

# 元智大學 101 學年度研究所 碩士班 招生試題卷

系(所)別： 資訊管理學系碩士班

組別： 資管組 A

科目： 統計學

用紙第 / 頁共 2 頁

●不可使用電子計算機

無計算或無說明過程 不予計分

1. Please state the definition for the following terms:  
(a) Sample space (4%). (b) Event (4%). (c) Random Variable (4%).
2. In answering a question on a multiple choice test, John either knows the answer or he guesses. Let  $p$  be the probability that John knows the answer and  $1-p$  the probability that he guesses. Assume that John who guesses at the answer will be correct with probability  $1/m$ . What is the conditional probability that John knew the answer to a question given that he answered it correctly? (8%)
3. Compute the expectation (expected value) of a Poisson random variable with parameter  $\lambda$ . (8%)
4. Suppose the random variable  $X$  can assume only the values 1, 2, 3, 4, and 5, each with probability 0.2. Let  $Y = X^2$ . Compute the coefficient of correlation between  $X$  and  $Y$ . (8%)
5. Mary is designing a study concerning the weight of college students. She wants to determine the appropriate number of students she should sample for the study. Mary feels she can tolerate a 0.2 deviation between the sample mean and the true mean. She is willing to take a risk of 0.05. And past research has reported a standard deviation that is approximately 0.6. How many subjects should Mary sample? (8%)
6. John has collected  $n$  pairs  $(x_i, y_i)$  of real data to develop a linear regression line  $y = a + bx$ . Now he intends to use the same data to develop another regression line of the form  $y = \alpha \cdot \beta^x$ . Please explain how you can use the linear regression technique to obtain  $\alpha$  and  $\beta$ . (12%)
7. The following table shows the distribution of the daily number of power failures reported in Taiwan on  $n$  days, where  $\sum_{i=0}^4 n_i = n$ . Please describe how you test at the significance level  $\alpha$  whether the daily power failures in Taiwan may be regarded as a Poisson random variable. (12%)

Number of failures	0	1	2	3	4
Number of days	$n_0$	$n_1$	$n_2$	$n_3$	$n_4$

8. If  $s^2$  is the variance of a random sample of size  $n$  taken from a normal distribution having the variance, Please show how you determine the  $1-\alpha$  confidence interval for  $\sigma^2$ . (12%)
9. Suppose that an experimenter has available the results of  $k$  independent random samples, each of size  $n$ , from  $k$  different populations. We are concerned with testing the hypothesis that the means of these  $k$  populations are all equal. Let  $y_{ij}$  denote the  $j$ th observation in the  $i$ th sample,  $\bar{y}_i$  denote the mean of the  $i$ th sample, and  $\bar{y}$  denote the overall mean of all observations.
  - (a) Show that  $\sum_{i=1}^k \sum_{j=1}^n (y_{ij} - \bar{y})^2 = \sum_{i=1}^k \sum_{j=1}^n (y_{ij} - \bar{y}_i)^2 + n \cdot \sum_{i=1}^k (\bar{y}_i - \bar{y})^2$  (10%)
  - (b) Please describe step-by-step how you test the hypothesis at the significance level  $\alpha$ . (10%)

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