



1. A liquid flows through a capillary with an inside radius  $R=10^{-3}$  m and a length  $L=0.4$  m. The viscosity of the liquid is  $1.5 \times 10^{-3}$  Pa·s. The velocity distribution inside the capillary is

$$v = 0.3 \left[ 1 - \left( \frac{r}{R} \right)^2 \right] \text{ m/s, where } r \text{ is the radial coordinate.}$$

- (a) What is the volumetric flow rate? (10%)  
 (b) What is the pressure drop  $\Delta p$  across the capillary during flow? (10%)

Hint: the flux of r-momentum in the flow direction  $\tau = \frac{\Delta p}{2L} r$

2. An oil with heat capacity  $c_p = 2.5$  kJ/kg·K is flowing through a double-pipe heat exchanger at a rate of 7500 kg/h and is to be cooled from 373 K to 343 K. Cooling water ( $c_p = 4.187$  kJ/kg·K) entering at 298 K and flowing **counterflow** at a rate of 3500 kg/h is available.

- (a) Calculate the outlet temperature of the cooling water (5%)  
 (b) Calculate the overall heat transfer coefficient in  $\text{W/m}^2 \cdot \text{K}$  if the heat-transfer area inside the heat exchanger is  $6.5 \text{ m}^2$  (10%)

3. A Newtonian fluid is confined between two parallel infinite plates with a distance  $B$  apart. The lower plate is moving leftward at a constant velocity  $v_0$  and the upper plate is moving rightward at a constant velocity  $2v_0$ . The pressure gradient in the flow is  $\frac{P_0 - P_L}{L}$ . Assuming that the flow is steady-state and laminar and gravity is negligible, find the velocity distribution (15%)



4. 利用逆流式套管熱交換器(countercurrent double-pipe heat exchanger)，以  $105^{\circ}\text{C}$  凝結水蒸汽(condensing steam)將空氣自  $30^{\circ}\text{C}$  加熱至  $80^{\circ}\text{C}$ 。假設主要熱傳阻力控制在空氣熱對流部份。已知空氣熱對流的熱傳係數(h)經驗式為  $Nu = 0.023 Re^{0.8} Pr^{0.4}$ ，式中 Nu 為納瑟數(Nusselt number)、Re 為雷諾數(Reynolds number)、Pr 為普蘭多數(Prandtl number)。若改用  $120^{\circ}\text{C}$  凝結水蒸汽加熱空氣同樣自  $30^{\circ}\text{C}$  加熱至  $80^{\circ}\text{C}$ ，試問所加熱空氣的流量為原所加熱空氣流量的多少倍？ (15 分)
5. 有一液珠懸浮於靜止不動氣體中，液珠成分為 A，氣體為 A 和 B。若 B 不溶於 A，而 A 自液珠表面蒸發，然後擴散至氣相中。因液珠很小可視為球狀，假設液體之蒸發速率緩慢，液珠的半徑 R 可視為不變。試推導出計算液珠蒸發速率的方程式。 (20 分)
6. 在  $298\text{K}$  及  $1\text{atm}$  下，一填料塔(packing tower)中利用有機胺溶液吸收二氧化碳。氣體進入時含  $1.26\text{ mol}\%$  的二氧化碳，離去時含  $0.04\text{ mol}\%$ 。假設在操作條件範圍，二氧化碳與有機胺溶液間平衡關係遵守亨利定律(Henry's law)，亦即  $y_{\text{CO}_2} = 1.575x_{\text{CO}_2}$ 。氣體流速為  $2.3\text{ g}\cdot\text{mol}/\text{s}$ ，液體流速為  $4.8\text{ g}\cdot\text{mol}/\text{s}$ 。已知填料塔直徑為  $40\text{ cm}$ ，總體質傳係數(overall mass transfer coefficient) 與單位體積的表面積的乘積  $K_y a$  為  $5.0 \times 10^{-5}\text{ mol}/(\text{cm}^3\cdot\text{s})$ ，試計算填料塔高為多少 m? (15 分)