

# 國立臺北大學 111 學年度碩士班一般入學考試試題

系(所)組別：都市計劃研究所甲組

科目：微積分

第1頁 共1頁

可 不可使用計算機

- (10%) Suppose the function  $f(x) = 3x^3 - ax^2 + bx + c$  has extreme values at  $x = 1, \frac{1}{3}$  and  $f(2) = 0$ . Find  $a, b, c$ .
- (20%) Evaluate the following limit.
  - $\lim_{x \rightarrow 0} \left(\frac{1}{x^2}\right)^x$
  - $\lim_{y \rightarrow \pi/2} \left(\frac{\pi}{2} - y\right) \tan y$
  - $\lim_{t \rightarrow 1} \frac{t-1}{\ln t - \sin \pi t}$
  - $\lim_{x \rightarrow 2} \frac{x-2}{x^2-4}$
- (20%) Evaluate the following integrals.
  - $\int_0^2 x\sqrt{16-3x^2} dx$
  - $\int x \cos 2x dx$
  - $\int \frac{e^x + e^{-x}}{e^x - e^{-x}} dx$
  - $\int \frac{2x+1}{3x^2+x-2} dx$
- (10%) Find the local extrema of  $f(x) = \frac{12}{5}x^5 + \frac{5}{4}x^4 - \frac{14}{3}x^3 - \frac{5}{2}x^2 + 2x + 3$ , where  $-1 \leq x \leq 1$ .
- (10%) Find the tangent line of  $x^4 - x^2y + 2xy^4 = 4$  passing through  $(1,1)$ .
- (10%) Find  $\iint_R x + y dA$ , where  $R = \{(x,y) | 0 \leq 2y \leq x+4, x \leq y \leq x-2\}$ .
- (20%) Find the radius of convergence of the power series.
  - $\sum_{n=0}^{\infty} x^n$
  - $\sum_{n=0}^{\infty} \frac{x^{2n+1}}{n!}$
  - $\sum_{n=0}^{\infty} \frac{(4x-5)^{2n+1}}{n^{3/2}}$
  - $\sum_{n=0}^{\infty} (-2)^n (n+1)(x-1)^n$

試題隨卷繳交