

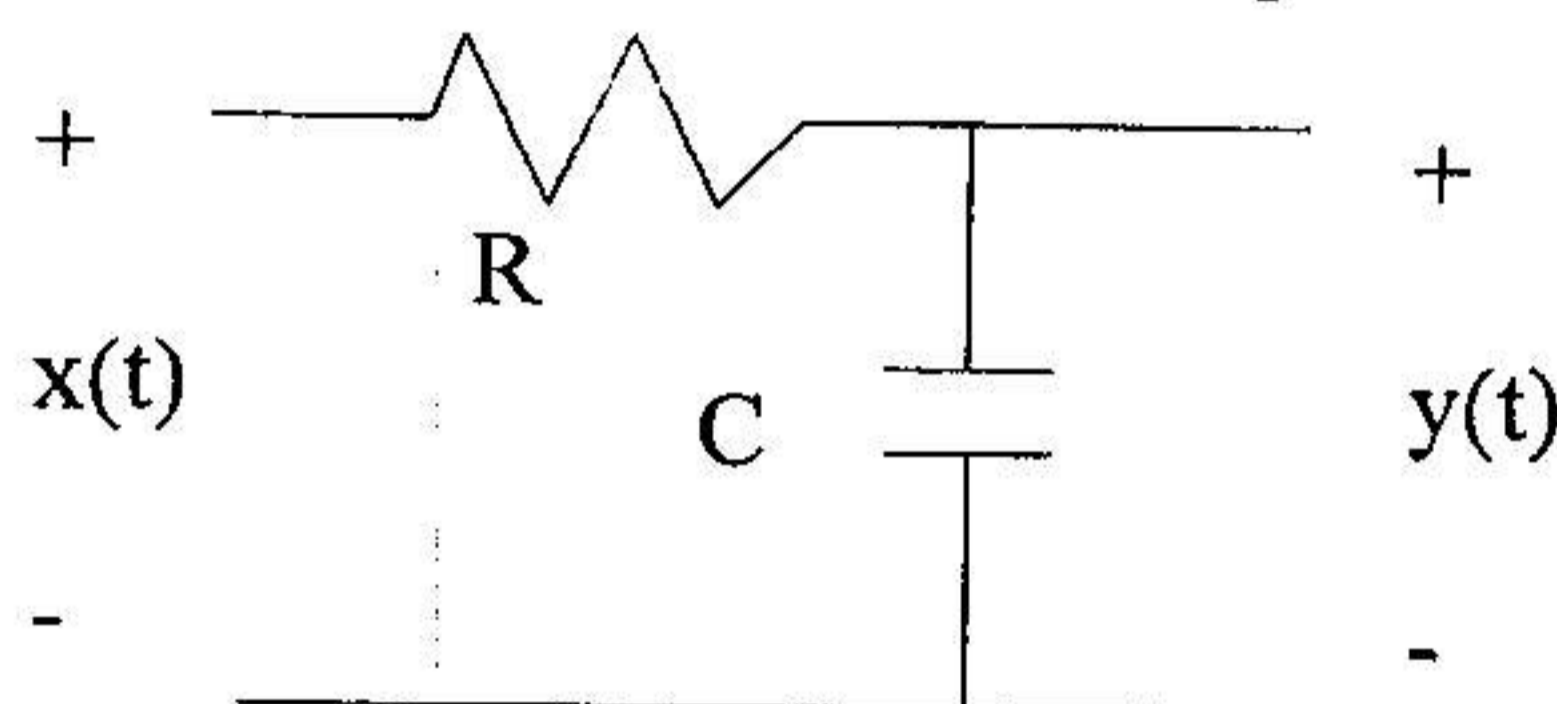
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注意：考生請務必依以下 3 項規定做答，違者不予給分!!

- 一、本試卷共五大題，務要依題號順序(1,2,3,4,5)做答於答案卷上。
- 二、每題均要由一空白頁開始作答，不論會不會寫，均要清楚編明題號。
- 三、每題均分(a), (b)兩小題，每小題中有 underline 處表示答題重點，請針對重點作答，並在答案卷上清楚標示所要求的圖形及答案。(答非所問及字跡難以辨認者均不給分)

題目開始

1. Consider a communication channel which is modeled as a low-pass RC filter shown below:



where  $R=10^3$  Ohms and  $C=100 \mu\text{F}$ .

