

## 國立臺灣科技大學103學年度碩士班招生試題

系所組別： 自動化及控制研究所碩士班乙組

科 目： 控制系統

(總分為100分)

1. A block diagram of a servomotor with tachometer feedback is shown as Figure 1.
- When  $D(s) = 0$ , find the error signal  $E(s)$  in the presence of the reference input  $X(s)$ . (7%)
  - When  $X(s) = 0$ , find the error signal  $E(s)$  in the presence of the disturbance input  $D(s)$ . (7%)
  - When  $X(s)$  is a unit step and  $D(s) = 0$ , calculate the steady-state error of the system. (7%)
  - When  $D(s)$  is a unit ramp and  $X(s) = 0$ , calculate the steady-state error of the system. (7%)

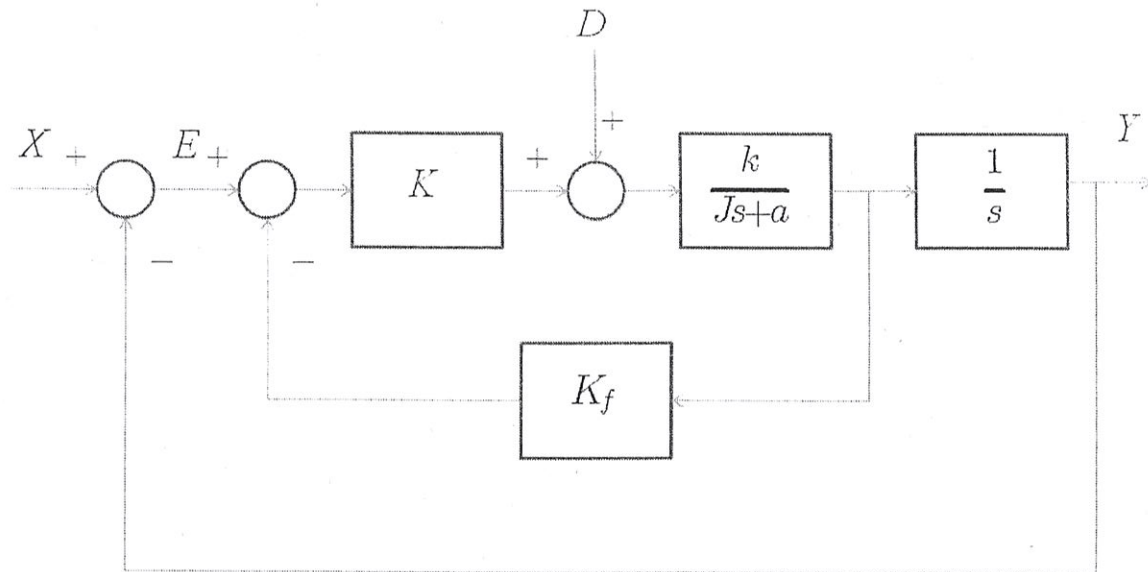


Figure 1



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2.

(a) Consider the characteristic equation of a linear time-invariant closed-loop system:  $s^3 + (k_3 + 3)s^2 + (k_2 + 4)s + k_1 = 0$ , where  $k_1$ ,  $k_2$ , and  $k_3$  are real constants. Using Routh-Hurwitz criterion, determine the constraints for  $k_1$ ,  $k_2$ , and  $k_3$  so that the closed-loop system is stable. (7%)

(b) Using Routh-Hurwitz criterion, determine the stability of the closed-loop system that has the characteristic equation:

$$s^4 + 2s^3 + 10s^2 + 20s + 5 = 0. \text{ (7\%)}$$

3. (8%) A unity feedback control system has the open-loop transfer function:

$$G(s) = \frac{A}{s(s+a)}.$$

Compute the sensitivity of the closed-loop transfer function to changes in the parameter  $A$ .

4. Consider a system as  $\dot{x} = \begin{bmatrix} -3 & -2 \\ 0 & 1 \end{bmatrix} x + \begin{bmatrix} 2 \\ 1 \end{bmatrix} u$  and  $y = [1 \ 1]x$ .

(a) (10%) Find the transfer function of the system.

(b) (10%) Find  $x_1(t)$  and  $x_2(t)$  when  $u(t)=0$  for  $t \geq 0$ ,  $x_1(0)=1$  and

$$x_2(0) = 2.$$



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5. Consider a stable control system with unity feedback as follows (figure 2)

