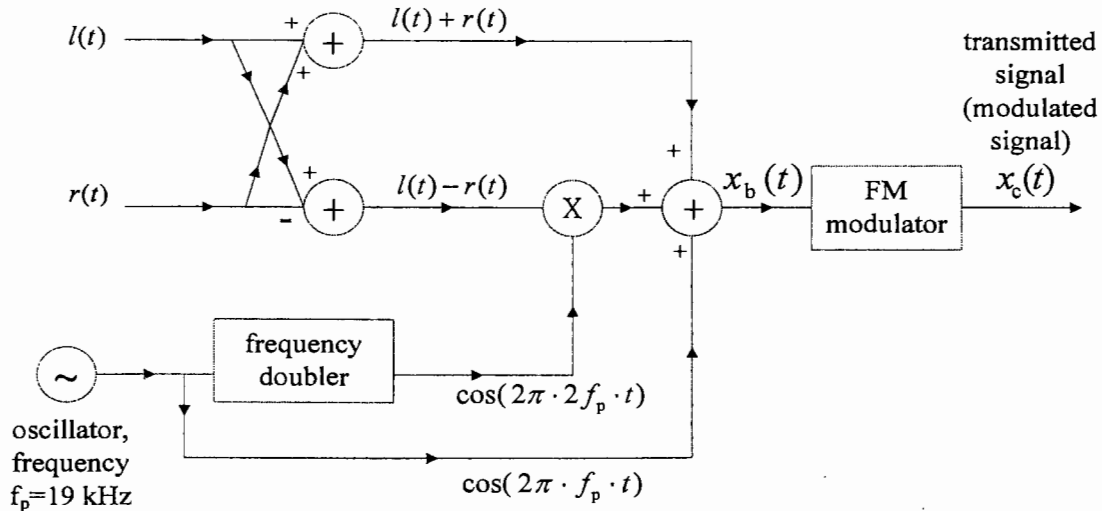
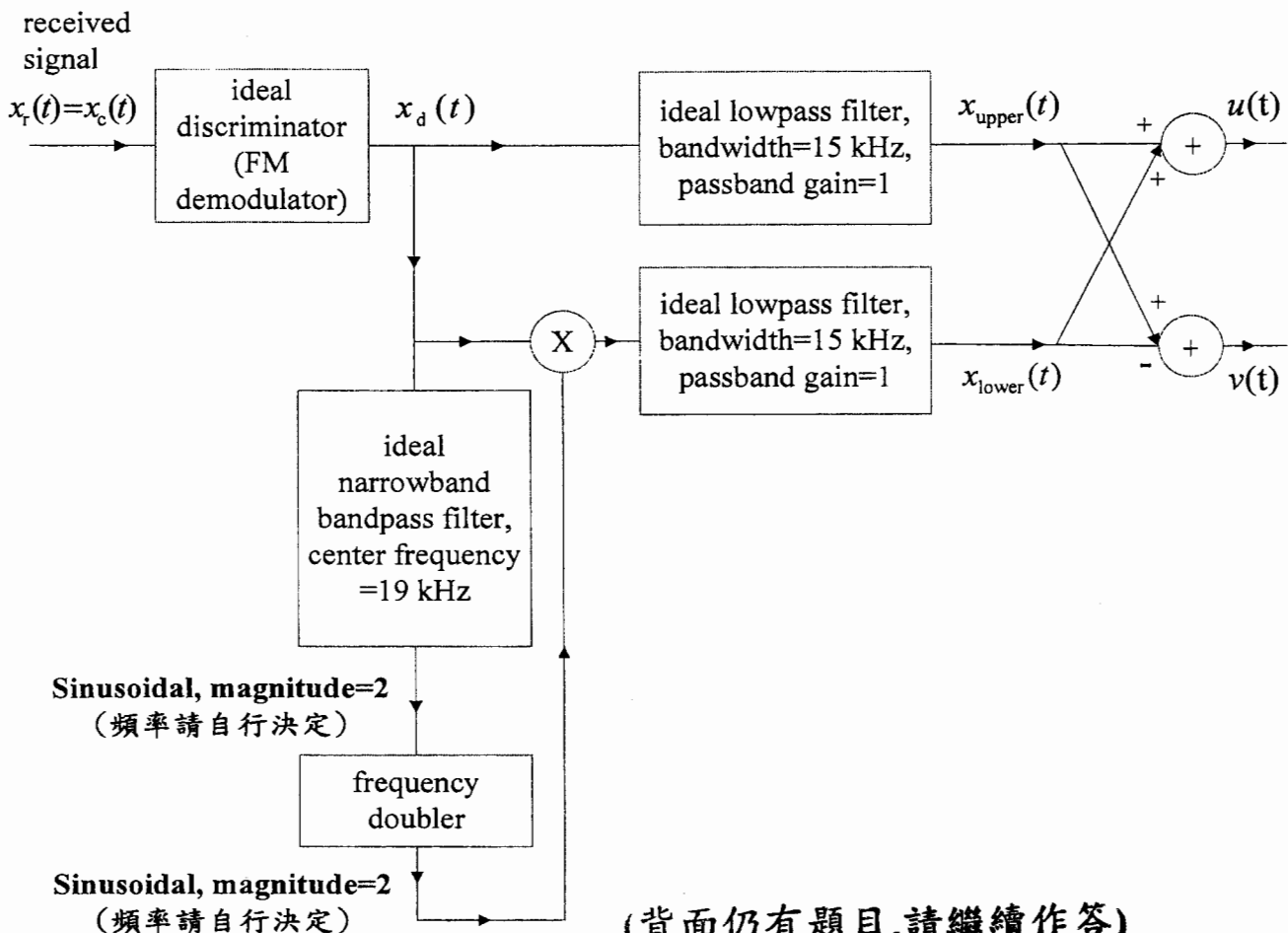


