

系 所：工業設計學系

考試科目：統計方法

考試日期：0224，節次：3

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※ 考生請注意：本試題不可使用計算機。請於答案卷(卡)作答，於本試題紙上作答者，不予計分。

1. Calculate the value of the following questions: (15分，每題3分)
  - (a) Find the area under the standard normal curve to the left of  $z = 1.12$
  - (b) Find the area under the standard normal curve over the interval  $z = -0.25$  to  $z = 1.88$
  - (c) Find the critical  $t$  value for one-tailed test with  $df = 8$  at the 0.05 level of significance
  - (d) Find the critical  $t$  value for non-directional test with  $df = 20$  at the 0.01 level of significance
  - (e) Calculate the value of the  $z$  test for  $x = 142$ ;  $\sigma = 35$ ;  $n = 49$ ;  $\mu_{hyp} = 150$
2. During their first swim through a water maze, 12 laboratory rats made the following number of errors (blind alleyway entrance): 5, 12, 5, 3, 24, 7, 5, 12, 5, 6, 8, 12 (15分)
  - (a) Find the mode, median, mean, and standard deviation for these data. (8%)
  - (b) Without constructing a frequency distribution or graph, would you characterize the shape of this distribution as balanced, positively skewed, or negatively skewed? Why? (7%)
3. A new wearable device is designed and its weight with a mean of 525 grams and a standard deviation of 30 grams, which follows a normal distribution. A random sample of 49 wearable devices has a mean weight of 532 grams. Please use the customary procedure to test the null hypothesis at the 0.05 level of significance. (15分)
4. A company wants to know how many days, in average, a salesman sales a new product with the AR design. He randomly picked the sales records of 64 products from the corporate computer center. He found the product deals were averagely made in 18 days. What is the 95% Confidence Interval (C.I.) averaged days for the product being successfully sold? (Assuming the standard deviation of the population mean is 2 days) (15分)
5. Each of the following pairs represents the number of licensed drivers (X) and the number of cars (Y) for five houses in my neighborhood: (20分)
 

DRIVERS (X)	CARS (Y)
5	4
5	3
2	2
3	2
1	1

  - (a) Construct a scatterplot to verify a lack of pronounced curvilinearity. (5%)
  - (b) Determine the least squares regression equation for these data. (10%)  
(Remember, you have to calculate  $r$ ,  $SS_y$ , and  $SS_x$ )
  - (c) Predict the number of cars for a new family with four drivers. (5%)

6. An investigator tests a claim that vitamin C reduces the frequency of common colds. To eliminate the variability due to different family environments, pairs of children from the same family are randomly assigned to either a treatment group that receives vitamin C or a control group that receives fake vitamin C. Each child has a score that reflects the total number of days ill because of colds during the school year. The scores are obtained for ten pairs of children. Please use  $t$  to test the null hypothesis at the 0.05 level of significance. (20分，每題4分)

PAIR NUMBER	DAYS ILL DUE TO COLDS	
	VITAMIN C ( $X_1$ )	FAKE VITAMIN C ( $X_2$ )
1	3	2
2	3	5
3	0	2
4	8	8
5	3	2
6	4	7
7	5	9
8	0	3
9	2	6
10	3	0

Please use the following step-by-step procedure of the hypothesis test: (a) Research Problem; (b) Statistical Hypotheses; (c) Decision Rule; (d) Calculations; (e) Decision and Interpretation.

