國立中山大學 107 學年度碩士暨碩士專班招生考試試題

科目名稱:微積分【應數系碩士班乙組】

題號: 424002

※本科目依簡章規定「不可以」使用計算機(問答申論題)

共1頁第1頁

計算題:共7題,子題分數平均分配。答題時,每題都必須寫下題號與詳細步驟。

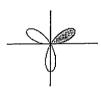
[1]. (10%) Let
$$F(x) = 2^x + \frac{1}{\sqrt{x^2 + 1}} + \int_0^x \cos(\pi s^2) ds$$
. Find $F'(x)$ and $F''(x)$.

- [2]. (16%)
 - (a) Find the Taylor series of $f(x) = \sin(x)$ at $x = \frac{\pi}{2}$.
 - (b) Evaluate $\lim_{x\to 0} \frac{x^3 \sin x^3}{x^9}$
- [3]. (20%) Evaluate the following integrals.

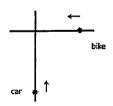
(a)
$$\int_0^{\pi} e^x \cos x dx$$

(a)
$$\int_0^{\pi} e^x \cos x dx$$
 (b) $\int_{-\infty}^{\infty} \frac{1}{x^2 + 2x + 5} dx$

- [4]. (14%) Find the interval of convergence for the power series $\sum_{i=1}^{\infty} \frac{3^{n}}{n} (5x-1)^{n}$.
- [5]. (12%) Find the area of one leaf of the three-leaf rose $r = \sin 3\theta$.



- [6]. (14%) Evaluate the iterated integral $\int_{0}^{\frac{\sqrt{\pi}}{2}} \int_{0}^{\frac{\sqrt{\pi}}{2}} \sin(x^2) dx dy$.
- [7]. (14%) A bike is traveling west at 20 km/h and a car is traveling north at 80 km/h. Both are headed for the intersection of the two roads. At what rate are the bike and the car approaching each other when bike is 30 m and car is 40 m from the intersection?



======= 全卷完 =======