國立高雄大學 103 學年度研究所碩士班招生考試試題

科目:工程數學 系所:應用物理學系 是否使用計算機:是 本科原始成績:100分

1. (10%) Solve the differential equation $(y+1)y'' = (y')^2$.

2. (10%) Solve the initial-value problem.

$$y'' - y = x + \sin x$$
, $y(0) = 2$, $y'(0) = 3$

3. (15%) Find the eigenvalues and eigenvectors of the matrix.

$$\mathbf{A} = \begin{bmatrix} 2 & -1 & 0 \\ 5 & 2 & 4 \\ 0 & 1 & 2 \end{bmatrix}$$

4. (10%) Use the inverse of coefficient matrix to solve the system.

$$x_1 + 2x_2 + 2x_3 = 1$$

$$x_1 - 2x_2 + 2x_3 = -3$$

$$3x_1 - x_2 + 5x_3 = 7$$

5. (10%) Use the Laplace transform to solve the initial-value problem.

$$y'' - 4y' + 4y = t^3$$
, $y(0) = 1$, $y'(0) = 0$

6. (10%) Find the Fourier series of the function.

$$f(x) = \begin{cases} x+1, & -1 < x < 0 \\ x-1, & 0 \le x < 1 \end{cases}$$

- 7. (10%) Evaluate $\oint_C \frac{e^{2z}}{z^4 + 2z^3 + 2z^2} dz, \text{ where the contour } C \text{ is circle } |z| = 4.$
- 8. (10%) Find the length of the graph of $r = 2 2\cos\theta$ from $\theta = 0$ to $\theta = 2\pi$.
- 9. (15%) Evaluate the surface integral $\iint_S (y^2 + 2yz)dS$, where S is the first-octant

portion of the plane 2x + y + 2z = 6.