

國立宜蘭大學

101 學年度研究所碩士班考試入學

統計學試題

(應用經濟與管理學系經營管理碩士班)

准考證號碼：

《作答注意事項》

1. 請先檢查准考證號碼、座位號碼及答案卷號碼是否相符。
2. 考試時間：100 分鐘。
3. 本試卷共有 3 大題，共計 100 分。
4. 請將答案寫在答案卷上。
5. 考試中禁止使用大哥大或其他通信設備。
6. 考試後，請將試題卷及答案卷一併繳交。
7. 本試卷採雙面影印，請勿漏答。
8. 本考科所需電子計算機由本校提供。

一、解釋名詞 (每一題 5 分，合計 25 分)

1. 分層隨機抽樣 (Stratified Random Sampling)
2. 一致性 (Consistency)
3. 變異係數 (Coefficient of Variation)
4. 偏判定係數 (Partial Determination Coefficient)
5. 互斥事件 (Mutually Exclusive Event)

二、選擇題 (每一題 7 分，合計 35 分)

1. In a questionnaire, respondents are asked to mark their gender as male or female. Gender is an example of the
(A) ordinal scale
(B) nominal scale
(C) ratio scale
(D) interval scale
(E) None of these alternatives is correct.
2. For any continuous random variable, the probability that the random variable takes on exactly a specific value is
(A) 1.00
(B) 0.50
(C) any value between 0 to 1
(D) almost zero
(E) None of these alternatives is correct.
3. In computing the standard error of the mean, the finite population correction factor is used when
(A) $N/n > 0.05$
(B) $N/n \leq 0.05$
(C) $n/N > 0.05$
(D) $n/N \leq 30$
(E) None of these alternatives is correct.
4. The standard deviation of a point estimator is called the
(A) standard deviation
(B) standard error
(C) point estimator
(D) variance of estimation
(E) None of these alternatives is correct.

5. If we change a 95% confidence interval estimate to a 99% confidence interval estimate, we can expect
- (A) the size of the confidence interval to increase
 - (B) the size of the confidence interval to decrease
 - (C) the size of the confidence interval to remain the same
 - (D) the sample size to increase
 - (E) None of these alternatives is correct.

三、計算題 (每一大題 10 分，合計 40 分)

1. 量販店王經理欲瞭解某自有品牌飲料的銷售情況，抽取最近 10 天每日的銷售記錄(單位：萬(C.C.))為樣本，取得資料分別如下：

| 編號 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|--------|---|---|----|---|----|---|----|----|----|----|
| 銷售量(x) | 2 | 7 | 13 | 8 | 12 | 4 | 24 | 10 | 11 | 9 |

- (1) 請根據上述的樣本資料，繪製其之盒形圖(box plot)。
 - (2) 此組樣本資料是否有潛在離群值(outliers)存在？若有，請寫出您的依據。
2. 設某特殊型燈管之壽命(單位：小時)服從如下的機率分配：

$$f(x) = \frac{1}{\theta^2} x e^{-\frac{x}{\theta}}, x > 0$$

今若獨立地檢驗 n 個此種燈管，得其壽命分別為 X_1, X_2, \dots, X_n 。試求參數 θ 的最大概似估計量(maximum likelihood estimator)。

3. 某公司記錄其產品 7 個月的銷售量(Y)(單位：千元)與廣告費用(X)(單位：千元)，並得到如下的訊息：

$$\sum_{i=1}^7 x_i = 490, \sum_{i=1}^7 x_i^2 = 35528, \sum_{i=1}^7 y_i = 902, \sum_{i=1}^7 y_i^2 = 116630, \sum_{i=1}^7 x_i y_i = 63759$$

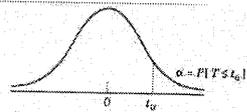
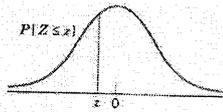
請在顯著水準 0.05 下，檢定銷售量(Y)與廣告費用(X)的相關係數是否為 0？

4. 某研究員欲瞭解三種不同藥物的治療程序對於解除頭痛之平均時間長度是否相同。因此，隨機將參與實驗的頭痛患者分派至此三種治療程序中，並得到下列訊息：

| 治療程序 | 樣本數 | 平均值 | 變異數 |
|------|-----|------|-----|
| 1 | 4 | 14.0 | 6.0 |
| 2 | 5 | 17.0 | 8.5 |
| 3 | 4 | 16.5 | 7.0 |

