系所:

科目:統計學

經營管理研究所(無組別)

是否使用計算機:是

考試時間:100分鐘 本科原始成績:100分

I. (60%)MULTIPLE CHOICE QUESTION

所有的答案請寫在答案卷,答案寫法如下列所示:

All answers must be written on the answer sheet

for example:

1	a	6	a	11	16	
2	b	7	b	12	17	
3	c	8	С	13	18	
4	d	9	d	14	19	
5	a	10	a	15	20	

- 1. Which of the following statement on a simple OLS regression function $\hat{Y} = \hat{\alpha} + \hat{\beta}X$ is true?
- a) Coefficient of determination \mathbb{R}^2 is equal to the correlation coefficient of the sample value X and Y.
- b) More samples necessarily leads to a lower $Var(\hat{\beta})$.
- c) $Var(\hat{\beta})$ is always greater than $Var(\hat{\alpha})$.
- d) Under the same significant level, if $\hat{\beta}$ is significantly greater than zero, then $\hat{\alpha}$ is also significantly greater than zero.
- 2. Which of the following statements is true?
- a) Third degree central moment equal to zero is a sufficient condition for a distribution to be symmetric.
- b) Fourth degree central moment is used to evaluate the skewness of a distribution.
- c) Fourth degree central moment is no less than third degree central moment for a symmetric distribution.
- d) A distributions skew to the right has positive third degree central moment.

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3. Which of the following statement about uniform distribution is true?

- a) It is a symmetric distribution.
- b) The cumulated probability function is independent of the random variable.
- c) Uniform distribution has zero mean.
- d) All the uniform distributions have equal variance.
- 4. Which of the following statement about Poisson distribution is **not** true?
- a) It is not a symmetric distribution.
- b) Its mean and variance are equal.
- c) Value of the random variable needs to be nonnegative.
- d) Sum of two independent Poisson distributions is not a Poisson distribution.
- 5. Which of the following statement about a χ^2 distribution is true?
- a) The shape of its probability density curve depends on the degree of freedom.
- b) It is a symmetric distribution.
- c) The value of the random variable can be negative.
- d) It is a ratio of two t distributions.
- 6. N samples is randomly selected from a normal distribution population with $X \square N(\mu, \sigma^2)$.

$$p\lim \frac{1}{N} \sum_{i=1}^{N} X_i =$$

- a) σ^2
- b) μ^2
- c) $\sigma^2 + \mu^2$

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d)
$$\frac{\sigma^2 + \mu^2}{2}$$

- 7. Along with 6, if we have two estimators $\overline{X} = \frac{1}{N} \sum_{i=1}^{N} X_i$ and $\widetilde{X} = \frac{1}{N+1} \sum_{i=1}^{N} X_i$ to estimate μ , which of the following statement is true?
- a) Both are unbias.
- b) Only \overline{X} is asymptotically unbias.
- c) \tilde{X} is more efficient than \bar{X} .
- d) Only \overline{X} is a consistent estimator.
- 8. If random variable X is uniformly distributed between 2 and 4, then Var(X) =
- a) $\frac{1}{2}$.
- b) $\frac{1}{3}$.
- c) $\frac{1}{4}$.
- d) $\frac{1}{12}$.
- 9. In a simple OLS regression function, which of the following distribution can be used to test whether *X* has a significant impact on Y?
- a) binomial distribution
- b) t distribution
- c) chi-square distribution
- d) hypergeometric distribution
- 10. The distribution of a standardized random variable will approach a standard normal

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distribution when the sample size is large enough is called _____.

- a) The central limit theorem
- b) Law of big data
- c) Law of normal distribution.
- d) Law of large number
- 11. To test that per capita GDP of Taiwan in 2019 is no less than twenty thousand US dollars, if the significant level is 5%, which of the following statement is true?
- a) Two tailors test is needed.
- b) Right tailor is needed.
- c) If the P-value is 0.03, then we cannot rejected null hypothesis.
- d) For a given sample, the P-value is negatively related to the per capita GDP level that we want to test.
- 12. If random variables X and Y are independent, and V(X) = 20 , V(Y) = 16, then V(2X + 0.5Y) =
- a) 48.
- b) 64.
- c) 84.
- d) 96.
- 13. The sum of three binomial random variables is a
- a) Poisson distribution.
- b) Laplace distribution.

