

國立聯合大學 108 學年度碩士班考試招生

電機工程學系 入學考試試題

科目： 工程數學 第 1 頁共 1 頁

1. Solve the initial value problem of the following differential equations.

(1). $y' - 2y = e^{-x}y^2, y(0) = 4$ (10%)

(2). $xy \sin x dx + (\sin x - x \cos x + y^2) dy = 0, y(0) = 3$ (10%)

(3). $y'' - 4y' + 4y = 8e^{2x}, y(0) = 1, y'(0) = 4$ (10%)

(4). $x^2y'' - 3xy' + 8y = 0, y(1) = 1, y'(1) = 5$ (10%)

2. Find the solutions of the following differential equations using Laplace transforms.

(1). $y'' + 3y' + 4y = \delta(t - 2), y(0) = 1, y'(0) = 3$ (10%)

(2). $y(t) + 2 \int_0^t y(t - \tau) \sin(\tau) d\tau = e^{-t}$ (10%)

3. There is the linear transformation $Av = W$, where the matrix of the linear transformation is

$$A = \begin{bmatrix} 4 & 0 & -2 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}.$$

(1). Find three eigenvalues of matrix of the linear transformation. (10%)

(2). Find three eigenvectors with respect to the eigenvalue of matrix of the linear transformation. (10%)

4. Calculate the following integral of the complex functions by using the residue theorem.

(1). $\oint_C \left(\frac{ze^{\pi z}}{z^2 - 4} + 2ze^{\pi/z} \right) dz$, counterclockwise around the circle $C: x^2 + 9y^2 = 9$. (10%)

(2). $\oint_C \frac{e^z \cos z}{(z - \pi/4)^3} dz$, counterclockwise around the circle $C: |z| = 1$. (10%)