現若假定每種程序解除頭痛之時間長度的母體服從常態分配且變異數相等，則請在顯著水準 0.05 下，檢定此三種治療程序解除頭痛的平均時間長度是否相同。

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 統計學教科



| z | .00 | .01 | .02 | .03 | .04 | .05 | .06 | .07 | .08 | .09 |
|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| -3.5 | .0002 | .0002 | .0002 | .0002 | .0002 | .0002 | .0002 | .0002 | .0002 | .0002 |
| -3.4 | .0003 | .0003 | .0003 | .0003 | .0003 | .0003 | .0003 | .0003 | .0003 | .0003 |
| -3.3 | .0005 | .0005 | .0005 | .0004 | .0004 | .0004 | .0004 | .0004 | .0004 | .0003 |
| -3.2 | .0007 | .0007 | .0006 | .0006 | .0006 | .0006 | .0006 | .0005 | .0005 | .0005 |
| -3.1 | .0010 | .0009 | .0009 | .0009 | .0008 | .0008 | .0008 | .0007 | .0007 | .0007 |
| -3.0 | .0013 | .0013 | .0012 | .0012 | .0012 | .0011 | .0011 | .0011 | .0010 | .0010 |
| -2.9 | .0019 | .0018 | .0018 | .0017 | .0016 | .0016 | .0015 | .0015 | .0014 | .0014 |
| -2.8 | .0026 | .0025 | .0024 | .0023 | .0023 | .0022 | .0021 | .0021 | .0020 | .0020 |
| -2.7 | .0035 | .0034 | .0033 | .0032 | .0031 | .0030 | .0029 | .0028 | .0027 | .0026 |
| -2.6 | .0047 | .0045 | .0044 | .0043 | .0041 | .0040 | .0039 | .0038 | .0037 | .0036 |
| -2.5 | .0062 | .0060 | .0059 | .0057 | .0055 | .0054 | .0052 | .0051 | .0049 | .0048 |
| -2.4 | .0082 | .0080 | .0078 | .0075 | .0073 | .0071 | .0069 | .0066 | .0064 | .0063 |
| -2.3 | .0107 | .0104 | .0102 | .0099 | .0096 | .0094 | .0091 | .0089 | .0087 | .0084 |
| -2.2 | .0139 | .0136 | .0132 | .0129 | .0125 | .0122 | .0119 | .0116 | .0113 | .0110 |
| -2.1 | .0179 | .0174 | .0170 | .0166 | .0162 | .0158 | .0154 | .0150 | .0146 | .0143 |
| -2.0 | .0228 | .0222 | .0217 | .0212 | .0207 | .0202 | .0197 | .0192 | .0188 | .0183 |
| -1.9 | .0287 | .0281 | .0274 | .0268 | .0262 | .0256 | .0250 | .0244 | .0239 | .0233 |
| -1.8 | .0359 | .0351 | .0344 | .0336 | .0329 | .0322 | .0314 | .0307 | .0301 | .0294 |
| -1.7 | .0446 | .0436 | .0427 | .0418 | .0409 | .0401 | .0392 | .0384 | .0375 | .0367 |
| -1.6 | .0548 | .0537 | .0526 | .0516 | .0505 | .0495 | .0485 | .0475 | .0465 | .0455 |
| -1.5 | .0668 | .0655 | .0643 | .0630 | .0618 | .0606 | .0594 | .0582 | .0571 | .0559 |
| -1.4 | .0808 | .0793 | .0778 | .0764 | .0749 | .0735 | .0721 | .0708 | .0694 | .0681 |
| -1.3 | .0968 | .0951 | .0934 | .0918 | .0901 | .0885 | .0869 | .0853 | .0838 | .0823 |
| -1.2 | .1151 | .1131 | .1112 | .1093 | .1075 | .1056 | .1038 | .1020 | .1003 | .0985 |
| -1.1 | .1357 | .1335 | .1314 | .1292 | .1271 | .1251 | .1230 | .1210 | .1190 | .1170 |
| -1.0 | .1587 | .1562 | .1539 | .1515 | .1492 | .1469 | .1446 | .1423 | .1401 | .1379 |
| -0.9 | .1841 | .1814 | .1788 | .1762 | .1736 | .1711 | .1685 | .1660 | .1635 | .1611 |
| -0.8 | .2119 | .2090 | .2061 | .2033 | .2005 | .1977 | .1949 | .1922 | .1894 | .1867 |
| -0.7 | .2420 | .2389 | .2358 | .2327 | .2297 | .2266 | .2236 | .2206 | .2177 | .2148 |
| -0.6 | .2743 | .2709 | .2676 | .2643 | .2611 | .2578 | .2546 | .2514 | .2483 | .2451 |
| -0.5 | .3085 | .3050 | .3015 | .2981 | .2946 | .2912 | .2877 | .2843 | .2810 | .2776 |
| -0.4 | .3446 | .3409 | .3372 | .3336 | .3300 | .3264 | .3228 | .3192 | .3156 | .3121 |
| -0.3 | .3821 | .3783 | .3745 | .3707 | .3669 | .3632 | .3594 | .3557 | .3520 | .3483 |
| -0.2 | .4207 | .4168 | .4129 | .4090 | .4052 | .4013 | .3974 | .3936 | .3897 | .3859 |
| -0.1 | .4602 | .4562 | .4522 | .4483 | .4443 | .4404 | .4364 | .4325 | .4286 | .4247 |
| 0.0 | .5000 | .4960 | .4920 | .4880 | .4840 | .4801 | .4761 | .4721 | .4681 | .4641 |