**Table A<sup>1</sup>**  
**PROPORTIONS (OF AREA) UNDER THE STANDARD NORMAL CURVE FOR VALUES OF Z.**

A	B	C	A	B	C	A	B	C
z			z			z		
0.00	.0000	.5000	0.56	.2123	.2877	1.12	.3686	.1314
0.01	.0040	.4960	0.57	.2157	.2843	1.13	.3708	.1292
0.02	.0080	.4920	0.58	.2190	.2810	1.14	.3729	.1271
0.03	.0120	.4880	0.59	.2224	.2775	1.15	.3749	.1251
0.04	.0160	.4840	0.60	.2257	.2743	1.16	.3770	.1230
0.05	.0199	.4801	0.61	.2291	.2709	1.17	.3790	.1210
0.06	.0239	.4761	0.62	.2324	.2676	1.18	.3810	.1190
0.07	.0279	.4721	0.63	.2357	.2643	1.19	.3830	.1170
0.08	.0319	.4681	0.64	.2389	.2611	1.20	.3849	.1151
0.09	.0359	.4641	0.65	.2422	.2578	1.21	.3869	.1131
0.10	.0398	.4602	0.66	.2454	.2546	1.22	.3888	.1112
0.11	.0438	.4562	0.67	.2486	.2514	1.23	.3907	.1093
0.12	.0478	.4522	0.68	.2517	.2483	1.24	.3925	.1075
0.13	.0517	.4483	0.69	.2549	.2451	1.25	.3944	.1056
0.14	.0557	.4443	0.70	.2580	.2420	1.26	.3962	.1038
0.15	.0596	.4404	0.71	.2611	.2389	1.27	.3980	.1020
0.16	.0636	.4364	0.72	.2642	.2358	1.28	.3997	.1003
0.17	.0675	.4325	0.73	.2673	.2327	1.29	.4015	.0985
0.18	.0714	.4286	0.74	.2704	.2296	1.30	.4032	.0968
0.19	.0753	.4247	0.75	.2734	.2266	1.31	.4049	.0951
0.20	.0793	.4207	0.76	.2764	.2236	1.32	.4066	.0934
0.21	.0832	.4168	0.77	.2794	.2206	1.33	.4082	.0918
0.22	.0871	.4129	0.78	.2823	.2177	1.34	.4099	.0901
0.23	.0910	.4090	0.79	.2852	.2148	1.35	.4115	.0885
0.24	.0948	.4052	0.80	.2881	.2119	1.36	.4131	.0869
0.25	.0987	.4013	0.81	.2910	.2090	1.37	.4147	.0853
0.26	.1026	.3974	0.82	.2939	.2061	1.38	.4162	.0838
0.27	.1064	.3936	0.83	.2967	.2033	1.39	.4177	.0823
0.28	.1103	.3897	0.84	.2995	.2005	1.40	.4192	.0808
0.29	.1141	.3859	0.85	.3023	.1977	1.41	.4207	.0793
0.30	.1179	.3821	0.86	.3051	.1949	1.42	.4222	.0778
0.31	.1217	.3783	0.87	.3078	.1922	1.43	.4236	.0764
0.32	.1255	.3745	0.88	.3106	.1894	1.44	.4251	.0749
0.33	.1293	.3707	0.89	.3133	.1867	1.45	.4265	.0735
0.34	.1331	.3669	0.90	.3159	.1841	1.46	.4279	.0721
0.35	.1368	.3632	0.91	.3186	.1814	1.47	.4292	.0708
0.36	.1406	.3594	0.92	.3212	.1788	1.48	.4306	.0694
0.37	.1443	.3557	0.93	.3238	.1762	1.49	.4319	.0681
0.38	.1480	.3520	0.94	.3264	.1736	1.50	.4332	.0668
0.39	.1517	.3483	0.95	.3289	.1711	1.51	.4345	.0655
0.40	.1554	.3446	0.96	.3315	.1685	1.52	.4357	.0643
0.41	.1591	.3409	0.97	.3340	.1660	1.53	.4370	.0630
0.42	.1628	.3372	0.98	.3365	.1635	1.54	.4382	.0618
0.43	.1664	.3336	0.99	.3389	.1611	1.55	.4394	.0606
0.44	.1700	.3300	1.00	.3413	.1587	1.56	.4406	.0594
0.45	.1736	.3264	1.01	.3438	.1562	1.57	.4419	.0582
0.46	.1772	.3228	1.02	.3461	.1539	1.58	.4429	.0571
0.47	.1808	.3192	1.03	.3485	.1515	1.59	.4441	.0559
0.48	.1844	.3156	1.04	.3508	.1492	1.60	.4452	.0548
0.49	.1879	.3121	1.05	.3531	.1469	1.61	.4463	.0537
0.50	.1915	.3085	1.06	.3554	.1446	1.62	.4474	.0526
0.51	.1950	.3050	1.07	.3577	.1423	1.63	.4484	.0516
0.52	.1985	.3015	1.08	.3599	.1401	1.64	.4495	.0505
0.53	.2019	.2981	1.09	.3621	.1379	1.65	.4505	.0495
0.54	.2054	.2946	1.10	.3643	.1357	1.66	.4515	.0485
0.55	.2088	.2912	1.11	.3665	.1335	1.67	.4525	.0475

