

## 科目：工程數學一(線性代數)

適用：電機系

編號：353

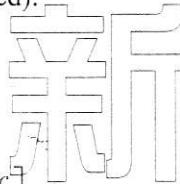
考生注意：

1. 依次序作答，只要標明題號，不必抄題。
2. 答案必須寫在答案卷上，否則不予計分。
3. 限用藍、黑色筆作答；試題須隨卷繳回。

本試題
共 / 頁
第 / 頁

1.  $A = \begin{bmatrix} 2 & 1 \\ -3 & 4 \\ 1 & 6 \end{bmatrix}, B = \begin{bmatrix} 0 & -1 & 0 \\ 4 & 0 & 2 \\ 8 & -1 & 7 \end{bmatrix}$

- Find (a)  $AB$  (if they are defined). (10 points)  
 (b)  $BA$  (if they are defined). (10 points)



2. Find  $(A^{-1})^T$  and  $(A^T)^{-1}$  for

$$A = \begin{bmatrix} 1 & 0 \\ 9 & 3 \end{bmatrix} \text{ and also } A = \begin{bmatrix} 1 & c \\ c & 0 \end{bmatrix}.$$

(20 points)

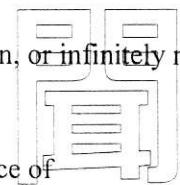
3. For which values of  $k$  does

(20 points)

$$kx + y = 1$$

$$x + ky = 1$$

have no solution, one solution, or infinitely many solutions?

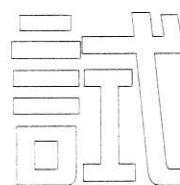


4. Find the rank and the nullspace of

(20 points)

$$B = \begin{bmatrix} 0 & 0 & 1 & 2 \\ 0 & 0 & 1 & 2 \\ 1 & 1 & 1 & 0 \end{bmatrix}$$

5. If  $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$



Find (a)  $A^0$

(10 point)

(b)  $A^n$

(10 point)