| d.f. | .25 | .10 | .05 | .025 | .01 | .00833 | .00625 | .005 |
|------|-------|-------|-------|-------|-------|--------|--------|-------|
| 1 | 3.000 | 3.078 | 3.314 | 3.706 | 5.024 | 5.024 | 5.024 | 5.024 |
| 2 | 1.677 | 1.886 | 2.074 | 2.330 | 3.000 | 3.000 | 3.000 | 3.000 |
| 3 | 1.249 | 1.433 | 1.601 | 1.845 | 2.353 | 2.353 | 2.353 | 2.353 |
| 4 | 1.064 | 1.253 | 1.407 | 1.626 | 2.015 | 2.015 | 2.015 | 2.015 |
| 5 | .940 | 1.133 | 1.277 | 1.462 | 1.753 | 1.753 | 1.753 | 1.753 |
| 6 | .859 | 1.056 | 1.190 | 1.343 | 1.626 | 1.626 | 1.626 | 1.626 |
| 7 | .800 | 1.000 | 1.129 | 1.259 | 1.535 | 1.535 | 1.535 | 1.535 |
| 8 | .750 | .950 | 1.074 | 1.190 | 1.457 | 1.457 | 1.457 | 1.457 |
| 9 | .700 | .900 | 1.020 | 1.129 | 1.389 | 1.389 | 1.389 | 1.389 |
| 10 | .650 | .850 | 0.967 | 1.069 | 1.328 | 1.328 | 1.328 | 1.328 |
| 11 | .600 | .800 | .915 | 1.010 | 1.274 | 1.274 | 1.274 | 1.274 |
| 12 | .550 | .750 | .863 | 0.952 | 1.225 | 1.225 | 1.225 | 1.225 |
| 13 | .500 | .700 | .811 | .897 | 1.181 | 1.181 | 1.181 | 1.181 |
| 14 | .450 | .650 | .759 | .843 | 1.141 | 1.141 | 1.141 | 1.141 |
| 15 | .400 | .600 | .707 | .789 | 1.104 | 1.104 | 1.104 | 1.104 |
| 16 | .350 | .550 | .655 | .735 | 1.070 | 1.070 | 1.070 | 1.070 |
| 17 | .300 | .500 | .603 | .681 | 1.038 | 1.038 | 1.038 | 1.038 |
| 18 | .250 | .450 | .552 | .628 | 1.008 | 1.008 | 1.008 | 1.008 |
| 19 | .200 | .400 | .500 | .575 | 0.980 | 0.980 | 0.980 | 0.980 |
| 20 | .150 | .350 | .447 | .520 | .954 | .954 | .954 | .954 |
| 21 | .100 | .300 | .394 | .464 | .930 | .930 | .930 | .930 |
| 22 | .050 | .250 | .340 | .408 | .907 | .907 | .907 | .907 |
| 23 | .000 | .200 | .287 | .353 | .886 | .886 | .886 | .886 |
| 24 | .000 | .150 | .236 | .299 | .866 | .866 | .866 | .866 |
| 25 | .000 | .100 | .187 | .248 | .847 | .847 | .847 | .847 |
| 26 | .000 | .050 | .140 | .200 | .829 | .829 | .829 | .829 |
| 27 | .000 | .000 | .095 | .154 | .812 | .812 | .812 | .812 |
| 28 | .000 | .000 | .052 | .110 | .796 | .796 | .796 | .796 |
| 29 | .000 | .000 | .011 | .068 | .780 | .780 | .780 | .780 |
| 30 | .000 | .000 | .000 | .028 | .765 | .765 | .765 | .765 |
| 40 | .000 | .000 | .000 | .000 | .708 | .708 | .708 | .708 |
| 50 | .000 | .000 | .000 | .000 | .658 | .658 | .658 | .658 |
| 60 | .000 | .000 | .000 | .000 | .615 | .615 | .615 | .615 |
| 70 | .000 | .000 | .000 | .000 | .578 | .578 | .578 | .578 |
| 80 | .000 | .000 | .000 | .000 | .545 | .545 | .545 | .545 |
| 90 | .000 | .000 | .000 | .000 | .515 | .515 | .515 | .515 |
| 100 | .000 | .000 | .000 | .000 | .488 | .488 | .488 | .488 |