-z

A' B' C'

-z

A' B' C'

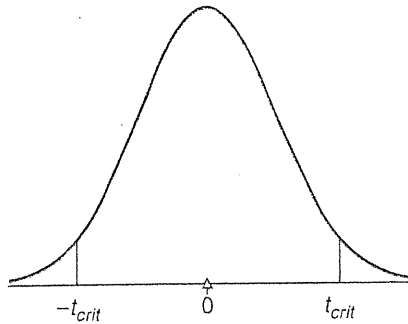
-z

A' B' C'

**Table A' (Continued)**  
**PROPORTIONS (OF AREA) UNDER THE STANDARD NORMAL CURVE FOR VALUES OF z**

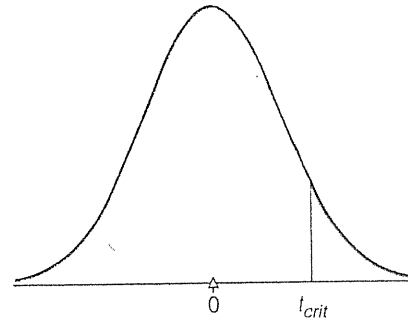
A	B	C		A	B	C		A	B	C
z				z				z		
1.68	.4535	.0465		2.24	.4875	.0125		2.80	.4974	.0026
1.69	.4545	.0455		2.25	.4878	.0122		2.81	.4975	.0025
1.70	.4554	.0446		2.26	.4881	.0119		2.82	.4976	.0024
1.71	.4564	.0436		2.27	.4884	.0116		2.83	.4977	.0023
1.72	.4573	.0427		2.28	.4887	.0113		2.84	.4977	.0023
1.73	.4582	.0418		2.29	.4890	.0110		2.85	.4978	.0022
1.74	.4591	.0409		2.30	.4893	.0107		2.86	.4979	.0021
1.75	.4599	.0401		2.31	.4896	.0104		2.87	.4979	.0021
1.76	.4608	.0392		2.32	.4898	.0102		2.88	.4980	.0020
1.77	.4616	.0384		2.33	.4901	.0099		2.89	.4981	.0019
1.78	.4625	.0375		2.34	.4904	.0096		2.90	.4981	.0019
1.79	.4633	.0367		2.35	.4906	.0094		2.91	.4982	.0018
1.80	.4641	.0359		2.36	.4909	.0091		2.92	.4982	.0018
1.81	.4649	.0351		2.37	.4911	.0089		2.93	.4983	.0017
1.82	.4656	.0344		2.38	.4913	.0087		2.94	.4984	.0016
1.83	.4664	.0336		2.39	.4916	.0084		2.95	.4984	.0016
1.84	.4671	.0329		2.40	.4918	.0082		2.96	.4985	.0015
1.85	.4678	.0322		2.41	.4920	.0080		2.97	.4985	.0015
1.86	.4686	.0314		2.42	.4922	.0078		2.98	.4986	.0014
1.87	.4693	.0307		2.43	.4925	.0075		2.99	.4986	.0014
1.88	.4699	.0301		2.44	.4927	.0073		3.00	.4987	.0013
1.89	.4706	.0294		2.45	.4929	.0071		3.01	.4987	.0013
1.90	.4713	.0287		2.46	.4931	.0069		3.02	.4987	.0013
1.91	.4719	.0281		2.47	.4932	.0068		3.03	.4988	.0012
1.92	.4726	.0274		2.48	.4934	.0066		3.04	.4988	.0012
1.93	.4732	.0268		2.49	.4936	.0064		3.05	.4989	.0011
1.94	.4738	.0262		2.50	.4938	.0062		3.06	.4989	.0011
1.95	.4744	.0256		2.51	.4940	.0060		3.07	.4989	.0011
1.96	.4750	.0250		2.52	.4941	.0059		3.08	.4990	.0010
1.97	.4756	.0244		2.53	.4943	.0057		3.09	.4990	.0010
1.98	.4761	.0239		2.54	.4945	.0055		3.10	.4990	.0010
1.99	.4767	.0233		2.55	.4946	.0054		3.11	.4991	.0009
2.00	.4772	.0228		2.56	.4948	.0052		3.12	.4991	.0009
2.01	.4778	.0222		2.57	.4949	.0051		3.13	.4991	.0009
2.02	.4783	.0217		2.58	.4951	.0049		3.14	.4992	.0008
2.03	.4788	.0212		2.59	.4952	.0048		3.15	.4992	.0008
2.04	.4793	.0207		2.60	.4953	.0047		3.16	.4992	.0008
2.05	.4798	.0202		2.61	.4955	.0045		3.17	.4992	.0008
2.06	.4803	.0197		2.62	.4956	.0044		3.18	.4993	.0007
2.07	.4808	.0192		2.63	.4957	.0043		3.19	.4993	.0007
2.08	.4812	.0188		2.64	.4959	.0041		3.20	.4993	.0007
2.09	.4817	.0183		2.65	.4960	.0040		3.21	.4993	.0007
2.10	.4821	.0179		2.66	.4961	.0039		3.22	.4994	.0006
2.11	.4826	.0174		2.67	.4962	.0038		3.23	.4994	.0006
2.12	.4830	.0170		2.68	.4963	.0037		3.24	.4994	.0006
2.13	.4834	.0166		2.69	.4964	.0036		3.25	.4994	.0006
2.14	.4838	.0162		2.70	.4965	.0035		3.30	.4995	.0005
2.15	.4842	.0158		2.71	.4966	.0034		3.35	.4996	.0004
2.16	.4846	.0154		2.72	.4967	.0033		3.40	.4997	.0003
2.17	.4850	.0150		2.73	.4968	.0032		3.45	.4997	.0003
2.18	.4854	.0146		2.74	.4969	.0031		3.50	.4998	.0002
2.19	.4857	.0143		2.75	.4970	.0030		3.60	.4998	.0002
2.20	.4861	.0139		2.76	.4971	.0029		3.70	.4999	.0001
2.21	.4864	.0136		2.77	.4972	.0028		3.80	.4999	.0001
2.22	.4868	.0132		2.78	.4973	.0027		3.90	.49995	.00005
2.23	.4871	.0129		2.79	.4974	.0026		4.00	.49997	.00003
-z				-z				-z		
A'	B'	C'		A'	B'	C'		A'	B'	C'

