 2 (9%)**

A liquid with a boiling point at 450 K and 1 atm. This liquid can be superheated to 465 K at 1 atm and then changing to vapor at the same temperature and pressure. Is this process spontaneous?

PS:  $\Delta H_{vap} = 45.6 \frac{\text{kJ}}{\text{mol}}$  at 450 K and 1 atm.  $C_{p,l} = 78 \frac{\text{J}}{\text{K-mol}}$  and  $C_{p,g} = 35 \frac{\text{J}}{\text{K-mol}}$ . (9%)

**Problem 3 (12%)**

Calculate the maximum temperature of complete combustion of ethylene at 298 K with:

- (a) The theoretical amount of air at 298 K. (6%)  
 (b) 20% excess air at 298 K. (6%)

	$\Delta H_f^0 (298\text{K})$ (kJ/mol)	$C_p^0$	
		A (J/K-mol)	$10^3 B$ (J/K <sup>2</sup> -mol)
C <sub>2</sub> H <sub>4</sub> (g)	52.5	11.8	119.7
H <sub>2</sub> O(g)	-241.8	30.5	10.3
H <sub>2</sub> O(l)	-285.8	75.5	0
CO <sub>2</sub> (g)	-393.5	44.2	8.8
O <sub>2</sub> (g)	0	30.0	4.2
N <sub>2</sub> (g)	0	28.6	3.8

PS:  $C_p^0 = A + BT$  is used over the working temperature region

$C_p^0$  and  $\Delta H_f^0$  mean the heat capacity and enthalpy at standard state (1 atm and 298 K)

**Problem 4 (20%)**

The equation of state for the van der Waals (vdW) fluid is given as  $\left(P + \frac{a}{V^2}\right) \cdot (V - b) = RT$ , where  $P$ ,  $V$ , and  $T$  are the pressure, molar volume and temperature, respectively, as well as  $a$  and  $b$  are constants specific to this vdW fluid.

(1) Please calculate the residual internal energy of this vdW fluid,  $U^R$ . (8%)

(2) Please estimate the residual enthalpy of this vdW fluid,  $H^R$ . (8%)

(3) Please compute  $\left(\frac{\partial C_v}{\partial V}\right)_T$  of this vdW fluid. (4%)

Please clearly state all assumptions you made leading to your answers. Express  $U^R$ ,  $H^R$  and  $\left(\frac{\partial C_v}{\partial V}\right)_T$  with proper thermodynamic variables. In your answers to (1) and (2), you could use  $C_P^R$  and  $C_V^R$  for isobaric and isochoric residual heat capacities, respectively.

**Problem 5 (13%)**

One mole of an ideal gas with  $C_P = (7/2) R$  and  $C_V = (5/2) R$  is compressed adiabatically in a piston-cylinder device from 2 bar and 300 K to 8 bar. The process is irreversible and requires 40% more than a reversible, adiabatic compression from the same state to the same final state on the same piston-cylinder device. Please calculate the final temperature and the entropy change of the gas.

**Problem 6 (6%)**

$G^E/RT$ ,  $\ln \gamma_1$ ,  $\ln \gamma_2$  must intersect at a point. If this were the case, please prove that it is real.

**Problem 7 (8%)**

Determine the following statements are "True" or "False".

(1)  $x_1 \bar{G}_1 + x_2 \bar{G}_2 = G$ , therefore  $x_1 \left(\frac{\partial \bar{G}_1}{\partial T}\right)_{P,x} + x_2 \left(\frac{\partial \bar{G}_2}{\partial T}\right)_{P,x} = \left(\frac{\partial G}{\partial T}\right)_{P,x}$  Hence,  $-x_1 \bar{S}_1 - x_2 \bar{S}_2 = -S$