(Continued) Percentage Points of $F(\nu_1, \nu_2)$ Distributions

自由度 1

| d.f. | .99 | .975 | .95 | .90 | .50 | .10 | .05 | .025 | .01 |
|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 161.5 | 189.5 | 215.7 | 224.6 | 230.2 | 234.0 | 236.8 | 238.9 | 240.5 |
| 2 | 18.51 | 19.00 | 19.16 | 19.25 | 19.30 | 19.33 | 19.35 | 19.37 | 19.38 |
| 3 | 10.13 | 9.55 | 9.28 | 9.12 | 9.01 | 8.94 | 8.89 | 8.85 | 8.81 |
| 4 | 7.71 | 6.94 | 6.59 | 6.36 | 6.26 | 6.16 | 6.09 | 6.04 | 6.00 |
| 5 | 6.59 | 5.78 | 5.41 | 5.19 | 5.05 | 4.95 | 4.88 | 4.82 | 4.77 |
| 6 | 5.89 | 5.14 | 4.76 | 4.53 | 4.39 | 4.28 | 4.21 | 4.15 | 4.10 |
| 7 | 5.42 | 4.64 | 4.26 | 4.03 | 3.89 | 3.78 | 3.71 | 3.65 | 3.60 |
| 8 | 5.06 | 4.26 | 3.88 | 3.65 | 3.51 | 3.40 | 3.33 | 3.27 | 3.22 |
| 9 | 4.78 | 3.98 | 3.60 | 3.37 | 3.23 | 3.12 | 3.05 | 2.99 | 2.94 |
| 10 | 4.55 | 3.75 | 3.37 | 3.14 | 3.00 | 2.89 | 2.82 | 2.76 | 2.71 |
| 11 | 4.35 | 3.55 | 3.17 | 2.94 | 2.80 | 2.69 | 2.62 | 2.56 | 2.51 |
| 12 | 4.18 | 3.38 | 3.00 | 2.77 | 2.63 | 2.52 | 2.45 | 2.39 | 2.34 |
| 13 | 4.04 | 3.24 | 2.86 | 2.63 | 2.49 | 2.38 | 2.31 | 2.25 | 2.20 |
| 14 | 3.92 | 3.12 | 2.74 | 2.51 | 2.37 | 2.26 | 2.19 | 2.13 | 2.08 |
| 15 | 3.82 | 3.02 | 2.64 | 2.41 | 2.27 | 2.16 | 2.09 | 2.03 | 1.98 |
| 16 | 3.74 | 2.94 | 2.56 | 2.33 | 2.19 | 2.08 | 2.01 | 1.95 | 1.90 |
| 17 | 3.67 | 2.87 | 2.49 | 2.26 | 2.12 | 2.01 | 1.94 | 1.88 | 1.83 |
| 18 | 3.61 | 2.81 | 2.43 | 2.20 | 2.06 | 1.95 | 1.88 | 1.82 | 1.77 |
| 19 | 3.56 | 2.76 | 2.38 | 2.15 | 2.01 | 1.90 | 1.83 | 1.77 | 1.72 |
| 20 | 3.51 | 2.71 | 2.33 | 2.10 | 1.96 | 1.85 | 1.78 | 1.72 | 1.67 |
| 21 | 3.47 | 2.67 | 2.29 | 2.06 | 1.92 | 1.81 | 1.74 | 1.68 | 1.63 |
| 22 | 3.43 | 2.63 | 2.25 | 2.02 | 1.88 | 1.77 | 1.70 | 1.64 | 1.59 |
| 23 | 3.40 | 2.60 | 2.22 | 1.99 | 1.85 | 1.74 | 1.67 | 1.61 | 1.56 |
| 24 | 3.37 | 2.57 | 2.19 | 1.96 | 1.82 | 1.71 | 1.64 | 1.58 | 1.53 |
| 25 | 3.34 | 2.54 | 2.16 | 1.93 | 1.79 | 1.68 | 1.61 | 1.55 | 1.50 |
| 26 | 3.32 | 2.52 | 2.14 | 1.91 | 1.77 | 1.66 | 1.59 | 1.53 | 1.48 |
| 27 | 3.30 | 2.50 | 2.12 | 1.89 | 1.75 | 1.64 | 1.57 | 1.51 | 1.46 |
| 28 | 3.28 | 2.48 | 2.10 | 1.87 | 1.73 | 1.62 | 1.55 | 1.49 | 1.44 |
| 29 | 3.26 | 2.46 | 2.08 | 1.85 | 1.71 | 1.60 | 1.53 | 1.47 | 1.42 |
| 30 | 3.25 | 2.45 | 2.07 | 1.84 | 1.70 | 1.59 | 1.52 | 1.46 | 1.41 |
| 40 | 3.18 | 2.39 | 2.01 | 1.77 | 1.65 | 1.54 | 1.47 | 1.41 | 1.36 |
| 50 | 3.13 | 2.34 | 1.96 | 1.72 | 1.60 | 1.49 | 1.42 | 1.36 | 1.31 |
| 60 | 3.09 | 2.30 | 1.92 | 1.68 | 1.56 | 1.45 | 1.38 | 1.32 | 1.27 |
| 70 | 3.06 | 2.27 | 1.89 | 1.65 | 1.53 | 1.42 | 1.35 | 1.29 | 1.24 |
| 80 | 3.04 | 2.25 | 1.87 | 1.63 | 1.51 | 1.40 | 1.33 | 1.27 | 1.22 |
| 90 | 3.02 | 2.23 | 1.85 | 1.61 | 1.49 | 1.38 | 1.31 | 1.25 | 1.20 |
| 100 | 3.01 | 2.22 | 1.84 | 1.60 | 1.48 | 1.37 | 1.30 | 1.24 | 1.19 |