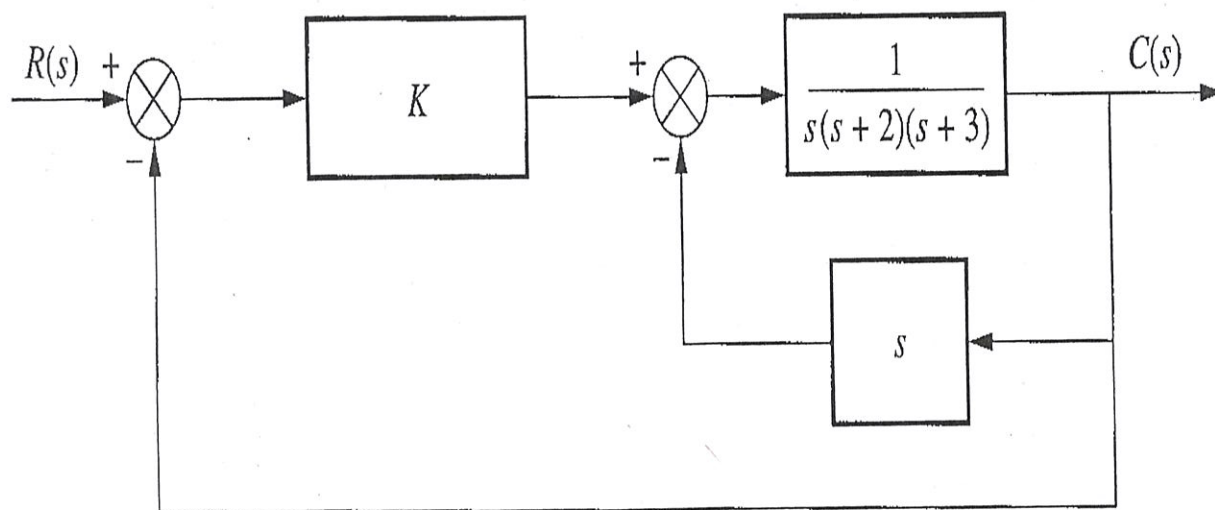


Figure 2

- (a) (5%) What type is the system?  
(b) (5%) Please find the corresponding error constant.



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6. Given the following Bode plot (figure 3) for a system  $KG(s)$  with  $K=1$ .

(a) (5%) Please estimate the phase margin of the system.

(b) (5%) For what range of  $K$  value the system will be stable?

(c) (10%) Please write an approximate transfer function for  $G(s)$ .

Be sure to state how you get those numbers.

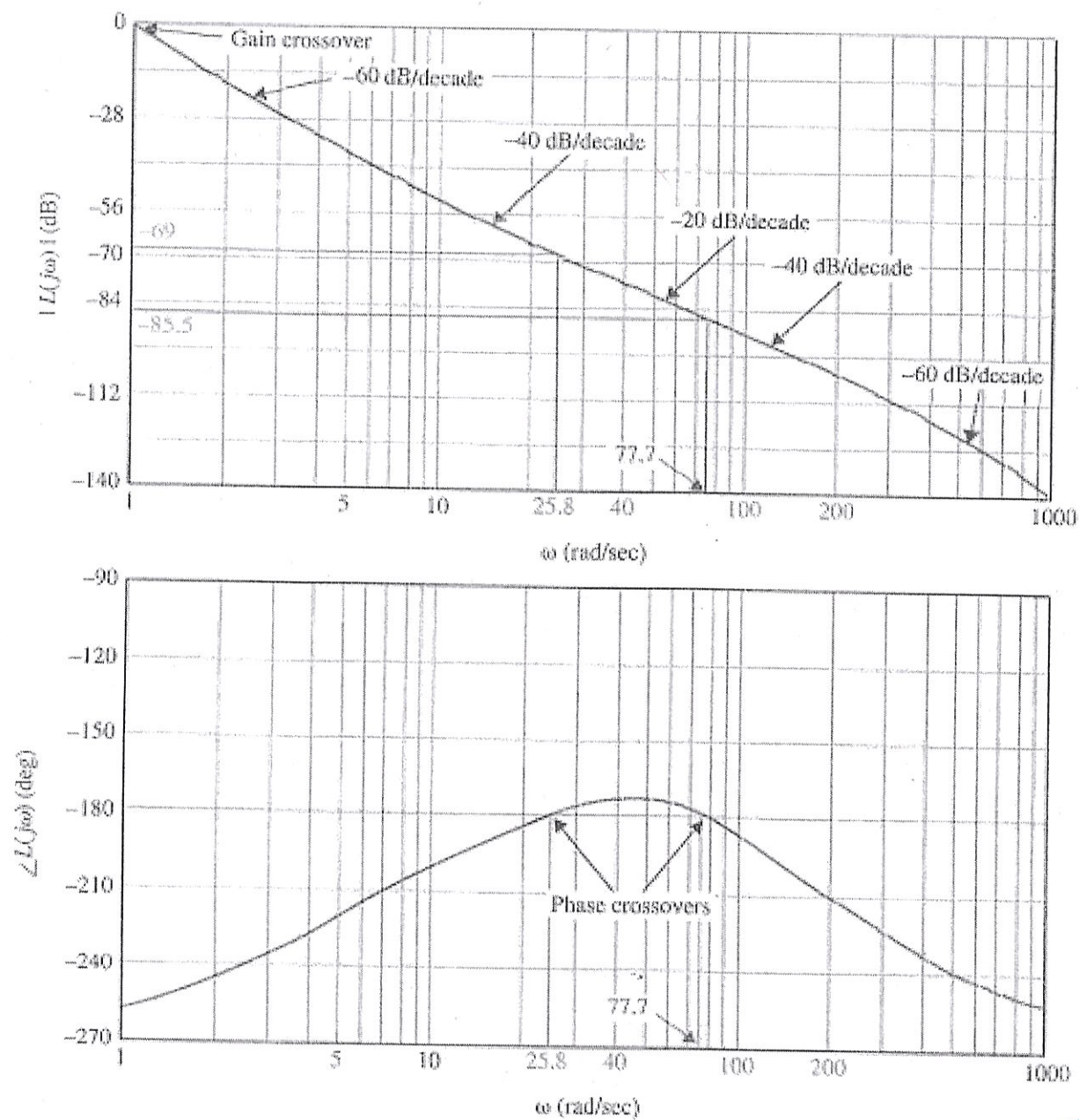


Figure 3.