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1. Consider the modulator structure shown below. (本大題 20%)



The two message signals to be transmitted,  $l(t)$  and  $r(t)$ , are both bandlimited with bandwidth=15 kHz. The transmitted signal is given by  $x_c(t) = A_c \cos(\omega_c t + \phi(t))$  where  $A_c$  is a constant,  $\omega_c$  is the carrier frequency (rad/sec),  $\phi(t) = K_f \int_{-\infty}^t x_b(\alpha) d\alpha$  is the phase deviation, and  $K_f$  is the frequency deviation constant. Let us assume that the received signal  $x_r(t)$  is exactly the same as the transmitted signal  $x_c(t)$ . The received signal is processed by the demodulator structure shown below, where  $u(t) = x_{upper}(t) + x_{lower}(t)$  and  $v(t) = x_{upper}(t) - x_{lower}(t)$ .



(背面仍有題目,請繼續作答)

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(a) Determine  $u(t)$ . Use the following model for the ideal discriminator shown in the demodulator structure:

$$x_d(t) = \frac{K_d}{2\pi} \frac{d\theta(t)}{dt} \text{ where } K_d \text{ is the discriminator constant. (10\%)}$$

(b) Is this demodulator structure a coherent demodulator? Justify your answer. If your answer is a yes, explain what the modulator does to facilitate coherent demodulation and what the demodulator does to obtain a coherent reference. If your answer is a no, briefly explain how the noncoherent demodulator works. (5%)

(c) 本題之 modulator structure 讓你聯想到與哪些類比調變方法有何相似之處? (5%)

[Note: 你的答案應包含: "XX 部份和 XXX modulation scheme 相似, 因為...(簡要說明相似點)". 必須寫出二個相似點。]

2. Consider the DSB-SC (double-sideband suppressed carrier) system in which the transmitted signal is given by  $x_c(t) = m(t)\cos(\omega_c t + \theta_0)$  where  $m(t)$  represents the message signal,  $\omega_c$  is the carrier frequency (rad/sec), and  $\theta_0$  represents the initial phase of the oscillator at the transmitter. Let us assume that the received signal  $x_r(t)$  is given by  $x_r(t) = x_c(t - \tau_0)$  where  $\tau_0$  denotes the propagation delay. Demonstrate how you can recover  $m(t - \tau_0)$  from  $x_r(t)$  in a coherent manner.

[Note] (a) You can assume that the receiver can achieve perfect carrier synchronization by using, for example, the phase-locked loop techniques. (b) You need to draw the block diagram of the coherent demodulator that you design, in addition to mathematically showing that your design actually works. (本大題 10%)

3. Consider the following LTI system

$$y(n) = \alpha x(n) + (1 - \alpha)y(n - 1)$$

where

$\alpha > 0$ : a real-valued constant,

$x(n)$ : input of the system,

$y(n)$ : output of the system with  $y(n)=0$  for  $n<0$ . (本大題 20%)

(a) Draw the block diagram of this system. (5%)

(b) Determine the unit impulse response of this system. Is this system a finite impulse response (FIR) or infinite impulse response (IIR) system? Justify your answer. (5%)

(c) Determine the range of  $\alpha$  such that this system is stable. (5%)

(d) Determine the unit impulse response of the inverse of the system. (5%)

4. Compare the bandwidth efficiencies  $R_b/B$ , where  $R_b$  and  $B$  are respectively bit rate and null-to-null bandwidth, of various M-ary digital modulation schemes, including the PSK, QAM, coherent FSK and non-coherent FSK. Note that the minimum frequency separation is assumed for FSK. (本大題 20%)

5. Consider the non-coherent FSK with the transmitted signals as

$$s_1(t) = A\cos(\omega_c t + \theta), 0 \leq t \leq T$$

and

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$$s_2(t) = A \cos((w_c + \Delta w)t + \theta), 0 \leq t \leq T$$

where  $\Delta w$  is sufficiently large that  $s_1(t)$  and  $s_2(t)$  occupy different spectral regions. The AWGN channel environment with noise power  $N$  is assumed. Calculate the error probability.

Note that the Ricean probability density function can be expressed as

$$f_R(r) = \frac{r}{\sigma^2} \exp\left(-\frac{r^2 + A^2}{2\sigma^2}\right) I_0\left(\frac{rA}{\sigma^2}\right), r \geq 0$$

where  $A$  is the amplitude of the specular component;  $\sigma^2$  is the variance of each quadrature diffuse component;  $I_0(u)$  is the modified Bessel function of the first kind and order zero. (本大題 15%)

6. Consider a two-hypothesis decision problem where

$$f_Z\left(\frac{z}{H_1}\right) = \frac{\exp\left(-\frac{1}{2}z^2\right)}{\sqrt{2\pi}}$$

and

$$f_Z\left(\frac{z}{H_2}\right) = \frac{1}{2} \exp(-|z|)$$

(a) Find the likelihood ratio  $\Lambda(Z)$ . (5%)

(b) Letting the threshold  $\eta$  be arbitrary, find the decision region  $R_1$  and  $R_2$ . Note that both  $R_1$  and  $R_2$  cannot be connected regions for this problem; that is, they will involve a multiplicity of line segments. (10%) (本大題 15%)