**Table B<sup>a</sup>**  
**CRITICAL VALUES OF *t***



Two-tailed or Nondirectional Test  
LEVEL OF SIGNIFICANCE  
(*p*-value in color)

<i>df</i>	<i>p</i> > .05	<i>p</i> < .05	<i>p</i> < .01	<i>p</i> < .001
	.05*	.01**	.001	
1	12.706	63.657	636.62	
2	4.303	9.925	31.598	
3	3.182	5.841	12.924	
4	2.776	4.604	8.610	
5	2.571	4.032	6.869	
6	2.447	3.707	5.959	
7	2.365	3.499	5.408	
8	2.306	3.355	5.041	
9	2.262	3.250	4.781	
10	2.228	3.169	4.587	
11	2.201	3.106	4.437	
12	2.179	3.055	4.318	
13	2.160	3.012	4.221	
14	2.145	2.977	4.140	
15	2.131	2.947	4.073	
16	2.120	2.921	4.015	
17	2.110	2.898	3.965	
18	2.101	2.878	3.922	
19	2.093	2.861	3.883	
20	2.086	2.845	3.850	
21	2.080	2.831	3.819	
22	2.074	2.819	3.792	
23	2.069	2.807	3.767	
24	2.064	2.797	3.745	
25	2.060	2.787	3.725	
26	2.056	2.779	3.707	
27	2.052	2.771	3.690	
28	2.048	2.763	3.674	
29	2.045	2.756	3.659	
30	2.042	2.750	3.646	
40	2.021	2.704	3.551	
60	2.000	2.660	3.460	
120	1.980	2.617	3.373	
∞	1.960	2.576	3.291	



