

# 國立臺北科技大學 108 學年度碩士班招生考試

系所組別：1411、1412、1413、1421、1422

能源與冷凍空調工程系碩士班甲、乙組

## 第一節 工程數學 試題

第一頁 共一頁

### 注意事項：

1. 本試題共 6 題，共 100 分。
2. 不必抄題，作答時請將試題題號及答案依照順序寫在答案卷上。
3. 全部答案均須在答案卷之答案欄內作答，否則不予計分。

1. Solve the Bernoulli differential equation. (15%)

$$y' + \frac{1}{x}y = 3x^2y^3$$

2. Find the solution by the method of undetermined coefficients. (15%)

$$y'' + 2y' - 3y = 4x^2 - x + 11e^{2x}$$

3. Find the solution by a power series method. (20%)

$$y'' + x^2y = 0$$

4. Solve the initial value problem by Laplace transform. (15%)

$$y'' + 4y = f(t), y(0) = 0, y'(0) = 0$$

$$\text{where } f(t) = \begin{cases} 0 & \text{for } t < 3 \\ t & \text{for } t \geq 3 \end{cases}$$

5. Solve the initial value problem by Laplace transform. (15%)

$$y'' - 2y' - 8y = f(t), y(0) = 1, y'(0) = 0$$

6. Solve the initial value problem by Laplace transform. (20%)

$$x'' - 2x' + 3y' + 2y = 4$$

$$2y' - x' + 3y = 0$$

$$x(0) = x'(0) = y(0) = 0$$