

本試題是否可以使用計算機： 可使用， 不可使用（請命題老師勾選）

考試日期：0301，節次：2

[1] Answer the following questions with a choice (single choice) of T (True), F (False) and C (case by case). (30%)

- (a) Once the value of  $K_D$  of a PD controller is fixed, increasing the value of  $K_P$  will increase the phase margin monotonically.
- (b) Adding a zero to the loop transfer function will always increase the bandwidth of the closed-loop system.
- (c) The phase-lead controller may not be effective if the negative slope of the uncompensated process transfer function is too steep near the gain-crossover frequency.
- (d) Nichols chart can be used to find BW and  $M_r$  information of a closed-loop system.
- (e) Bode plot can be used for stability analysis for minimum- as well as nonminimum-phase transfer functions.
- (f) The following characteristic equation of a continuous-data system represents an unstable system since it contains a negative coefficient.
- $$s^3 - s^2 + 5s + 10 = 0$$
- (g) Increasing the undamped natural frequency will generally reduce the rise time of the step response.
- (h) The following transfer function  $G(s)$  can be approximated by  $G_L(s)$  since the pole at  $-20$  is much larger than the dominant pole at  $s = -1$
- $$G(s) = \frac{10}{s(s+1)(s+20)} \quad G_L = \frac{10}{s(s+1)}$$
- (i) Given the equation:  $1 + KG_1(s)H_1(s) = 0$ , where  $G_1(s)H_1(s)$  is a rational function of  $s$ , and does not contain  $K$ , the roots of  $\frac{dG_1(s)H_1(s)}{ds}$  are all breakaway points on the root loci ( $-\infty < K < \infty$ ).
- (j) Without modification, all the rules and properties for the construction of root loci in the  $s$ -plane can be applied to the construction of root loci of discrete-data systems in the  $z$ -plane.

[2] Consider the discrete-time system

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+1) \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 2 & 0 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} r(k), \quad y(k) = \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix}$$

With  $r(k) = u(k) - u(k-2)$ , where  $u(k)$  is the unit-step input, and  $x_1(0) = 0, x_2(0) = 0$

Find  $y(k)$  (10%)

(背面仍有題目,請繼續作答)

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[3] The block diagram of a linearized idle-speed engine-control system of an automobile is shown in Fig. 1. The system is linearized about a nominal operating point, so all the variables represent linear-perturbed quantities. The following variables are defined:  $T_m(t)$  is the engine torque;  $T_D$  the constant load-disturbance torque;  $\omega(t)$ , the engine speed;  $u(t)$ , the input-voltage to the throttle actuator; and  $\alpha$ , the throttle angle. The time delay in the engine model can be approximated by (20%)

$$e^{-0.2s} \cong \frac{1 - 0.1s}{1 + 0.1s}$$

(a) Draw a state diagram for the system by decomposing each block individually. Assign the state variable from right to left in ascending order.

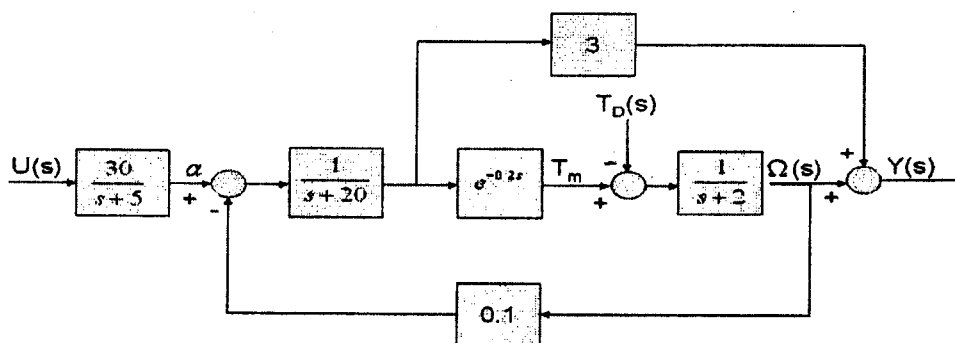


FIG. 1

(b) Write the state equation from the state diagram obtained in part (a), in the form of

$$\frac{dx(t)}{dt} = Ax(t) + B \begin{bmatrix} u(t) \\ T_D(t) \end{bmatrix}$$

(c) Write  $Y(s)$  as a function of  $U(s)$  and  $T_D(s)$ . Write  $\Omega(s)$  as a function of  $U(s)$  and  $T_D(s)$ .

[4] The block diagram of a feedback control system is shown in Fig. 2 (15%)

(a) Apply the Nyquist criterion to determine the range of  $K$  for stability.  
 (b) Check the answer obtained in part (a) with the Routh-Hurwitz criterion.

$$G(s) = \frac{K}{(s+4)(s+5)}$$

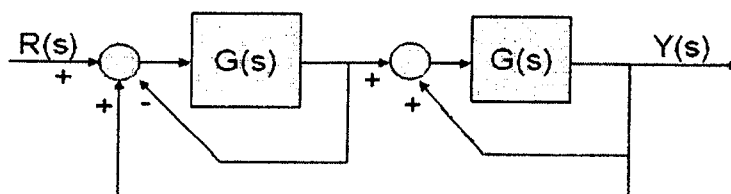


FIG. 2

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[5] A block diagram of a control system is shown in Fig. 3. (15%)

- (a) Determine the system completely state controllable and observable of the systems, conditions on the A, B, C, and D matrices.
- (b) Determine the system completely state controllable and observable of the systems, conditions on the pole-zero cancellation of the transfer function  $Y(s)/U(s)$ .

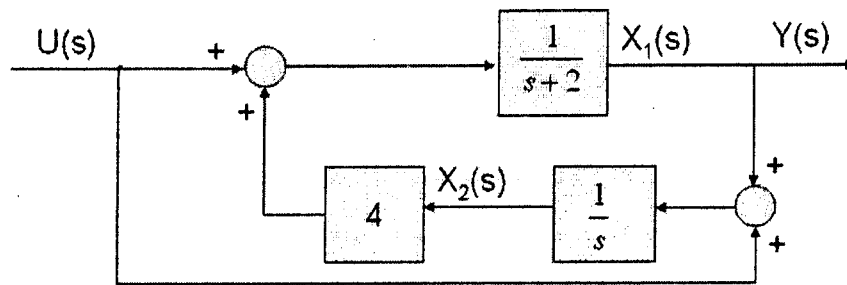


FIG. 3

[6] A R-C circuit system is shown in Fig4. The fixed parameter of the system are given as  $R=1\Omega, C=1F$ . (10%)

- (a) Find the transfer function  $\frac{Y(z)}{R(z)}$
- (b) When input voltage  $r(t) = e^{-t}$ , Find output voltage  $y(kT)$ .

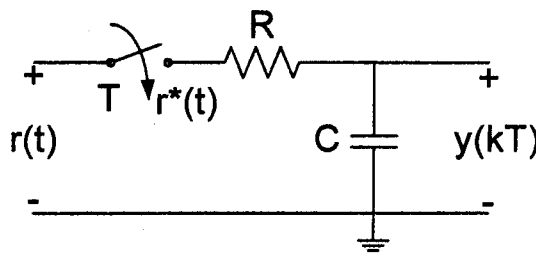


FIG. 4