

考試科目	微積分	所別	圖書所	考試時間	4月2日(上) 星期日 午第一節
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1. A company estimates that it can sell 1000 units per week if it sets the unit price at \$ 3.00, but that its weekly sales will rise by 100 units for each 10¢ decrease in price. If  $x$  is the number of units sold each week ( $x \geq 1000$ ), find:
  - (a) (10%) the price function,  $p(x)$
  - (b) (10%) the number of units and the corresponding price that will maximize weekly revenue;
  - (c) (10%) the maximum weekly revenue.
  
2. (15%) Find the vertical and horizontal asymptotes of the graph of  $y = f(x)$  if
 
$$f(x) = \frac{2x}{x-1}$$
  
3. (15%) Find the number  $c$  guaranteed by the Mean Value Theorem for
 
$$f(x) = 2\sqrt{x} \text{ on } [1,4].$$
  
4. (15%) Evaluate  $\int_0^1 [x^2 + (x^2 + 1)^4 x] dx$
  
5. (a) (15%) Find the equation of the tangent line  $x^2 y^2 + 3xy = 10y$  at the point (2,1)
  
- (b) (10%) Find  $dy/dx$  :  $y = \sqrt[3]{x} + \frac{1}{\sqrt{x}}$

備	考	試題隨卷繳交
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命題委員：

(簽章) 91年 3月 29日