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- c) hypergeometric distribution.
- d) normal distribution.

考試時間:100分鐘

- 14. Which of the following statements about the property of an estimator is **not** true?
- a) Unbias cannot assure consistent.
- b) Consistent not necessarily assures unbias.
- c) There are only one estimator with the properties of both unbias and consistency.
- d) An unbias estimator is not necessarily more efficient than a bias estimator.
- 15. When we use n random samples (X_i, Y_i) to obtain the OLS regression function $\hat{Y}_i = \hat{\alpha} + \hat{\beta}X_i$, the coefficient of determination R^2 is not equal to
- a) r_{xy}^2
- c) $\frac{\hat{\beta}\sum (X_i \overline{X})^2}{\sum (Y_i \overline{Y})^2}$
- d) $\frac{\sum (Y_i \hat{Y}_i)^2}{\sum (Y_i \overline{Y})^2}$
- 16. In general, we use _____to test whether the variance of two populations are equal.
- a) z-test
- b) t-test
- c) χ^2 test
- d) F test

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- 17. According to Chebyshev inequality, the probability that the distance between a random variable and the expected value of the random variable is no greater than three times of standard deviation is no less than
- a) $\frac{1}{4}$
- b) $\frac{3}{4}$
- c) $\frac{8}{9}$
- d) $\frac{15}{16}$
- 18. The probability density function of random variable X is $f(x) = \frac{e^{-3}3^x}{x!}$, x = 0,1,2...Var(X) = ?
- a) 1
- b) 3
- c) 6
- d) 9
- 19. A normal distribution is $X \square N(\mu, \theta)$ with known mean μ and unknown variance θ . If we have n samples $x_1, x_2, ... x_n$, the maximum likelihood estimator of θ is
- a) $\frac{1}{n} \sum_{i=1}^{n} (x_i \mu)^2$.
- b) $\frac{1}{n-1}\sum_{i=1}^{n}(x_i-\mu)^2$.
- c) $\frac{1}{n} \sum_{i=1}^{n} (x_i \overline{x})^2$.
- d) $\frac{1}{n} \sum_{i=1}^{n} (x_i \overline{x})^2$.

科目:統計學

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20. There are two projects as follows:

Project A: If success, the profit is 400,000; if not success: the loss is 40,000.

Project B: If success, the profit is 500,000; if not success: the loss is 115,000.

If they have the same success probability and expected profit, the success probability is

- a) $\frac{1}{4}$.
- b) $\frac{2}{7}$.
- c) $\frac{3}{7}$.
- d) $\frac{4}{7}$.

II (20%) $Y = \alpha + \beta X + \varepsilon$ is the impact of X on Y in the population. If we have 40 random samples of (x_i, y_i) , and have $r_{XY} = 0.9$, $\overline{X} = 600$, $\overline{Y} = 6$, $S_X = 60$, $S_Y = 0.8$

- (i) Find the OLS equation $\hat{Y} = \hat{\alpha} + \hat{\beta}X$ and R^2 .
- (ii) If we transform the 40 random samples to regress $2+0.8y_i$ on $100+1.2x_i$, find the OLS equation $\tilde{Y} = \tilde{\alpha} + \tilde{\beta}X$ and R^2 .

III (20%) Let $Y_1, Y_2, Y_3, \dots, Y_n$ be n uncorrelated random variables with the same mean μ and variance σ^2 and denote \overline{Y} as the sample average.

- (i) Find $E(\overline{Y})$ and $Var(\overline{Y})$.
- (ii) If we define the class of linear estimators of μ as $G = a_1Y_1 + a_2Y_2 + \dots + a_nY_n$,

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本科原始成績:100分

where every a_i is constant, if G is an unbiased estimator of μ , what restriction on the a_i needed?

- (iii) Find Var(G)
- (iv) Along with (i)-(iii), show that $Var(G) \ge Var(\overline{Y})$.