

系 所：資源工程學系

考試科目：統計學

考試日期：0223，節次：3

第1頁，共8頁

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每題五分，共二十題

1. Stratified random sampling is a method of selecting a sample in which
 - a. the sample is first divided into strata, and then random samples are taken from each stratum
 - b. various strata are selected from the sample
 - c. the population is first divided into strata, and then random samples are drawn from each stratum
 - d. None of these alternatives is correct.
2. A population consists of 8 items. The number of different simple random samples of size 3 that can be selected from this population is
 - a. 24
 - b. 56
 - c. 512
 - d. 128
3. A random sample of 121 bottles of cologne showed an average content of 4 ounces. It is known that the standard deviation of the contents (i.e., of the population) is 0.22 ounces. In this problem the 0.22 is
 - a. a parameter
 - b. a statistic
 - c. the standard error of the mean
 - d. the average content of colognes in the long run
4. The level of significance is the
 - a. maximum allowable probability of Type II error
 - b. maximum allowable probability of Type I error
 - c. same as the confidence coefficient
 - d. same as the p-value
5. For a one-tailed test (upper tail), a sample size of 18 at 95% confidence, $t =$
 - a. 2.12
 - b. -2.12
 - c. -1.740
 - d. 1.740
6. Whenever the population standard deviation is unknown and the population has a normal or near-normal distribution, which distribution is used in developing an interval estimation?
 - a. standard distribution
 - b. z distribution
 - c. beta distribution
 - d. t distribution

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7. A random sample of 144 observations has a mean of 20, a median of 21, and a mode of 22. The population standard deviation is known to equal 4.8. The 95.44% confidence interval for the population mean is
- 15.2 to 24.8
 - 19.200 to 20.800
 - 19.216 to 20.784
 - 21.2 to 22.8

Exhibit AA

$$n = 36 \quad \bar{x} = 24.6 \quad S = 12 \quad H_0: \mu \leq 20$$
$$H_a: \mu > 20$$

8. Refer to Exhibit AA. The standardized test statistic equals
- 2.3
 - 0.38
 - 2.3
 - 0.38
9. For a one-tailed hypothesis test (upper tail) the p-value is computed to be 0.034. If the test is being conducted at 95% confidence, the null hypothesis
- could be rejected or not rejected depending on the sample size
 - could be rejected or not rejected depending on the value of the mean of the sample
 - is not rejected
 - is rejected
10. To construct an interval estimate for the difference between the means of two populations which are normally distributed and have equal variances, we must use a t distribution with (let n_1 be the size of sample 1 and n_2 the size of sample 2)
- $(n_1 + n_2)$ degrees of freedom
 - $(n_1 + n_2 - 1)$ degrees of freedom
 - $(n_1 + n_2 - 2)$ degrees of freedom
 - $n_1 - n_2 + 2$

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Exhibit BB

The following information was obtained from matched samples.

The daily production rates for a sample of workers before and after a training program are shown below.

Worker	Before	After
1	20	22
2	25	23
3	27	27
4	23	20
5	22	25
6	20	19
7	17	18

11. Refer to Exhibit BB. The null hypothesis to be tested is $H_0: \mu_d = 0$. The test statistic is
- 1.96
 - 1.96
 - 0
 - 1.645
12. In an analysis of variance where the total sample size for the experiment is n_T and the number of populations is K , the mean square within treatments is
- $SSE/(n_T - K)$
 - $SSTR/(n_T - K)$
 - $SSE/(K - 1)$
 - SSE/K

Exhibit CC

$$f(x) = (1/10) e^{-x/10} \quad x \geq 0$$

13. Refer to Exhibit CC. The mean of x is
- 0.10
 - 10
 - 100
 - 1,000
14. Refer to Exhibit CC. The probability that x is between 3 and 6 is
- 0.4512
 - 0.1920
 - 0.2592
 - 0.6065

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15. In a regression model involving more than one independent variable, which of the following tests must be used in order to determine if the relationship between the dependent variable and the set of independent variables is significant?
- t test
 - F test
 - Either a t test or a chi-square test can be used.
 - chi-square test
16. In simple linear regression analysis, which of the following is not true?
- The F test and the t test yield the same results.
 - The F test and the t test may or may not yield the same results.
 - The relationship between X and Y is represented by means of a straight line.
 - The value of $F = t^2$.

Exhibit DD

The table below gives beverage preferences for random samples of girls and boys.

	Girls	Boys	Total
Coffee	50	200	250
Tea	100	150	250
Soft Drink	200	200	400
Other	<u>50</u>	<u>50</u>	<u>100</u>
	400	600	1,000

We are asked to test for independence between age (i.e., boy and girl) and drink preferences.

