

考試科目	近代物理	所別	應用物理研究所 (8162, 8163)	考試時間	2月25日(六)第四節
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說明：

Fill in each underlined blank in the statements of all the problems, referring to the key words or key constants listed below, and answer the questions.

Bohr, Galilean; Hartree; Weinberg; Einstein; Maxwell; Feymann; Thomas; Newton; Lorentz; Larmor; Stern-Gerlach; de Broglie; Compton; Schroedinger; g-factor; Stefan-Boltzmann factor; Planck constant; Sommerfeld; de Broglie; Rayleigh-Jeans; Rydberg; Raman; Zeeman; Rutherford; Thomson; orbital; spin; inertial; black-body; magneton;

$6.67 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2$ ;  $6.626 \times 10^{-34} \text{ J}\cdot\text{s}$ ;  $1.381 \times 10^{-23} \text{ J/K}$ ;  $8.617 \times 10^{-5} \text{ eV/K}$ ;  
 $4.136 \times 10^{-15} \text{ eV}\cdot\text{s}$ ;  $1.602 \times 10^{-19} \text{ C}$ ;  $9.109 \times 10^{-31} \text{ Kg}$ ;  $8.854 \times 10^{-12} \text{ F}\cdot\text{m}$ ;  
 $1.257 \times 10^{-6} \text{ H/m}$ ;  $5.292 \times 10^{-11} \text{ m}$ ;  $1.097373 \times 10^7 \text{ m}^{-1}$

Example:

Write down the equation for the law of gravitation which is discovered by the 23-year-old \_\_\_\_\_ in 1665.

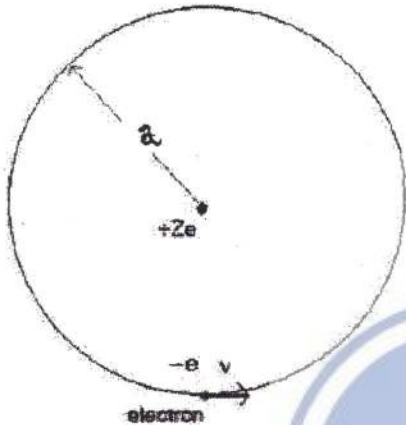
Answer:  $F = G \frac{m_1 m_2}{r^2}$  ; Issac Newton

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(1) (26%)

(a) In \_\_\_\_\_'s model, the orbital angular momentum  $L$  of an electron in an atom is postulated to be quantized. (2%)

$$L = nh \quad (n=1,2,\dots)$$



(b) The energy levels are then

$$E_n = -R_\infty \frac{Z^2 hc}{n^2}$$

Find the expression and the value of the \_\_\_\_\_ constant  $R_\infty$ . (8%)

(c) In quantum mechanics, the energy levels are obtained by finding the eigenvalues of the \_\_\_\_\_ equation. (2%) Write down the time-independent equation for one-electron atom. (6%)

(d) A model of one-dimension one-electron atom in the effective potential

$$V(z) = \begin{cases} -\frac{A e^2}{4z} & \text{if } z > 0 \\ \infty & \text{if } z < 0 \end{cases}$$

can be used to find the energy levels of an electron trapped by the induced electric field on the surface of liquid helium. The energy levels are  $E_n = -\frac{R^*}{n^2}$  ( $n=1,2,\dots$ )

Find  $R^* = ?$ . (8%)

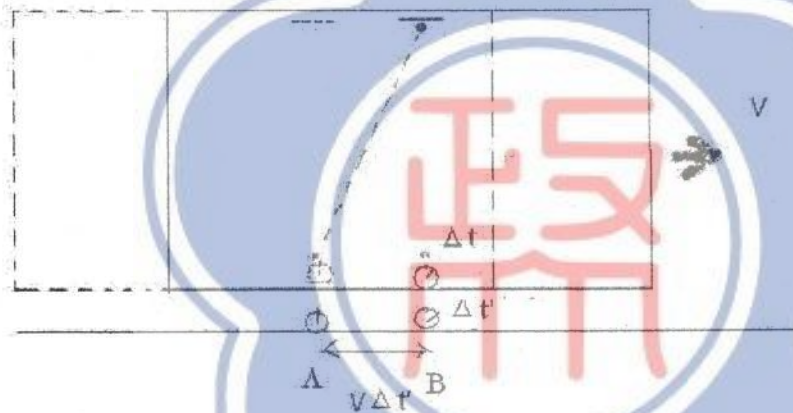
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(2) (20%)

(a) Basic postulates of special theory of relativity: the speed of light as well as the physical laws are the same in all \_\_\_\_\_ reference frames. (2%)

A train is moving forward with speed  $v$  in the  $+x$  direction relative to the observer on the ground. A light signal is sent from a source on the floor of the train, in the  $+z$  direction, and reaches the ceiling of the train after time  $\Delta t$ . For the observer on the ground, the signal takes time  $\Delta t'$  from the source to the ceiling. The speed of light is  $c$  in both the frame  $S$  on the train and the frame  $S'$  on the ground.

