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國立臺灣大學104學年度碩士班招生考試試題

科目:電磁學及電磁波

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※ 注意:請用 2B 鉛筆作答於答案卡,並先詳閱答案卡上之「畫記說明」。 以下均為單選題

- 1. (4%) Find the total charge contained in a cylindrical volume defined by  $r \le 2$  m and  $0 \le z \le 3$  m if  $\rho_v = 20rz$  (mC/m<sup>3</sup>).
  - (A) 0.5 C
  - (B) 1 C
  - (C) 1.5 C
  - (D) 2 C
- 2. (4%) If  $\overline{J} = \hat{y}4xz(A/m^2)$ , find the current I flowing through a square with corners at
  - (0, 0, 0), (2, 0, 0), (2, 0, 2), and (0, 0, 2)
  - (A) 10 A
  - (B) 12 A
  - (C) 14 A
  - (D) 16 A
- 3. (4%) Given the electric flux density  $\overline{D} = \hat{x}2(x+y) + \hat{y}(3x-2y)$  (C/m²), determine the total charge Q enclosed in a cube 2 m on a side.
  - (A) 0 C
  - (B) 1 C
  - (C) 2 C
  - (D) 3 C
- 4. (4%) Current I flows along the positive z-direction in the inner conductor of a long coaxial cable and returns through the outer conductor. The inner conductor has radius a, and the inner and outer radii of the outer conductor are b and c, respectively. Determine the magnetic field in  $r \ge c$  region.
  - (A)  $\frac{rI}{2\pi a^2}$
  - (B)  $\frac{I}{2\pi r}$
  - (C) 0
  - (D)  $\frac{\sqrt{b^2+c^2}}{2\pi r^2}$
- 5. (4%) Given that a current sheet with surface current density  $\overline{J_s} = \hat{x}8$  (A/m) exists at y
  - = 0, the interface between two magnetic media, and  $\overline{H_1} = \hat{z}11$  (A/m) in medium 1 ( $\nu > 0$ ),

determine  $\overline{H_2}$  in medium 2 (y < 0).

- (A)  $\hat{z}1$
- (B)  $\hat{z}3$
- (C)  $\hat{x}1$
- (D)  $\hat{x}3$

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6. (4%) A wire carrying a current of 4 A is formed into a circular loop. If the magnetic field at the center of the loop is 20 A/m, what is the radius of the loop if the loop has 10 turns.

- (A) 1m
- (B) 2 m
- (C) 3 m
- (D) 4 m

7. (4%) For a uniform plane wave of frequency  $10^6$  Hz propagating in a nonmagnetic material medium, the propagation constant is known to be (0.05+j0.1) (1/m). Find the distance in which the fields are attenuated by  $e^{-1}$ .

- (A) 5 m
- (B) 10 m
- (C) 15 m
- (D) 20 m

8. (4%) The region z<0 and z>0 are nonmagnetic perfect dielectrics of permittivities ,  $\varepsilon_1$  and  $\varepsilon_2$  , respectively. For a uniform plane wave incident from the region z<0 normally onto the boundary z=0, find  $\frac{\varepsilon_1}{\varepsilon_2}$  for the electric field of the reflected wave is -1/3 times the electric field of the incident wave.

- (A) 2
- (B) 4
- (C) 6
- (D) 8

9. (4%) In a region of static electric field  $\overline{E} = yz\hat{x} + zx\hat{y} + xy\hat{z}$ , find the potential difference V<sub>A</sub>-V<sub>B</sub> for A(2,2,2) and B(1,1,1).

- (A) 0 V
- (B) 5 V
- (C) -7 V
- (D) -1 V

10. (4%) The magnetic field in a given dielectric medium is given by

 $\overline{H} = \hat{y}6\cos(2z)\sin(2\times10^7t - 0.1x)$  (A/m), where x and z are in meters. Determine

the phase velocity of the electromagnetic wave.