17. Refer to Exhibit DD. With a .05 level of significance, the critical value for the test is
- 1.645
 - 7.815
 - 14.067
 - 15.507
18. Refer to Exhibit DD. The expected number of boys who prefer coffee is
- 0.25
 - 0.33
 - 150
 - 200

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Exhibit EE

Below you are given a partial computer output based on a sample of 7 observations, relating an independent variable (x) and a dependent variable (y).

Predictor	Coefficient	Standard Error
Constant	24.112	8.376
x	-0.252	0.253

Analysis of Variance

SOURCE	SS
Regression	196.893
Error	94.822

19. Based on Exhibit EE, to test for the significance of the slope, what is the t test statistics?

- a. 3.222
- b. 3.650
- c. 3.986
- d. 4.126

20. Based on Exhibit EE, to perform an F test, what is the F test statistic?

- a. 9.766
- b. 9.932
- c. 10.382
- d. 11.010

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表 標準常態機率分配之面積或機率

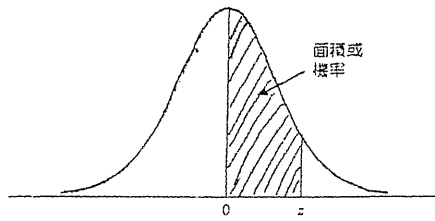


Table with 11 columns (z from 0.0 to 0.9) and 20 rows (z from 0.0 to 3.0). It lists cumulative probabilities for a standard normal distribution.

表 右尾面積的 t 分配表。例如，若自由度為 10，則 $t_{0.025} = 2.228$

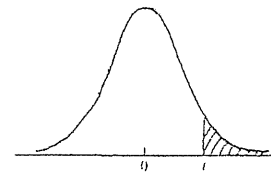
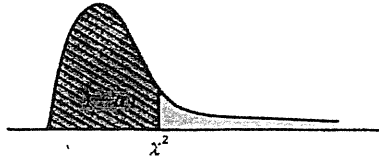


Table with 6 columns (right-tail areas: 0.10, 0.05, 0.025, 0.01, 0.005) and 20 rows (degrees of freedom from 1 to infinity). It lists t-values for various right-tail areas and degrees of freedom.

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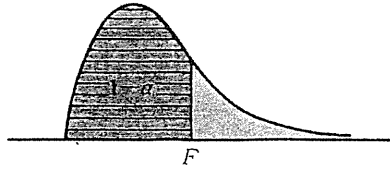
附表 ◆ χ^2 分配



自由度	機 率 $1 - \alpha$							
	.005	.010	.025	.050	.950	.975	.990	.995
1	---	---	---	.004	3.84	5.02	6.63	7.88
2	.01	.02	.05	.10	5.99	7.38	9.21	10.60
3	.07	.11	.22	.35	7.81	9.35	11.34	12.84
4	.21	.30	.48	.71	9.49	11.14	13.28	14.86
5	.41	.55	.83	1.15	11.07	12.83	15.09	16.75
6	.68	.87	1.24	1.64	12.59	14.45	16.81	18.55
7	.99	1.24	1.69	2.17	14.07	16.01	18.48	20.28
8	1.34	1.65	2.18	2.73	15.51	17.53	20.09	21.96
9	1.73	2.09	2.70	3.33	16.92	19.02	21.67	23.59
10	2.16	2.56	3.25	3.94	18.31	20.48	23.21	25.19
11	2.60	3.05	3.82	4.57	19.68	21.92	24.72	26.76
12	3.07	3.57	4.40	5.23	21.03	23.34	26.22	28.30
13	3.57	4.11	5.01	5.89	22.36	24.74	27.69	29.82
14	4.07	4.66	5.63	6.57	23.68	26.12	29.14	31.32
15	4.60	5.23	6.26	7.26	25.00	27.49	30.58	32.80
16	5.14	5.81	6.91	7.96	26.30	28.85	32.00	34.27
17	5.70	6.41	7.56	8.67	27.59	30.19	33.41	35.72
18	6.26	7.01	8.23	9.39	28.87	31.53	34.81	37.16
19	6.84	7.63	8.91	10.12	30.14	32.85	36.19	38.58
20	7.43	8.26	9.59	10.85	31.41	34.17	37.57	40.00
21	8.03	8.90	10.28	11.59	32.67	35.48	38.93	41.40
22	8.64	9.54	10.98	12.34	33.92	36.78	40.29	42.80
23	9.26	10.20	11.69	13.09	35.17	38.08	41.64	44.18
24	9.89	10.86	12.40	13.85	36.42	39.36	42.98	45.56
25	10.52	11.52	13.12	14.61	37.65	40.65	44.31	46.93
26	11.16	12.20	13.84	15.38	38.89	41.92	45.64	48.29
27	11.81	12.88	14.57	16.15	40.11	43.19	46.96	49.64
28	12.46	13.56	15.31	16.93	41.34	44.46	48.28	50.99
29	13.12	14.26	16.05	17.71	42.56	45.72	49.59	52.34
30	13.79	14.95	16.79	18.49	43.77	46.98	50.89	53.67
40	20.71	22.16	24.43	26.51	55.76	59.34	63.69	66.77
50	27.99	29.71	32.36	34.76	67.50	71.42	76.15	79.49
60	35.53	37.48	40.48	43.19	79.08	83.30	88.38	91.95
70	43.28	45.44	48.76	51.74	90.53	95.02	100.43	104.22
80	51.17	53.54	57.15	60.39	101.88	106.63	112.33	116.32
90	59.20	61.75	65.65	69.13	113.14	118.14	124.12	128.30
100	67.33	70.06	74.22	77.93	124.34	129.56	135.81	140.17

