

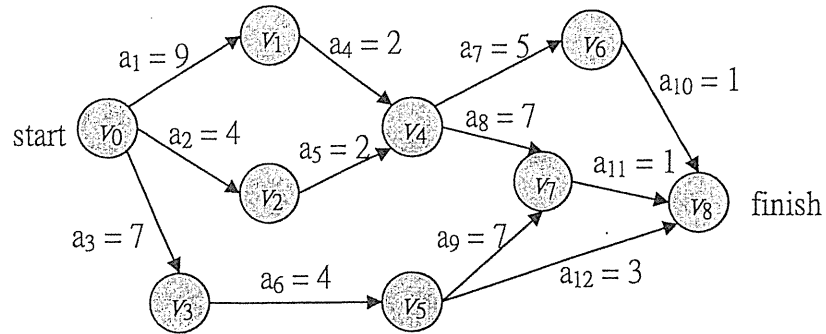
※ 考生請注意：本試題不可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

Part I.

資料結構 (50%)

1. Answer **True** or **False** for the following statements. Give correct answers or explain clearly for **False** statements. (12%)
 - (1) Let G be a graph with e edges and v vertices. If G is represented by adjacency matrix, DFS requires $O(e^2)$ time. (4%)
 - (2) The path from vertex u to vertex v on a minimal cost spanning tree of an undirected graph G is also a shortest path from u to v . (4%)
 - (3) In static hashing, the worst-case number of comparisons needed for a successful search is $O(n)$ for open addressing. The number could be reduced to $O(\log n)$ by using chaining method. (4%)

2. Consider the following AOE network: (18%)



- (1) Obtain $e(i)$ and $l(i)$ for all activity i . (7%)
 - (2) List all critical activities. (7%)
 - (3) List all critical paths. (4%)
3. Given the following 8 runs: (20%)

5	8	23	1	4	3	16	11
13	18	27	15	10	20	17	21
22	30	38	19	24	32	35	25

- (1) Draw the corresponding winner tree. (5%)
- (2) Draw the restructured winner tree after one record has been output. (5%)
- (3) Draw the loser tree based on the answer of question (2). (5%)
- (4) Derive the total required time to merge n records through a winner tree with k runs. (5%)

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二、演算法：(50%)

4. (10%) How can we prove the given problem is NP-complete?
5. (10%) Give an algorithm that determines whether or not a given undirected graph $G=(V,E)$ contains a cycle. Your algorithm should run in $O(V)$ time, independent of $|E|$.
6. (10%) True or false, please explain your answer.
 - (a) (2%) 0-1 knapsack problem can be solved by greedy strategy.
 - (b) (2%) In an undirected graph, we can apply the Depth-First-Search algorithm (DFS) to get tree edges and cross edges.
 - (c) (2%) Based on the top-down approach, we can use the memorization to reduce the time.
 - (d) (2%) Unweighted longest simple path problem has the optimal sub-structure.
 - (e) (2%) If we first apply the topology sort to a directed graph and then run the DFS algorithm on this graph, no back edges can be obtained.
7. (10%) Use Master theorem to solve the recurrence $T(n) = T(2n/3) + 1$.
8. (10%) Write the breadth first spanning tree starting at node 0 (visit the smaller number first).

