

## 國立中山大學100學年度碩士班招生考試試題

科目：控制系統【電機系碩士班乙組】

**Problem 1 (20%)** A circuit made of a non-inverting amplifier and a device  $G$  is displayed in Fig. 1, and the device  $G$  has the Nyquist plot in Fig. 2. Assume the op-amp is ideal. Determine  $R$  to make the circuit stable with the gain margin of 20 dB.

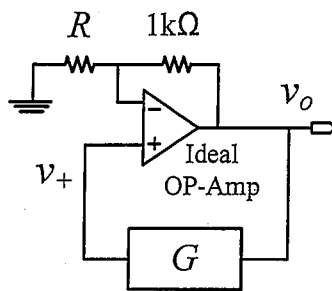


Fig. 1

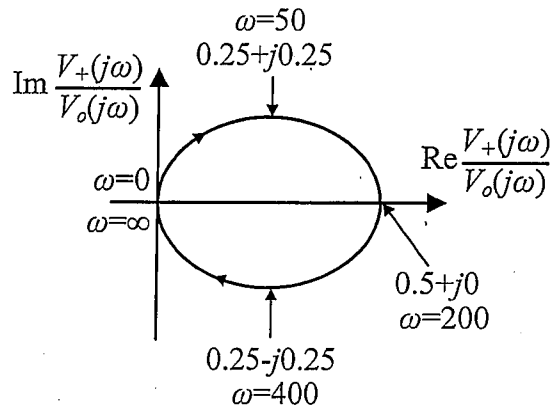


Fig. 2

**Problem 2 (45%)** Figure 3 shows a circuit to control the angular position  $\theta$  of the motor. The position  $\theta$  is measured and converted to the voltage of equal magnitude, and fed back through the circuit. Assume that the op-amp is ideal, and that the frequency response  $P(j\omega)$  of the motor from the current  $i$  to the position  $\theta$  is plotted in Fig. 4.

- (15%) Roughly estimate the parameters  $k$ ,  $a$  and  $b$  of the motor's transfer function  $P(s) = k/[(s+a)(s+b)]$ , according to the Bode plot in Fig. 4.
- (15%) Determine  $R$  so that the control system is stable with the phase margin of about 50 degree.
- (15%) Determine the steady-state value of  $\theta$ , given  $R = 1\Omega$ .

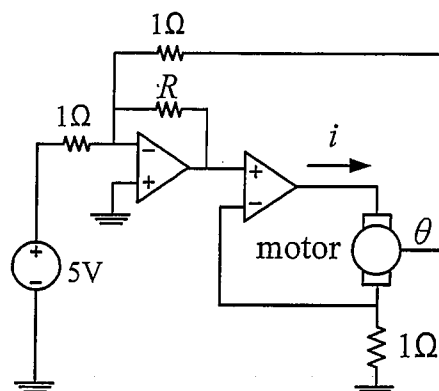


Fig. 3.

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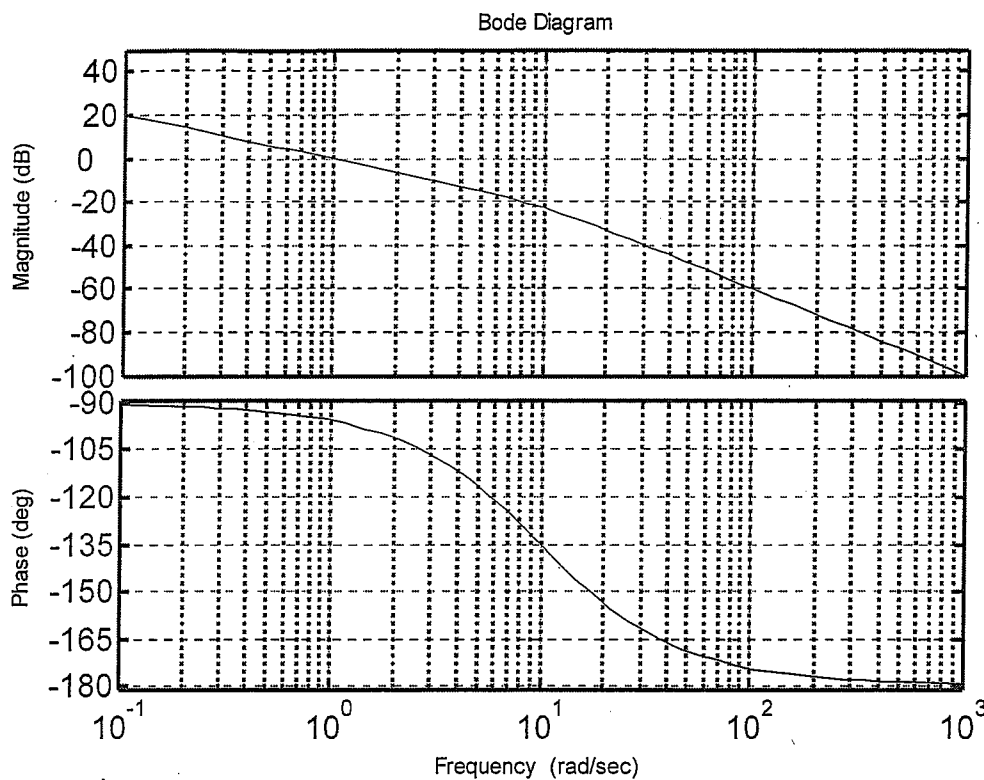


Fig. 4.

**Problem 3 (25%)** Find if the following controllers would stabilize the plant  $P$  in Fig. 5. Note: All answers need justifications or no scores will be given.

- (a) (5%)  $C(s) = \frac{-s+2}{s+2}$ , (b) (5%)  $C(s) = \frac{s+2}{s}$ , (c) (5%)  $C(s) = \frac{4s+2}{s-2}$ ,  
 (d) (5%)  $C(s) = \frac{-0.5s+2}{s}$ , (e) (5%)  $C(s) = 5$ .

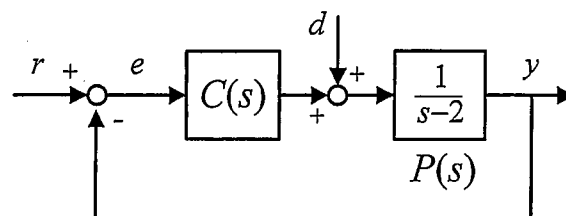


Fig. 5

**Problem 4 (10%)** A function  $y$  is expressed in terms of the following linear convolution. Is it bounded for  $t > 0$ ? Justify your answer.

$$y(t) = \int_0^t \sin(\tau) \cos(t-\tau) d\tau.$$