- (a) Sketch the two output waveforms  $y_1(t)$  and  $y_2(t)$  for the 2-impulse input  $x_1(t) = \delta(t) - \delta(t-1)$  and square-wave input  $x_2(t) = 2 \times \text{rect}(t-1.5)$ , respectively. (10%)
  - (b) Find the average power of the output  $y(t)$  for the DC-plus-sinusoid input  $x(t) = 2 + \cos(10t)$ . (10%)
2. Consider a passband signal  $x(t) = \cos(2\pi \times 11t) + \cos(2\pi \times 15t) + \text{sinc}(t) \times \cos(2\pi \times 13t)$  which is to be down-converted to baseband I/Q signals. Assume the I/Q down-converter multiplies  $x(t)$  by two orthogonal LO carriers  $\{2 \times \cos(2\pi \times 12t), 2 \times \sin(2\pi \times 12t)\}$ , and the cutoff frequency of the output ideal LPF is  $f_c = 2.5$  Hz
    - (a) Find the output I component  $y_I(t)$  from the I/Q down-converter. (10%)
    - (b) If the input to the specified down-converter is only AWGN with PSD  $N_0/2 = 10^{-4}$  W/Hz, find the first-order PDF  $f_R(r)$  of the corresponding output envelope  $R(t) = \sqrt{y_I^2(t) + y_Q^2(t)}$ . (10%)
3. An analog bipolar message signal  $m(t)$  is transmitted using a QPSK system with the following specifications:
    - The message bandwidth is  $W=5$  kHz.
    - Uniform quantization is used, and the quantization error should be less than 0.1% of  $\max\{m(t)\}$ .
    - The system bit rate is  $R_b=200$  kbps
    - The transmitter uses a square-root raised cosine baseband pulse shaping with a rolloff factor of  $\alpha=0.5$ .
    - The carrier frequency is  $f_c = 10$  MHz.
    - The passband QPSK signal  $s(t)$  has a transmitted power of 1 W.
    - (a) Find the oversampling ratio  $\text{OSR} = f_s/f_{\text{Nyquist}}$  at which the message signal  $m(t)$  is sampled, where  $f_s$  is the sampling frequency, and  $f_{\text{Nyquist}}$  is the Nyquist rate. (10%)
    - (b) Find and sketch the power spectrum density (PSD)  $S(f)$  of the QPSK signal. You should accurately mark all important values for  $S(f)$  on the two axes. (10%)

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4. Consider an 8-ary signaling scheme. The signaling waveform in a symbol duration  $T = 1$  sec can be expressed as

$$s(t) = \sqrt{\frac{1}{3}} \sum_{k=1}^3 a_k \phi_k(t) \quad 0 \leq t \leq T$$

where  $\mathbf{a} = [a_1 \ a_2 \ a_3] = [\pm 1 \ \pm 1 \ \pm 1]$  denotes the 8-ary symbol, and the set  $\{\phi_1(t), \phi_2(t), \phi_3(t)\}$  forms the orthonormal basis in  $0 \leq t \leq 1$ . Assume the waveform  $s(t)$  is passing through an AWGN channel with noise PSD  $N_0/2 = 10^{-1}$  W/Hz, and the channel output is denoted as  $x(t)$ .

- (a) Sketch the **signal constellation** and define the **decision region** for the particular symbol  $\mathbf{a}_0 = [1 \ 1 \ 1]$ . (10%)  
 (b) Assume equally likely symbols and gray coding, find the **bit error rate**  $P_b$  of the optimum receiver. (10%)

5. A quaternary symbol sequence  $x_n \in \{-3, -1, 1, 3\}$  is passing through a cascade of three LTI filters, including the transmit (TX) pulse shaping filter with frequency response  $G(f) = \mathcal{F}\{g(t)\} = 0.1 \times \text{rect}(0.01f)$ , then the physical channel with impulse response  $c(t) = \delta(t) + \delta(t-0.01)$  plus an AWGN noise  $w(t)$  with PSD  $N_0/2 = 10^{-4}$  W/Hz, finally the receive (RX) filter with impulse response  $h(t)$  matched to  $g(t)$ , i.e.,  $h(t) = g(-t)$ . The transmit signal at the TX filter output can be expressed as  $s(t) = \sum_{n=-\infty}^{\infty} x_n g(t - 0.01n)$ , and the RX filter output is expressed as  $y(t) = s(t) \otimes c(t) \otimes h(t) + n(t)$ , where  $\otimes$  denotes convolution integral, and  $n(t) = w(t) \otimes h(t)$  is the output noise. Let  $y_n = y(nT_s)$  denote the sampled signal of  $y(t)$  at the sampling rate  $f_s = 1/T_s = 100$  Hz.

- (a) Assume equally likely symbols, find the **signal-to-noise ratio** (SNR) in dB at the RX filter output. (10%)  
 (b) Under noise-free situation, find the discrete-time relation between  $x_n$  and  $y_n$ , and devise a **receiver structure** to recover  $y_n$  from  $x_n$ . Discuss the major advantage and disadvantage of your receiver. (10%)