

國立中山大學 104 學年度碩士暨碩士專班招生考試試題

科目名稱：微積分【海工系碩士班丙組選考】

題號：459007

※本科目依簡章規定「可以」使用計算機（廠牌、功能不拘）（問答申論題） 共 1 頁第 1 頁

1. (20%) 【Limits】

(a) (5%) $\lim_{x \rightarrow 0} \frac{|x|}{x}$; (b) (5%) $\lim_{x \rightarrow 1} \frac{1 - \sqrt{x}}{1 - x}$
(c) (5%) $\lim_{x \rightarrow 8} \frac{x - 8}{\sqrt[3]{x} - 2}$; (d) (5%) $\lim_{x \rightarrow 0} \sin\left(\frac{1}{x}\right), x > 0$

2. (30%) 【Differentiation】

(a) (10%) Given $2x^3 - 2y^2 = 5$, find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$.
(b) (10%) Given $y = 3u + 1$, $u = x^{-2}$, $x = 1 - s$, find $\frac{dy}{ds}$.
(c) (10%) Find the slope of the curve $x^3 - 3xy^2 + y^3 = 1$ at $(2, -1)$.

3. (30%) 【Integration】

(a) (10%) $\int x^2 e^{3x} dx$; (b) (10%) $\int x \cos x^2 dx$
(c) (10%) $\int_0^1 \frac{x^2 - 4x + 3}{(x - 2)^2} dx$

4. (10%) 【Application】

Find the arc length (弧長) of the curve $y = \frac{x^3}{6} + \frac{1}{2x}$ from $x = 1$ to $x = 2$.

5. (10%) 【Application】

Find the area bounded by the graphs of $x^2 + y^2 = 4$ and $r = 4 \cos \theta$.