自由度 2

| d.f. | .99 | .975 | .95 | .90 | .50 | .10 | .05 | .025 | .01 |
|------|-------|------|------|------|-------|-------|-------|-------|-------|
| 1 | .0002 | .001 | .004 | .02 | .45 | 2.71 | 3.84 | 5.02 | 6.63 |
| 2 | .02 | .05 | .10 | .21 | 1.39 | 4.61 | 5.99 | 7.38 | 9.21 |
| 3 | .11 | .22 | .35 | .58 | 2.37 | 6.25 | 7.81 | 9.35 | 11.34 |
| 4 | .30 | .48 | .71 | 1.06 | 3.36 | 7.78 | 9.49 | 11.14 | 13.28 |
| 5 | .55 | .83 | 1.15 | 1.61 | 4.35 | 9.24 | 11.07 | 12.83 | 15.09 |
| 6 | .87 | 1.24 | 1.64 | 2.20 | 5.35 | 10.64 | 12.59 | 14.45 | 16.81 |
| 7 | 1.24 | 1.69 | 2.17 | 2.83 | 6.35 | 12.02 | 14.07 | 16.01 | 18.48 |
| 8 | 1.65 | 2.18 | 2.73 | 3.49 | 7.34 | 13.36 | 15.51 | 17.53 | 20.09 |
| 9 | 2.09 | 2.70 | 3.33 | 4.17 | 8.34 | 14.68 | 16.92 | 19.02 | 21.67 |
| 10 | 2.56 | 3.24 | 3.94 | 4.87 | 9.34 | 15.99 | 18.31 | 20.48 | 23.21 |
| 11 | 3.05 | 3.81 | 4.57 | 5.58 | 10.34 | 17.28 | 19.68 | 21.92 | 24.72 |
| 12 | 3.57 | 4.40 | 5.23 | 6.30 | 11.34 | 18.55 | 21.03 | 23.34 | 26.22 |
| 13 | 4.11 | 5.01 | 5.89 | 7.04 | 12.34 | 19.81 | 22.36 | 24.74 | 27.69 |
| 14 | 4.66 | 5.62 | 6.57 | 7.79 | 13.34 | 21.06 | 23.68 | 26.12 | 29.14 |