

國立中山大學100學年度碩士班招生考試試題

科目：工程數學【材光系碩士班乙組】

1. Find the general solution of $2y \frac{d^3 y}{dx^3} + 2(y + 3 \frac{dy}{dx}) \frac{d^2 y}{dx^2} + 2(\frac{dy}{dx})^2 = \sin x$ (15%)

2. Use Frobenius method to find the general solution of $x^2 y'' + 6xy' + (6 - 4x^2)y = 0$. (20%)

3. Find the eigenvalues, eigenfunctions and verify the orthogonality of the solution by direct calculation. $y'' + \lambda y = 0$, $y(\pi) = y(-\pi)$, $y'(\pi) = y'(-\pi)$. (15%)

4. A surface is defined by $z = x^2 + y^2$, calculate the surface area defined on the domain $0 \leq x^2 + y^2 \leq 4$ (15%)

5. $f(x) = x$, $-\pi \leq x \leq \pi$, $f(x) = f(x + 2\pi)$, solve
 (1) Fourier series, (20%, each 10%)
 (2) complex Fourier series

6. Solve nonhomogeneous boundary condition of heat equation

$$\frac{\partial u(x,t)}{\partial t} = c^2 \frac{\partial^2 u(x,t)}{\partial x^2} \quad (15\%)$$

$$u(0,t) = A_1, u(L,t) = A_2, u(x,0) = f(x), \text{ where } 0 < x < L, t > 0$$