- (A)  $2 \times 10^8$  (m/s)
- (B)  $3 \times 10^8$  (m/s)
- (C)  $5 \times 10^8$  (m/s)
- (D)  $1.5 \times 10^8$  (m/s)

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11. (5%) The magnetic field associated with a uniform plane wave propagating in the

+z-direction in free space is given by  $\overline{H} = H_0 \cos(6\pi \times 10^7 t - 0.2\pi z) \hat{y}$  (A/m). Find

the instantaneous power flow across a surface of area  $1\text{m}^2$  in the z=0 plane at  $t=(1/8) \mu s$ .

- (A) 0 W
- (B) 1 W
- (C) 1.5 W
- (D) 3 W
- 12. (5%) The electric field of a plane wave is given by

$$\overline{E}(z,t) = \hat{x} 3 \cos(\omega t - kz) + \hat{y} 4 \cos(\omega t - kz) (V/m)$$
. Determine the

polarization state of the corresponding electromagnetic wave.

- (A) Linear Polarization
- (B) Right-Hand Circular Polarization
- (C) Left-Hand Circular Polarization
- (D) Elliptical Polarization
- 13. (4%) The general expression of the voltage on a lossless transmission line in the sinusoidal steady state is

$$V\left(z,t\right) = A\cos\left[\omega\left(t-\frac{z}{v_p}\right) + \theta\right] + B\cos\left[\omega\left(t+\frac{z}{v_p}\right) + \phi\right].$$

Which one of the following statements is wrong?

(A) The current can be expressed as

$$I(z,t) = \frac{1}{Z_0} \left\{ A \cos \left[ \omega \left( t - \frac{z}{v_p} \right) + \theta \right] + B \cos \left[ \omega \left( t + \frac{z}{v_p} \right) + \phi \right] \right\}$$

, where  $Z_0$  is the characteristic impedance of the transmission line.

- (B) If B is zero, there is no standing wave on the transmission line.
- (C) The first term and the second term represent the waves going in the  $\pm z$  and  $\pm$ z directions, respectively.
- (D)  $\omega/v_p$  is the propagation constant.
- 14. (4%) A 50- $\Omega$  transmission line is terminated by a load. Which one of the following statements is wrong?
  - (A) If the load impedance is 0  $\Omega$  and the electrical length of the transmission line is 90 degree, the input impedance is  $\infty$ .
  - (B) If the load impedance is 100  $\boldsymbol{\Omega}$  and the electrical length of the transmission line is 90 degree, the input impedance is 20  $\Omega$ .
  - (C) If the load impedance is 200  $\Omega$  and the electrical length of the transmission line is 180 degree, the input impedance is 200  $\Omega$ .
  - (D) If the load impedance is 30  $\boldsymbol{\Omega}$  and the electrical length of the transmission line is 360 degree, the input impedance is 30  $\Omega_{\cdot}$

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15. (4%) For the system impedance of  $Z_0$ , what is the component which can match the impedance at point A to point B along the constant VSWR circle as shown in Fig. 1?

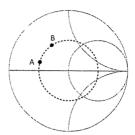


Fig. 1

- (A) A series capacitor.
- (B) A series resistor.
- (C) A series transmission line with characteristic impedance of  $Z_0$ .
- (D) A shunt short-circuited transmission line with characteristic impedance of  $Z_0$ .
- 16. (4%) Which one cannot allow TEM wave propagation?
  - (A) Rectangular metal waveguide.
  - (B) Coaxial cable.
  - (C) Parallel-plate waveguide.
  - (D) Stripline.
- 17. (4%) For a rectangular metallic waveguide with dimensions of a = 4 cm and b = 2 cm, which one of the following statements is wrong?
  - (A) The mode with the lowest cutoff frequency is the dominate mode.
  - (B) The dominant mode is  $TE_{10}$  mode.
  - (C) In the frequency range between the cutoff frequencies of  $TE_{10}$  and  $TE_{11}$  modes, only one mode is allowed to propagate in the waveguide.
  - (D) The rectangular metallic waveguide can be treated as a high-pass filter.
- 18. (4%) In the system shown in Fig. 2, which one of the following statements is wrong?

