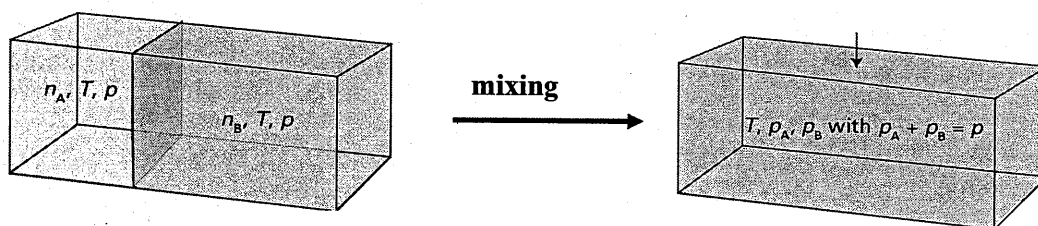


※ 考生請注意：本試題不可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

一、簡答題：每題 5 分，答案正確才給分 (40 %)

1. For the process involving pure compound B:  $B(s) \rightarrow B(l)$ ,  $\Delta H^\circ = 9.0 \text{ kJ/mol}$ , the melting point is  $27^\circ\text{C}$ , and  $\Delta S^\circ = 30.0 \text{ J/mol}\cdot\text{K}$ . What is the entropy change of this transformation?
2. Write down an equation to prove why heat spontaneously transfers from higher temperature to lower temperature in a closed system?
3. Calculate the value of the  $\Delta G_{\text{mix}}$  for the ideal gases in terms of molar fractions of  $\chi_A$  and  $\chi_B$  in the following figure.



4. Suppose the concentration of a solute decays exponentially ( $c = c_0 \exp(-x/\lambda)$ ,  $\lambda$ : decay constant) along the length of a container. Please calculate the thermodynamic force.
5. When a sample of 4-heptanone was irradiated for 100 s with 300 nm radiation with a powder of 100 W under conditions of total absorption, it was found that 3.0 mmol  $\text{C}_2\text{H}_4$  was formed. Please calculate the quantum yield of  $\text{C}_2\text{H}_4$  formation. (列出式子即可，無須算出絕對數值)
6. Use the molar partition function ( $q_m$ ) and the difference in molar energies ( $\Delta_r E^0$ ) of ground states of product (P) and reactant (R) to demonstrate the chemical equilibrium constant for a reaction of  $\text{R} \leftrightarrow \text{P}$ .
7. Calculate the energy of a particle in a two dimensional square box of side  $L$  in the state with  $n_1 = 3$  and  $n_2 = 8$ .
8. Use the Hückel approximation to set up the Hamiltonian matrix for the  $\pi$  orbitals of cyclobutadiene.

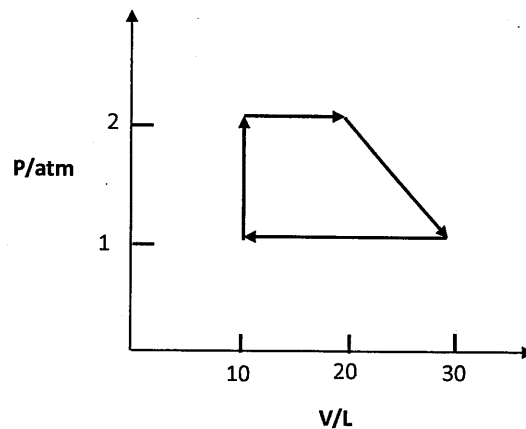
二、問答題 (每題 10 分，須寫出計算或推導過程才予計分) (60 %)

1. In the Eley-Rideal mechanism of a surface catalyzed reaction, a gas-phase molecule (A) collides with another molecule (B) already absorbed on the surface. The adsorption B follows a Langmuir isotherm. Please calculate the  $\theta_B$  and derive the Eley-Rideal rate law in terms of  $P_A$ ,  $P_B$ ,  $k_r$ : rate constant and  $\alpha = k_a/k_d$

2. (a) A polyester can be regarded as the stepwise condensation from a hydroxyacid HO-M-COOH monomer. We expect the -COOH concentration decreasing to be overall second-order in the concentration of -OH and -COOH (denoted as A) groups. Please derive the integration rate law of the polymerization, in which the rate constant is independent of the chain length. (6 %)

(b) It is known that the degree of polymerization is  $[A]_0/[A]$ , please derive the degree of polymerization in terms of rate constant and give a simple method to increase the polymer chain length of the stepwise polymerization? (4 %)

3. Calculate the  $w$ ,  $q$  and  $\Delta S$ ,  $\Delta S(\text{surrounding})$  and  $\Delta S(\text{universe})$  of the following cycle when the surrounding temperature is keep at  $27^\circ\text{C}$ .



4. (a). Draw a plot of the Gibbs energy vs. temperature of a pure substance in solid, liquid and gas phases and also demonstrate the melting, vaporization and sublimation points. (5 %)

(b). Derive the equation of  $G(p) = G(p_0) + RT \ln(p/p_0)$  for an ideal gas. (2%)

(c). Draw a forbidden point of a one-component system. (3 %)

5. (a). Draw a diagram to show the atomic orbital energy levels of H and F atoms and the molecular orbitals they form. From this diagram, please explain why the HF is polar molecule. (6 %)

(b). The general form of the HF molecular orbital is  $\psi = C_H \psi_H + C_F \psi_F$  ( $C_H$  and  $C_F$  are the coefficients of H and F atoms). In the anti-bonding orbital, which value ( $C_H$  or  $C_F$ ) is larger? Why? (4 %)

6. (a). Use *total* wavefunction including the spin of the particles to prove the Pauli exclusion principle. (6 %)

(b). The ruby ( $\text{Al}_2\text{O}_3$  containing small portion of  $\text{Cr}^{3+}$  ions) laser is an example three-level laser. The ground state is  $^4\text{A}$  of the  $\text{Cr}^{3+}$  ion. The process of pumping a majority of the  $\text{Cr}^{3+}$  ion into  $^4\text{T}$  excited state is followed by a radiationless transition to the  $^2\text{E}$  excited state. The laser transition is  $^2\text{E} \rightarrow ^4\text{A}$ , and give rise to 694 nm radiation. Please use the above description to draw the transitions of the energy states in a ruby laser. (4 %)