## 國立臺灣大學 107 學年度碩士班招生考試試題

題號:357

科目: 應用力學(B)

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Note: refer to the figures on bottom for the corresponding problems

1. [20 points] Determine (a) the force in members ED, DC, HC, EH, GH, and HI of the truss, and state if the members are in tension or compression; (b) how many zero-force members are existing in this truss.

- 2. [12 points] The rectangular gate shown in section is 3 m long (perpendicular to the paper) and is hinged about its upper edge *B*. The gate divides a channel leading to a fresh-water lake on the left and a saltwater tidal basin on the right. Calculate the torque *M* on the shaft of the gate at *B* required to prevent the gate from opening when the salt-water level drops to 1 m. (The densities of fresh water and salt water are 1.000 g/cm<sup>3</sup> and 1.030 g/cm<sup>3</sup>, respectively.)
- 3. [16 points] A 6.5-m ladder AB leans against a wall as shown. Determine the smallest value of  $\mu_s$  at A for which equilibrium is maintained under the following two conditions: (a) the coefficient of static friction  $\mu_s$  is zero at B; (b) the coefficient of static friction  $\mu_s$  is the same at A and B.
- 4. [20 points] A 2-kg block A is pushed up against a spring compressing it a distance x = 0.1 m. The block is then released from rest and slides down the 20° incline until it strikes a 1-kg sphere B which is suspended from a 1 m inextensible rope. The spring constant k = 800 N/m, the coefficient of friction between A and the ground is 0.2, the distance A slides from the unstretched length of the spring d = 1.5 m and the coefficient of restitution between A and B is 0.8. When  $\alpha = 40^\circ$ , determine (a) the speed of B and (b) the tension in the rope.
- 5. [16 points] The mechanism is presented here and the angular velocity  $\omega_0$  of the disk is constant. Determine (a) the angular velocity  $\omega_{AB}$  and the angular acceleration  $\alpha_{AB}$  of link AB; (b) the velocity  $v_B$  and the acceleration of  $a_B$  of collar B for the instant represented. Assume the quantities  $\omega_0$  and r to be known. (Each answer for 4 pt)
- 6. [16 points] Collar *B* moves to the left with a speed of 5 m/s, which is increasing at a constant rate of 1.5 m/s<sup>2</sup>, relative to the hoop, while the hoop rotates with the angular velocity and angular acceleration shown. Determine the magnitudes of the velocity and acceleration of the collar at this instant.