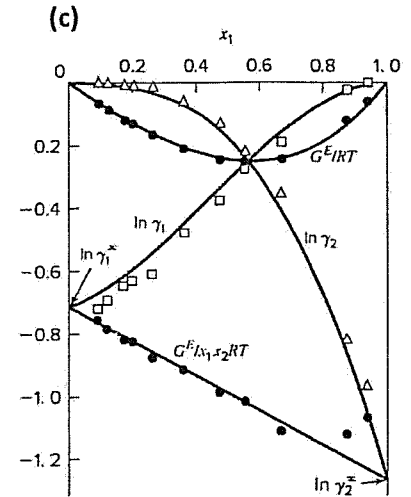
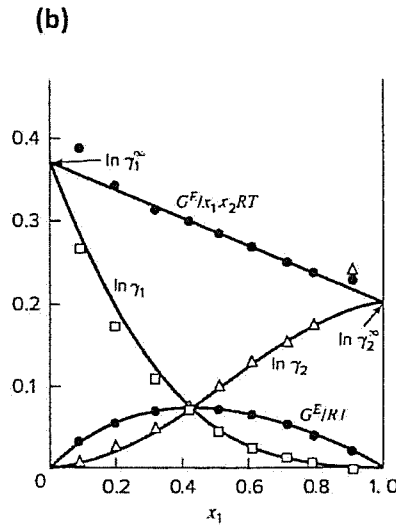
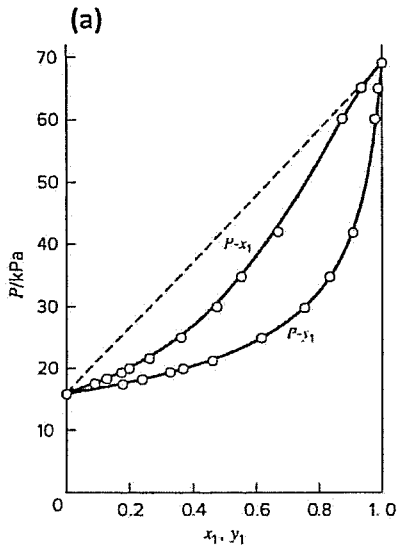
(2) When  $x_2 \rightarrow 1$ , the slope of  $\ln \gamma_1$  vs  $x_1$  approaches 0.

背面尚有試題

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**Problem 8 (5%)**

Which figure (Figure (b) or Figure (c)) is related to Figure (a)? Please choose.



**Problem 9 (14%)**

(a) Please choose two from the sections (a), (b), (c), (d), (e), (f) which are related to Fig. 1. (8%)

(b) Please explain the reason on your choice. (6%)

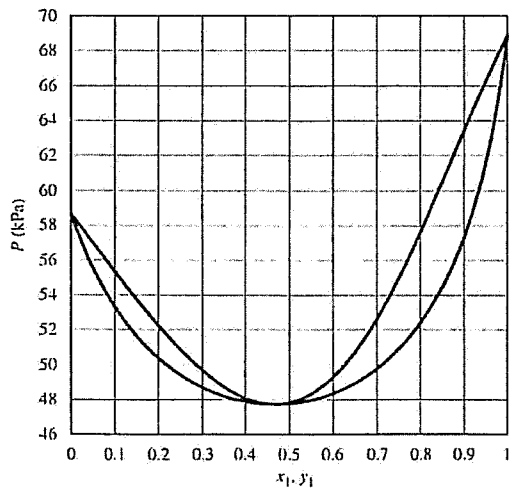


Fig. 1 Pxy diagram for vapor/liquid equilibrium of a mixed-solvent system at 50°C.

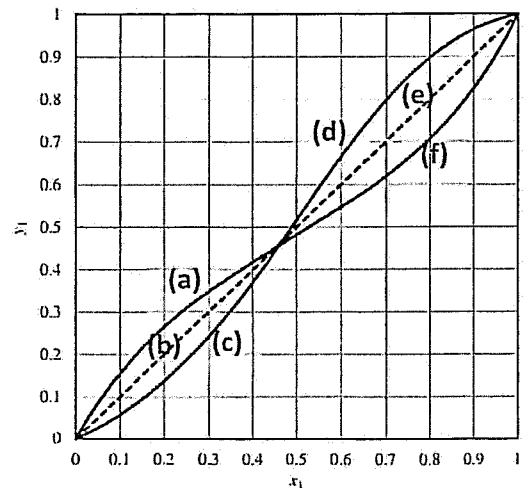


Fig. 2 xy diagram for different mixed-solvent system at 1 bar.