

# 國立臺灣師範大學 100 學年度碩士班招生考試試題

科目：自動控制

適用系所：機電科技學系

注意：1.本試題共 2 頁，請依序在答案卷上作答，並標明題號，不必抄題。2.答案必須寫在指定作答區內，否則不予計分。

1. Given the electrical network of Figure 1,

(1) Find the state-space representation if the output is the current through the resistor. (10 分)

(2) Find the input-output transfer function relating the current through the resistor,  $I_R(s)$ , to the input voltage,  $V(s)$ . (10 分)

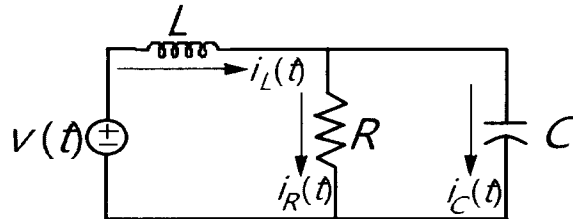


Figure 1.

2. Consider a DC motor speed control system of Figure 2, where  $D(s)=K$ ,  $G(s)=\frac{1}{s+2}$ , and

$H(s)=\frac{2}{s+4}$ , determine an appropriate gain  $K$  so that the whole system steady-state error to a unit step input is minimized. (10 分)

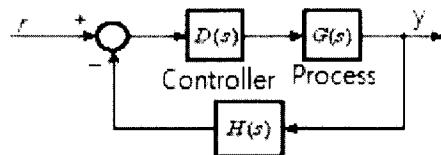


Figure 2.

3. Figure 3 shows a thermal control system in which hot air is circulated to keep the temperature of a

chamber constant. The transfer function of the plant can be adequately represented by  $\frac{\theta(s)}{U(s)} = \frac{1}{s+1}$ .

(1) What are the functions of the controller in this system? (5 分)

(2) Determine the values of  $K_1$  and  $K_2$  which meet the following specification on the feedback system: maximum overshoot  $M_p \leq 20\%$ , setting time  $t_s \leq 2$  sec. (15 分)

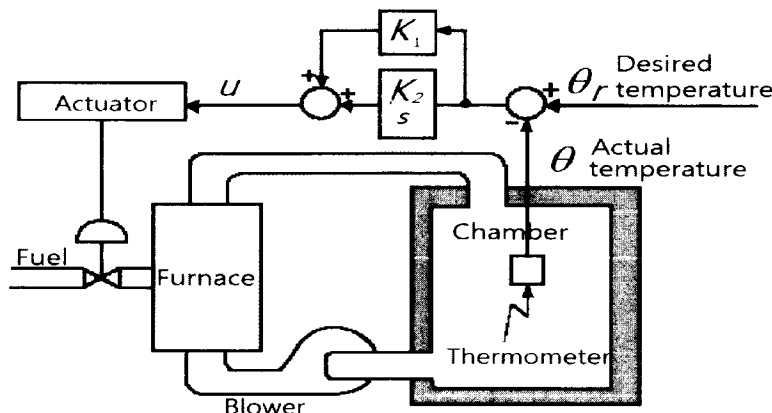


Figure 3.

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4. Suppose system  $Y(s) = \frac{(s+10)}{s^2 + 2s + 5} R(s)$  and  $R(s) = \frac{1}{s}$ . Please determined the peak time ( $t_p$ ), and the maximum overshoot ( $M_p$ ), where  $\dot{y}(t = t_p) = 0$  and  $M_p = y(t_p) - 1$ . (10 分)

5. A single-loop feedback controlled system has a characteristic equation,  $1 + G(s)H(s) = 0$  with  $G(s)H(s) = \frac{K}{s(s+1)(s+5)}$ ;  $K \geq 0$ .

