

國立高雄第一科技大學 101 學年度 碩士班 招生考試 試題紙

系所別：機械與自動化工程系

組別：不分組

考科代碼：2132

考科：工程數學(二)

注意事項：

- 1、本科目得使用本校提供之電子計算器。
- 2、請於答案卷上規定之範圍作答，違者該題不予計分。

1. Please find the general solution of the given linear system: (15%)

$$\begin{aligned}x_1 - x_2 + 3x_3 - x_4 &= 1 \\x_2 - 3x_3 + 5x_4 &= 2 \\x_1 - x_3 + x_4 &= 0 \\x_1 + 2x_3 - x_4 &= -5\end{aligned}$$

2. Please find (a) an orthogonal matrix that (b) diagonalizes the given matrix A : (15%)

$$A = \begin{bmatrix} 3 & 0 & -2 \\ 0 & 2 & 0 \\ -2 & 0 & 0 \end{bmatrix}$$

3. Please find the angle between the two surfaces at the given point of intersection. (15%)

$$S_1: x^2 + y^2 + z^2 = 4; \quad S_2: z^2 + x^2 = 2; \quad \text{at } (1, \sqrt{2}, 1)$$

4. Please find the flux of $\vec{F} = x\vec{i} + y\vec{j} + z\vec{k}$ across the part of the sphere $x^2 + y^2 + z^2 = 4$ lying between the planes $z = 1$ and $z = 2$. (15%)

5. (a) Please solve for all z such that $e^z = 1 + 2i$. (10%)

- (b) If the three roots for $z^3 = 1$ are z_1, z_2, z_3 , please find $z_1 + z_2 + z_3 = ?$ (10%)

6. Please find the temperature $u(x, t)$ in a laterally insulated copper bar 80 cm long if the initial temperature is $100 \sin(\pi x/80)^\circ\text{C}$ and both ends are kept at 0°C . How long will it take for the maximum temperature in the bar to drop to 50°C ? (density for copper is $\rho = 8.92 \text{ gm/cm}^3$, specific heat $\sigma = 0.092 \text{ cal/gm }^\circ\text{C}$, and thermal conductivity $k = 0.95 \text{ cal/cm sec }^\circ\text{C}$) Please solve the problem with one dimensional heat equation: $\partial u / \partial t = c^2 \partial^2 u / \partial x^2$, where $c = k / \rho \sigma$. (20%)