(b) Find the relation between  $\Delta t$  and  $\Delta t'$ ? (4%)



(c) During time  $\Delta t'$ , the light source on the train has moved a distance  $L'$  from label A to label B marked on the ground. For an observer on the train, the distance between A and B is  $L$ . Find the relation between  $L$  and  $L'$ . (4%)

(d) The coordinates  $(x,y,z,t)$  in  $S$  are related to the coordinates  $(x',y',z',t')$  in  $S'$  by the \_\_\_\_\_ transformation. (2%)

Write down the transformation equations for the case when an event at  $t=0$  and  $x=0,y=0,z=0$  in  $S$  is observed to occur at  $t'=0, x'=0, y'=0, z'=0$  in  $S'$ . (4%)

(e) What are the equations for the transformation between the velocities for a particle moving at velocity  $(u_x, u_y, u_z)$  observed in  $S$  and at  $(u'_x, u'_y, u'_z)$  observed in  $S'$ ? (4%)

備註	試題隨卷繳交
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(3)(28%)

(a) An electron moving circularly around the nucleus. The relation between the magnetic dipole moment  $\vec{\mu}_l$  produced by the motion and its angular momentum  $\vec{L}$  is

$$\vec{\mu}_l = - \frac{g_l \mu_b}{\hbar} \vec{L}, \text{ where } \mu_b = \frac{e\hbar}{2m} \text{ is called the } \underline{\hspace{2cm}},$$

and its the value is  $\underline{\hspace{1cm}}$  where the  $\underline{\hspace{1cm}}$  g-factor,  $g_l = \underline{\hspace{1cm}}$ . (8%)

(b) The motion of the electron in presence of the magnetic field produced by the nucleus, is in analogy to a spinning top. The phenomena is called  $\underline{\hspace{2cm}}$  precession. The relativistic effect, on the other hand, causes the  $\underline{\hspace{2cm}}$  precession, that the magnetic dipole arisen from the internal degree of freedom is expressed as

$$\vec{\mu}_s = - \frac{g_s \mu_b}{\hbar} \vec{S}, \text{ where } \vec{S} \text{ is } \underline{\hspace{2cm}} \text{ and } g_s = \underline{\hspace{1cm}}. \text{ (10\%)}$$

(c) The energy levels of an atom in a uniform magnetic field  $\vec{B}$  split according to the angular momentum quantum numbers. This is called  $\underline{\hspace{2cm}}$  effect. (2%)

The energy splitting is  $\Delta E = g \mu_b B m_z$ . Express  $g$  in terms of the quantum numbers of the total angular momentum,  $j$ , its component in the direction of  $\vec{B}$ ,  $m_z$ , the total orbital angular momentum,  $l$ , and the total spin angular momentum,  $s$ . (6%)

(d) The beams of atoms in a non-uniform magnetic field are separated according to their angular momentum states in the  $\underline{\hspace{2cm}}$  experiments. (2%)

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(4) (16%)

(a) In proposing the idea that electromagnetic waves are quantized as photons, the physicists \_\_\_\_\_ postulated that the photon energy  $E$  of frequency  $\nu$  is \_\_\_\_\_, \_\_\_\_\_ proposed that the momentum  $p$  and wave vector  $k$  are related by \_\_\_\_\_. \_\_\_\_\_ used the same relations to propose the idea of material waves.

(10%)

(b) A beam of neutrons that emerges from a nuclear reactor contains neutrons with a variety of energies. To obtain neutrons with an energy of 0.06 eV, the beam is passed through a crystal whose atomic planes are 20 Å apart. At what angle relative to the original beam will the desired neutrons be diffracted? (6%)

(5) (10%)

Find the transmission and reflection coefficients for the quantum waves in a one-dimensional step potential.

