

1. Find $2\dot{y}(t) + 4y(t) = x(t)$, $y(0) = 3$, $x(t) = 5$, $t \geq 0$ (25%)

2. Find the Inverse Matrix of A (25%)

$$A = \begin{bmatrix} 4 & 6 & 5 \\ 2 & 3 & 2 \\ 1 & -5 & -2 \end{bmatrix}$$

3. Try to show the process of diagonalizing the (25%)

matrix $A = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix}$

4. Try to find out the differential equation with the general solution of $y = C_1 \sin x + C_2 \cos x$ (25%)