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附表 ● F 分配



$1 - \alpha = 0.95$

$\nu_1 \backslash \nu_2$	1	2	3	4	5	6	7	8	9
1	161.45	199.50	215.71	224.58	230.16	233.99	236.77	238.88	240.54
2	18.513	19.000	19.164	19.247	19.296	19.330	19.353	19.371	19.385
3	10.128	9.5521	9.2766	9.1172	9.0135	8.9406	8.8868	8.8452	8.8123
4	7.7086	6.9443	6.5914	6.3883	6.2560	6.1631	6.0942	6.0410	5.9988
5	6.6079	5.7861	5.4095	5.1922	5.0503	4.9503	4.8759	4.8183	4.7725
6	5.9874	5.1433	4.7571	4.5337	4.3874	4.2839	4.2066	4.1468	4.0990
7	5.5914	4.7374	4.3468	4.1203	3.9715	3.8660	3.7870	3.7257	3.6767
8	5.3177	4.4590	4.0662	3.8378	3.6875	3.5806	3.5005	3.4381	3.3881
9	5.1174	4.2565	3.8626	3.6331	3.4817	3.3738	3.2927	3.2296	3.1789
10	4.9646	4.1028	3.7083	3.4780	3.3258	3.2172	3.1355	3.0717	3.0204
11	4.8443	3.9823	3.5874	3.3567	3.2039	3.0946	3.0123	2.9480	2.8962
12	4.7472	3.8853	3.4903	3.2592	3.1059	2.9961	2.9134	2.8486	2.7964
13	4.6672	3.8056	3.4105	3.1791	3.0254	2.9153	2.8321	2.7669	2.7144
14	4.6001	3.7389	3.3439	3.1122	2.9582	2.8477	2.7642	2.6987	2.6458
15	4.5431	3.6823	3.2874	3.0556	2.9013	2.7905	2.7066	2.6408	2.5876
16	4.4940	3.6337	3.2389	3.0069	2.8524	2.7413	2.6572	2.5911	2.5377
17	4.4513	3.5915	3.1968	2.9647	2.8100	2.6987	2.6143	2.5480	2.4943
18	4.4139	3.5546	3.1599	2.9277	2.7729	2.6613	2.5767	2.5102	2.4563
19	4.3808	3.5219	3.1274	2.8951	2.7401	2.6283	2.5435	2.4768	2.4227
20	4.3513	3.4928	3.0984	2.8661	2.7109	2.5990	2.5140	2.4471	2.3928
21	4.3248	3.4668	3.0725	2.8401	2.6848	2.5727	2.4876	2.4205	2.3661
22	4.3009	3.4434	3.0491	2.8167	2.6613	2.5491	2.4638	2.3965	2.3419
23	4.2793	3.4221	3.0280	2.7955	2.6400	2.5277	2.4422	2.3748	2.3201
24	4.2597	3.4028	3.0088	2.7763	2.6207	2.5082	2.4226	2.3551	2.3002
25	4.2417	3.3852	2.9912	2.7587	2.6030	2.4904	2.4047	2.3371	2.2821
26	4.2252	3.3690	2.9751	2.7426	2.5868	2.4741	2.3883	2.3205	2.2655
27	4.2100	3.3541	2.9604	2.7278	2.5719	2.4591	2.3732	2.3053	2.2501
28	4.1960	3.3404	2.9467	2.7141	2.5581	2.4453	2.3593	2.2913	2.2360
29	4.1830	3.3277	2.9340	2.7014	2.5454	2.4324	2.3463	2.2782	2.2229
30	4.1709	3.3158	2.9223	2.6896	2.5336	2.4205	2.3343	2.2662	2.2107
40	4.0848	3.2317	2.8387	2.6060	2.4495	2.3359	2.2490	2.1802	2.1240
60	4.0012	3.1504	2.7581	2.5252	2.3683	2.2540	2.1665	2.0970	2.0401
120	3.9201	3.0718	2.6802	2.4472	2.2900	2.1750	2.0867	2.0164	1.9588
∞	3.8415	2.9957	2.6049	2.3719	2.2141	2.0986	2.0096	1.9384	1.8799