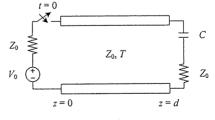


Fig. 2

- (A)  $V(z,t) = V_0/2$  for z = 0 and 0 < t < T.
- (B) The voltage across the capacitor, C, is 0 when t = T.
- (C) The reflection voltage at z = d is 0 when t = T.
- (D) V(z,t) at z=d will be  $V_0/2$  as t tends to infinity.

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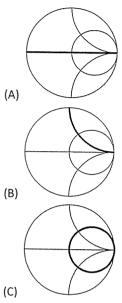
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19. (4%) Which thick line on the Smith chart represents purely real reflection coefficients?



- (D) None of the above.
- 20. (4%) Fig. 3 shows the equivalent circuit for an infinitesimal section of transmission line. For a low-loss transmission line, we assume  $\omega L >> R$  and  $\omega C >>$ G, which one of the following statements is wrong?

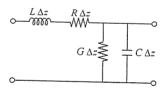


Fig. 3

- (A) Characteristic impedance  $\approx \sqrt{L/C}$ .
- (B) Propagation constant  $\approx \omega \sqrt{LC}$ .
- (C)  $\it L$  accounts for the magnetic field due to current flow.
- (D) R accounts for the dielectric loss.
- 21. (4%) A short-ended 50- $\Omega$  transmission line is operated at 2 GHz. The wavelength of the transmission line at 2 GHz is 10 cm. Which length can make the input impedance of the short-ended transmission line to be capacitive?
  - (A) 1.25 cm.
  - (B) 2.5 cm.
  - (C) 3.75 cm.
  - (D) None of the above.

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22. (4%) A parallel plate waveguide is filled by the dielectric with  $\varepsilon = 9\varepsilon_0$  and  $\mu = \mu_0$ . If the cutoff frequency of TE<sub>1,0</sub> mode for the waveguide is 10 GHz, find the spacing, d, between the two plate.

- (A) 1 cm.
- (B) 0.5 cm.
- (C) 1/3 cm.
- (D) None of the above.
- 23. (4%) Fig. 4 shows the reflection and transmission of an obliquely incident uniform plane wave on a plane boundary between two different perfect dielectric media. Which one of the following statements is wrong?

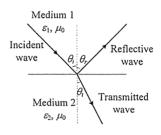


Fig. 4

- (A)  $\theta_r = \theta_i$ .
- (B) For the case of normal incident, the reflection coefficients of perpendicular polarization and parallel polarization are equal.
- (C) If  $\theta_i > \sin^{-1}\sqrt{\varepsilon_2/\varepsilon_1}$ , the time average power of the incident wave is entirely reflected.
- (D) If an elliptically polarization wave incidents with  $\theta_{\rm i}=\tan^{-1}\sqrt{\varepsilon_1/\,\varepsilon_2}$  , the reflected wave will be linearly polarized perpendicular to the plane of incidence
- 24. (6%) Fig. 5(a) and (b) represent the standing wave patterns of a transmission line terminated by a short circuit and an unknown load  $(Z_L)$ , respectively. If the  $d_{min}$  is  $\lambda_a/4$  and the characteristic impedance of the transmission line and the source impedance are both 50  $\Omega$ , what is the impedance of  $Z_{\ell}$ ? ( $\lambda_g$ : wavelength of the transmission line)

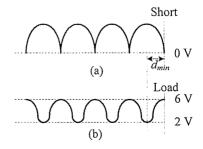


Fig. 5

- (A)  $30 j 40 \Omega$ .
- (B) 16.67  $\Omega$ .
- (C) 150  $\Omega$ .
- (D) None of the above.