



1. Convert the following 2's complement binary numbers to decimal. (20%)

- (a) 1010
- (b) 0110
- (c) 01011010
- (d) 11111110
- (e) 0011100111010011

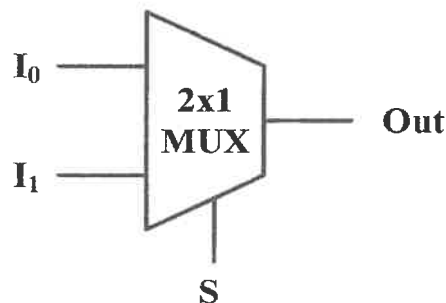
2. Implement the XOR function by means of : (10%)

- (a) NAND gates only.
- (b) NOR gates only.

Please draw the gate-level circuit.

3. Implement a 4-to-1 mux using only 2-to-1 muxes making sure to properly connect all of the terminals. Remember that you will have 4 inputs, 2 control signals, and 1 output. Write out the truth table for this circuit. (10%)

4. A symbol of 2-to-1 mux is listed below. Please draw the gate-level circuit of 2-to-1 mux. (10%)



5. Given an array of 100 elements. Write an algorithm or C program with comments to do bubble sort. Draw a flowchart. How many comparisons and how many swaps the algorithm will take at worst? What is the time complexity of this algorithm? Which sorting algorithm is faster than bubble sort? (13%)

6. Describe a Turing machine. What are the similarities between a Turing machine and a personal computer? What are the differences? (13%)



7. Write an algorithm to find all the prime numbers less than or equal to  $n$ . Use comments to explain your program and draw a flowchart to illustrate the algorithm. Show that your algorithm work for  $n=25$  (12%)
8. Write down the Euclidean algorithm to find the greatest common divisor between two positive integers  $a$  and  $b$ . You cannot use any division or mod function but you can use subtraction. Write down a recursive version of the Euclidean algorithm. This recursive version can use the mod function. Show that both algorithms work with two examples for each algorithm? (12%)