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國立政治大學圖書館

1. Let the national-income model be
- $$Y = C + I + G_0 \quad (C = \text{Consumption}, Y = \text{Income}, I = \text{Investment},$$
- $$C = a + b(Y - T_0) \quad G = \text{Government Expenditure}, T = \text{Income Tax})$$
- $$I = c + dY$$
- (a) Identify the endogenous variables.
- (b) Write the model in matrix notation and test whether the coefficient matrix is nonsingular.
- (c) Solve the system by Gauss-Jordan reduction method. ($\bar{Y}, \bar{C}, \bar{T}$)
- (d) Find $\frac{\partial Y}{\partial G_0}, \frac{\partial Y}{\partial T_0}$. Interpret their meaning and determine their sign. (20%)

2. For the matrix

$$A = \begin{bmatrix} 0 & 2 & 2 \\ 2 & 0 & 2 \\ 2 & 2 & 0 \end{bmatrix}$$

- (a) Write the characteristic equation and eigenvalues.
- (b) Find the eigenvectors corresponding to the eigenvalues.
- (c) Diagonalize A by an orthogonal matrix. (20%)

3. A consumer has utility function

$$U = x_1 x_2$$

And she faces the money-income constraint

$$2x_1 + 3x_2 \leq 100$$

And the time constraint

$$x_1 + 4x_2 \leq 80$$

Solve for her utility-maximizing consumption bundle and the values of the shadow prices of the constraints. (15%)

4. Given production function $Q = Q(L, K)$

- (a) How would you express algebraically the Isoquant for the output of 260?
- (b) Write out the slope of the Isoquant.
- (c) Write out the profit function of the firm.
- (d) Find the first and second order condition for the optimal combination of inputs.
- (e) Find the comparative-static derivatives $\frac{\partial \bar{L}}{\partial P}, \frac{\partial \bar{L}}{\partial P_L}, \frac{\partial \bar{L}}{\partial P_K}$
- (L=lable, K=capital, P = price of the product, P_L = price of L, P_K = price of K) (20%)

5. Solve $(t + y^2)dy + (y - t^2)dt = 0$ (10%)

6. Evaluate

(a) $\int_0^1 \int_{\sqrt{y}}^1 e^{y^2} dy dx$

(b) $\int_0^1 x \ln x dx$

(15%)