

1. What is the characteristics of SHORT-CIRCUIT EVALUATION? Give each of || and && an example (in C, C++, or JAVA) to demonstrate its merits. Be sure to explain your answer in details. (10%)
2. Write down the following requirement in C programming language. (15%)

Model\Year	2016	2015	2014	2013
TOYOTA	15	6	20	26
BMW	18	10	25	39
LEXUS	50	9	32	31

Use *int car[][]* to store the above annual car sale data from year 2013-2016 for a car sale company. Write a program in C programming language using **LOOP** to output the following information.

- (a) The total number of car sold for TOYOTA, the total number of car sold for BMW, and the total number of car sold for LEXUS from 2013 to 2016.
 - (b) Output the annual number of car sale for each year.
 - (c) Output the highest number of car sale info within 2013 to 2016 (year, brand, sale number).
3. Write down the following functions in C programming language.
 - (a) Implement the function *double Min(double[], int num)* which returns the minimum value of a given double array. (5%)
 - (b) Read the integer variable *a* and *b* from keyboard.
Implement the function *void swap (int* ptr_a, int* ptr_b)* to swap the contents of *a* and *b*. Print out the values of *a*, *b* before and after calling the *swap()*. (5%)
 4. (a) Write a recursive function *int rsum(int n)* and a non-recursive function *int non_rsum(int n)* by using **LOOP** in C programming language to compute the sum of the following equation, (10%)

$$1 \times 2 + 2 \times 3 + 3 \times 4 + \dots + (n-1) \times n.$$

- (b) Discuss the pros and cons of using recursion. When to use and not to use recursion in designing code? Concisely describe your explanation. (5%)

5. Give the Big- θ (Big-Theta) for each following running time estimates (where n is the size of the input problem). (5%)

- (a) $2^{1000} + 1000^2$
- (b) $1 + 2 + 3 + \dots + (n - 1) + n$
- (c) $10n + 100 \log n + n \log n^2$
- (d) $2^0 + 2^1 + \dots + 2^{n-1}$
- (e) $n \log n! + n^2$

6. (a) Design an efficient algorithm which takes as input an array which may contain duplicates. It returns true if all elements of the array occur an even number of times; otherwise it returns false. For example, on the array $\{2, 6, 2, 6, 7, 2, 2, 7\}$ it returns true, but on the array $\{1, 6, 2, 1, 2, 2, 6\}$ it returns false because 2 occurs an odd number of times. (10%)

- (b) Please show the time complexity of your designed algorithm. (5%)
- (c) Please demonstrate your designed algorithm on the array $\{2, 6, 2, 6, 7, 2, 2, 7\}$. (5%)

7. (a) Which array out of A , B , C , and D represents a binary heap (*min* heap)? Only one answer is correct. (5%)

	0	1	2	3	4	5	6	7	8	9	10	11
A=	1	3	5	2	4	6	7	9	11	8	10	
	0	1	2	3	4	5	6	7	8	9	10	11
B=	1	3	5	6	10	7	9	17	77	4	25	
	0	1	2	3	4	5	6	7	8	9	10	11
C=	1	3	9	4	5	77	10	7	6	25	17	
	0	1	2	3	4	5	6	7	8	9	10	11
D=	1	2	4	9	7	17	10	25	6	3	77	

- (b) Write the heap out as a binary tree. (5%)
- (c) Add 8 to the heap. How does the array look now for the new heap? (5%)

8. Consider an initially empty hash table of size M and a hash function $h(x)=x \bmod M$.

- (a) In the worst case, what is the time complexity in Big-Oh notation to insert n keys into the table if separate chaining is used to resolve collisions? Suppose that each entry (bucket) of the table stores an unordered linked list. When adding a new element to an unordered linked list, such an element is inserted at the beginning of the list. (3%)
- (b) What is the answer (time complexity in Big-Oh notation) for (a) if the linked lists are ordered? (3%)
- (c) Suppose that instead of a linked list, each bucket of the table is implemented as an AVL tree. Then, what is the answer (time complexity in Big-Oh notation) for (a)? (4%)