## 國立臺北大學 104 學年度碩士班一般入學考試試題

系(所)組別:通訊工程學系

科 目:機率

第1頁 共1頁

□可 ☑不可使用計算機

- 1. Let X be the number of heads in two tosses of a fair coin.
  - (a) Find the expected value E[X]. (10%)
  - (b) Find the variance VAR[X]. (10%)
- 2. Let X be the number of heads in N tosses of a fair coin. Find the probability mass function pmf. (10%)
- 3. If you draw 5 cards from a set of 52 playing cards, what is the probability that you get 4 "Kings"? (Just write down the equations. Do not need to calculate a final number.) (10%)
- 4. A fair coin is tossed 10 times. If the first 9 tosses are "heads", is it more likely to get a "tail" in the 10th toss? (Answer yes or no.) (5%)
- 5. Let S= {1, 2, 3, 4} and A= {1, 2}, B= {1, 4}. Assume the outcomes are equally probable. Are A and B independent events? Why? (5%)
- 6. X is a continuous uniform random variable with expected value E[X] = 7 and variance Var[X] = 3. What is  $f_X(x)$ , the probability density function of X? (10%)
- 7. Let X denote the duration in minutes of a telephone conversation. Assume that the density for X is given by

$$f_X(x) = (1/10)e^{-x/10}, \quad x > 0.$$

If you are waiting outside a telephone booth in the wind and rain, how long should you expect to wait, assuming you arrived one minute after the call started? (10%)

- 8. Let X and Y be independent exponential random variables with common parameter  $\lambda$ . Define Z = X + Y. Find the probability density function  $f_Z(z)$ . (10%)
- 9. X and Y are random variables with E[X] = E[Y] = 0 and Var[X] = 1, Var[Y] = 4 and correlation coefficient  $\rho_{X,Y} = 1/2$ . Find Var[X+Y]. (10%)
- 10. Suppose that X and Y are jointly continuous random variables with

$$f_{X,Y}(x,y) = \begin{cases} y-x, & 0 < x < 1, 1 < y < 2, \\ 0, & \text{otherwise.} \end{cases}$$

Find the covariance Cov[X, Y]. (10%)