- (1) Please sketch the root locus of this system. (15 分)
- (2) What is the change of the root locus when add a zero ( $s+3$ ) in the original system? (3 分)
- (3) What is the change of the root locus when add a zero ( $s+10$ ) in the original system? (3 分)

6. Figure 4 shows the system frequency response data on Bode plots.

- (1) Find: (a) gain crossover frequency  $\omega_g$ , (b) gain margin  $G.M.$ , (c) phase crossover frequency  $\omega_\phi$ , and (d) phase margin  $P.M.$  (12 分)
- (2) Assume that the system has minimum phase transfer function, estimate the transfer function. (7 分)

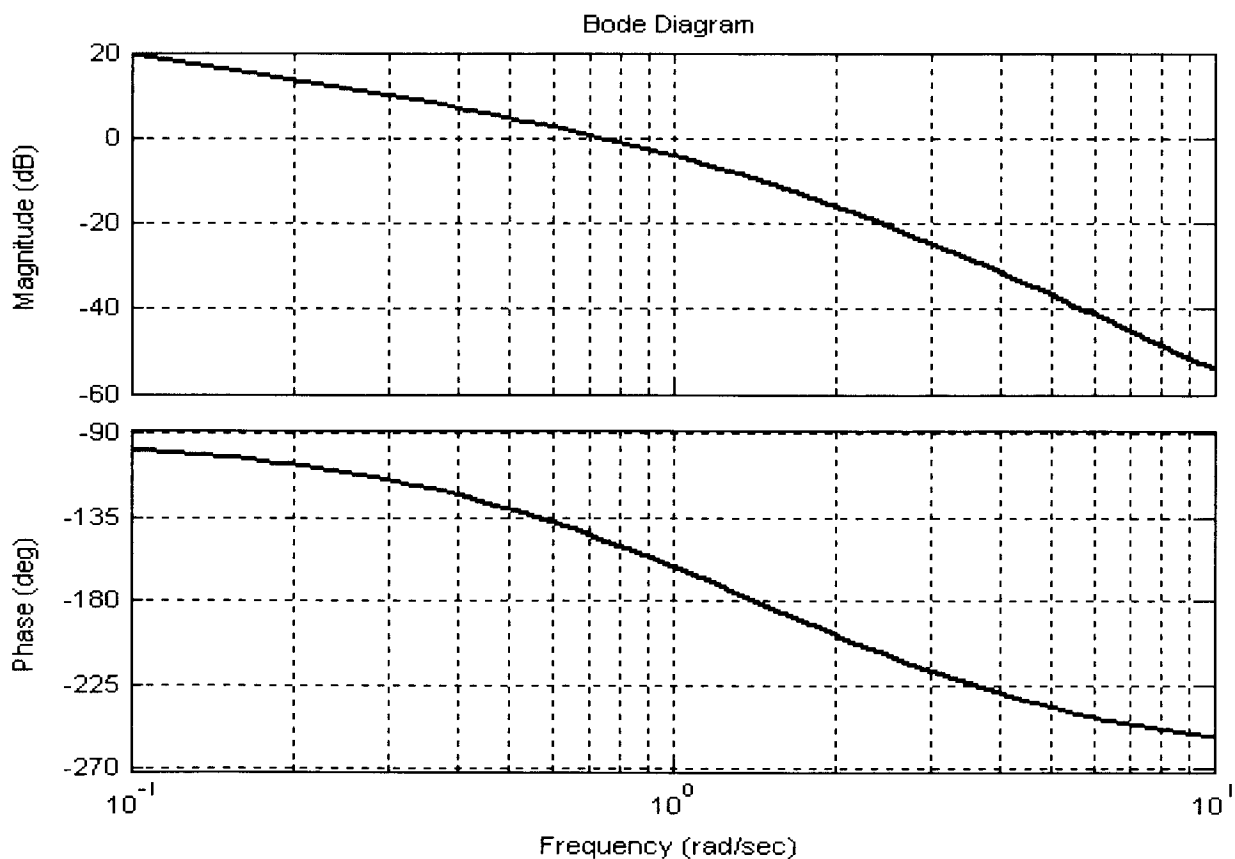


Figure 4