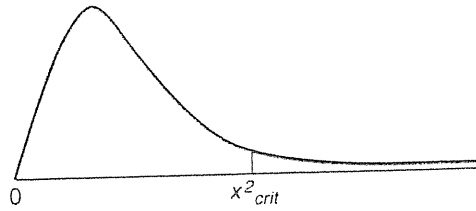
One-tailed or Directional Test  
LEVEL OF SIGNIFICANCE  
(*p*-value in color)

<i>df</i>	<i>p</i> > .05	<i>p</i> < .05	<i>p</i> < .01	<i>p</i> < .001
	.05	.01	.001	
1	6.314	31.821	318.31	
2	2.920	6.965	22.326	
3	2.353	4.541	10.213	
4	2.132	3.747	7.173	
5	2.015	3.365	5.893	
6	1.943	3.143	5.208	
7	1.895	2.998	4.785	
8	1.860	2.896	4.501	
9	1.833	2.821	4.297	
10	1.812	2.764	4.144	
11	1.796	2.718	4.025	
12	1.782	2.681	3.930	
13	1.771	2.650	3.852	
14	1.761	2.624	3.787	
15	1.753	2.602	3.733	
16	1.746	2.583	3.686	
17	1.740	2.567	3.646	
18	1.734	2.552	3.610	
19	1.729	2.539	3.579	
20	1.725	2.528	3.552	
21	1.721	2.518	3.527	
22	1.717	2.508	3.505	
23	1.714	2.500	3.485	
24	1.711	2.492	3.467	
25	1.708	2.485	3.450	
26	1.706	2.479	3.435	
27	1.703	2.473	3.421	
28	1.701	2.467	3.408	
29	1.699	2.462	3.396	
30	1.697	2.457	3.385	
40	1.684	2.423	3.307	
60	1.671	2.390	3.232	
120	1.658	2.358	3.160	
∞	1.645	2.326	3.090	

\*95% level of confidence

\*\*99% level of confidence

**Table D<sup>a</sup>**  
**CRITICAL VALUES OF  $\chi^2$**



LEVEL OF SIGNIFICANCE  
(p-value in color)

	$p > .10$	$p < .10$	$p < .05$	$p < .01$	$p < .001$
<i>df</i>	<b>.10</b>	<b>.05</b>	<b>.01</b>	<b>.001</b>	
1	2.71	3.84	6.64	10.83	
2	4.60	5.99	9.21	13.82	
3	6.25	7.81	11.34	16.27	
4	7.78	9.49	13.28	18.47	
5	9.24	11.07	15.09	20.52	
6	10.64	12.59	16.81	22.46	
7	12.02	14.07	18.48	24.32	
8	13.36	15.51	20.09	26.12	
9	14.68	16.92	21.67	27.88	
10	15.99	18.31	23.21	29.59	
11	17.28	19.68	24.72	31.26	
12	18.55	21.03	26.22	32.91	
13	19.81	22.36	27.69	34.53	
14	21.06	23.68	29.14	36.12	
15	22.31	25.00	30.58	37.70	
16	23.54	26.30	32.00	39.25	
17	24.77	27.59	33.41	40.79	
18	25.99	28.87	34.80	42.31	
19	27.20	30.14	36.19	43.82	
20	28.41	31.41	37.57	45.32	
21	29.62	32.67	38.93	46.80	
22	30.81	33.92	40.29	48.27	
23	32.01	35.17	41.64	49.73	
24	33.20	36.42	42.98	51.18	
25	34.38	37.65	44.31	52.62	
26	35.56	38.88	45.64	54.05	
27	36.74	40.11	46.96	55.48	
28	37.92	41.34	48.28	56.89	
29	39.09	42.56	49.59	58.30	
30	40.26	43.77	50.89	59.70	
40	51.80	55.76	63.69	73.40	
50	63.17	67.50	76.15	86.66	
60	74.40	79.08	88.38	99.61	
70	85.53	90.53	100.42	112.32	